编號: 271

國立成功大學102學年度碩士班招生考試試題

共4月 頁,第**1**頁

考試日期:0224, 節次:3

系所組別: 工業與資訊管理學系甲、乙、丙組

考試科目: 統計學

※ 考生請注意:本試題可使用計算機

-. (15%) The joint density of X and Y is given by

 $f(x, y) = \begin{cases} 6x^2y, & 0 \le x \le 1, 0 \le y \le 1\\ 0, & \text{otherwise} \end{cases}$

- a. Find the mean and the variance of X.
- b. Find the mean and the variance of Y.
- c. Find the conditional distribution of X given Y.

Hint: Note that
$$\sum_{i=1}^{\infty} ir^{i} = r / (1-r)^{2}$$
, $|r| < 1$.

- \equiv . (10%) Let X be a normal random variable with mean μ and unit variance. We want to test the hypothesis $\mu = 5$ at the 5% level of significance, using *n* independent samples of X.
 - a. What is the range of values of the sample mean for which the hypothesis is accepted?
 - b. Let n=10. Calculate the probability of accepting the hypothesis $\mu = 5$ when the true value of μ is 4.
- [2]. (15%) The NBA final is a seven game series, and the first team to win four games wins the series. Denote by p the probability that the Eastern Conference team wins a game and by q=1-p that the Western Conference team wins a game. Assume that these probabilities remain constant from game to game and that the outcomes of the games are mutually independent. Assume that the probability that the series ends in j games is given by

$$\binom{j-1}{3}\left[p^4q^{j-4}+q^4p^{j-4}\right], j=4,5,6,7.$$

There have been 52 finals in NBA's history (from 1947 to 1998). The number of finals that have gone for 4, 5, 6 and 7 games has been as follows: 4 games: 6 finals, 5 games: 11 finals, 6 games: 21 finals, 7 games: 14 finals.

Suppose we assume that the two finalists are evenly matched, so that p = q = 1/2. Show that the above model fits these data well.

背面仍有題目,請繼續作答)

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- Ξ A company designed four training programs about statistics for the students who will take the admission exam for a specific master program. The general manager of the company wants to know whether the four training programs have significantly different performance. The performance of a training program is evaluated by the mean scores of the students trained by the program. A student is a junior or a senior from college of management, engineering, or social science.
 - 1. (5%) State how to collect data when a completely randomized design is used.
 - 2. (5%) State how to collect data when a randomized block design is used.
 - 3. (5%) State how to collect data when the interaction between training programs and the colleges of students is also interested.
- \Rightarrow The manager of a coffee shop believes that the sales of coffee depend upon the weather. He has taken a sample of five days as shown below.

Cups of Coffee Sold 350 200 210 