## 編號： 271

國立成功大學102學年度碩士班招生考試試題

## 系所組別：工業與資訊管理學系甲，乙，丙組

## 考試科目：統計學

## ※ 考生請注意：本試題可使用計算機

－．（15\％）The joint density of X and Y is given by
$f(x, y)= \begin{cases}6 x^{2} \mathrm{y}, & 0 \leq \mathrm{x} \leq 1,0 \leq \mathrm{y} \leq 1 \\ 0, & \text { otherwise }\end{cases}$
a．Find the mean and the variance of $X$ ．
b．Find the mean and the variance of $Y$ ．
c．Find the conditional distribution of X given Y ．

二．（ $10 \%$ ）A newly married couple decides to continue having children until they have one of each sex．If the events of having a boy and a girl are independent and equiprobable，how many children should this couple expect？
Hint：Note that $\sum_{i=1}^{\infty} i r^{i}=r /(1-r)^{2},|r|<1$ ．

三．（ $10 \%$ ）Let X be a normal random variable with mean $\mu$ and unit variance．We want to test the hypothcsis $\mu=5$ at the $5 \%$ level of significance，using $n$ independent samples of X ．
a．What is the range of values of the sample mean for which the hypothesis is accepted？
b．Let $n=10$ ．Calculate the probability of accepting the hypothesis $\mu=5$ when the true value of $\mu$ is 4 ．

四．（ $15 \%$ ）The NBA final is a seven game series，and the first team to win four games wins the series．Denote by $p$ the probability that the Eastern Conference team wins a game and by $q=1-p$ that the Western Conference team wins a game． Assume that these probabilities remain constant from game to game and that the outcomes of the games are mutually independent．Assume that the probability that the series ends in $j$ games is given by
$\binom{j-1}{3}\left[p^{4} q^{j-4}+q^{4} p^{j-4}\right], j=4,5,6,7$.
There have been 52 finals in NBA＇s history（from 1947 to 1998）．The number of finals that have gone for 4，5， 6 and 7 games has been as follows：
4 games： 6 finals， 5 games： 11 finals， 6 games： 21 finals， 7 games： 14 finals．

Suppose we assume that the two finalists are evenly matched，so that $p=q=1 / 2$ ．Show that the above model fits these data well．
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五，A company designed four training programs about statistics for the students who will take the admission exam for a specific master program．The general manager of the company wants to know whether the four training programs have significantly different performance．The performance of a training program is evaluated by the mean scores of the students trained by the program．A student is a junior or a senior from college of management，engineering，or social science．
1．（5\％）State how to collect data when a completely randomized design is used．
2．（5\％）State how to collect data when a randomized block design is used．
3．（5\％）State how to collect data when the interaction between training programs and the colleges of students is also interested．

六，The manager of a coffee shop believes that the sales of coffee depend upon the weather．He has taken a sample of five days as shown below．

| Cups of Coffee Sold | Temperature |
| :---: | :---: |
| 350 | 50 |
| 200 | 60 |
| 210 | 70 |
| 100 | 80 |
| 60 | 90 |
| 40 | 100 |

1．（5\％）Use the method of least squares to compute an estimated regression line．
2．（5\％）Interpret the regression line．
3．（5\％）Compute the coefficient of determination and interpret．

七，（ $10 \%$ ）The temperatures in Tainan for the past seven days are $82,80,84,83,80,79$ ，and 82 ．Determine whether a constant 0.2 or 0.3 used for exponential smoothing is better for predicting the temperature data．

八，Answer the following two questions about nonparametric methods for statistics．
1．（5\％）What does＇nonparametric＇mean？
2．（5\％）When should a nonparametric method be used for analyzing data？

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TABLE 3 CHI－SQUARE DISTRIBUTION


Entries in the table give $\chi_{\alpha}^{2}$ values，where $\alpha$ is the area or probability in the upper tail of the chi－square distribution．
For example，with 10 degrees of freedom and a .01 area in the upper tail，$\chi_{.01}^{2}=23.209$ ．

| Degrees of Freedom | Area in Upper Tail |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | ． 995 | ． 99 | ． 975 | ． 95 | ． 90 | ． 10 | ． 05 | ． 025 | ． 01 | ． 005 |
| 1 | ． 000 | ． 000 | ． 001 | ． 004 | ． 016 | 2.706 | 3.841 | 5.024 | 6.635 | 7.879 |
| 2 | ． 010 | ． 020 | ． 051 | ． 103 | ． 211 | 4.605 | 5.991 | 7.378 | 9.210 | 10.597 |
| 3 | ． 072 | ． 115 | ． 216 | ． 352 | ． 584 | 6.251 | 7.815 | 9.348 | 11.345 | 12.838 |
| 4 | ． 207 | ． 297 | ． 484 | ． 711 | 1.064 | 7.779 | 9.488 | 11.143 | 13.277 | 14.860 |
| 5 | ． 412 | ． 554 | ． 831 | 1.145 | 1.610 | 9.236 | 11.070 | 12.832 | 15.086 | 16.750 |
| 6 | ． 676 | 872 | 1.237 | 1.635 | 2.204 | 10.645 | 12.592 | 14.449 | 16.812 | 18.548 |
| 7 | ． 989 | 1.239 | 1.690 | 2.167 | 2.833 | 12.017 | 14.067 | 16.013 | 18.475 | 20.278 |
| 8 | 1.344 | 1.647 | 2.180 | 2.733 | 3.490 | 13.362 | 15.507 | 17.535 | 20.090 | 21.955 |
| 9 | 1.735 | 2.088 | 2.700 | 3.325 | 4.168 | 14.684 | 16.919 | 19.023 | 21.666 | 23.589 |
| 10 | 2.156 | 2.558 | 3.247 | 3.940 | 4.865 | 15.987 | 18.307 | 20.483 | 23.209 | 25.188 |
| 11 | 2.603 | 3.053 | 3.816 | 4.575 | 5.578 | 17.275 | 19.675 | 21.920 | 24.725 | 26.757 |
| 12 | 3.074 | 3.571 | 4.404 | 5.226 | 6.304 | 18.549 | 21.026 | 23.337 | 26.217 | 28.300 |
| 13 | 3.565 | 4.107 | 5.009 | 5.892 | 7.041 | 19.812 | 22.362 | 24.736 | 27.688 | 29.819 |
| 14 | 4.075 | 4.660 | 5.629 | 6.571 | 7.790 | 21.064 | 23.685 | 26.119 | 29.141 | 31.319 |
| 15 | 4.601 | 5.229 | 6.262 | 7.261 | 8.547 | 22.307 | 24.996 | 27.488 | 30.578 | 32.801 |
| 16 | 5.142 | 5.812 | 6.908 | 7.962 | 9.312 | 23.542 | 26.296 | 28.845 | 32.000 | 34.267 |
| 17 | 5.697 | 6.408 | 7.564 | 8.672 | 10.085 | 24.769 | 27.587 | 30.191 | 33.409 | 35.718 |
| 18 | 6.265 | 7.015 | 8.231 | 9.390 | 10.865 | 25.989 | 28.869 | 31.526 | 34.805 | 37.156 |
| 19 | 6.844 | 7.633 | 8.907 | 10.117 | 11.651 | 27.204 | 30.144 | 32.852 | 36.191 | 38.582 |
| 20 | 7.434 | 8.260 | 9.591 | 10.851 | 12.443 | 28.412 | 31.410 | 34.170 | 37.566 | 39.997 |
| 21 | 8.034 | 8.897 | 10.283 | 11.591 | 13.240 | 29.615 | 32.671 | 35.479 | 38.932 | 41.401 |
| 22 | 8.643 | 9.542 | 10.982 | 12.338 | 14.041 | 30.813 | 33.924 | 36.781 | 40.289 | 42.796 |
| 23 | 9.260 | 10.196 | 11.689 | 13.091 | 14.848 | 32.007 | 35.172 | 38.076 | 41.638 | 44.181 |
| 24 | 9.886 | 10.856 | 12.401 | 13.848 | 15.659 | 33.196 | 36.415 | 39.364 | 42.980 | 45.558 |
| 25 | 10.520 | 11.524 | 13.120 | 14.611 | 16.473 | 34.382 | 37.652 | 40.646 | 44.314 | 46.928 |
| 26 | 11.160 | 12.198 | 13.844 | 15.379 | 17.292 | 35.563 | 38.885 | 41.923 | 45.642 | 48.290 |
| 27 | 13.808 | 12.878 | 14.573 | 16.151 | 18.114 | 36.741 | 40.113 | 43.195 | 46.963 | 49.645 |
| 28 | 12.461 | 13.565 | 15.308 | 16.928 | 18.939 | 37.916 | 41.337 | 44.461 | 48.278 | 50.994 |
| 29 | 13.121 | 14.256 | 16.047 | 17.708 | 19.768 | 39.087 | 42.557 | 45．72？ | 49.588 | 52.335 |

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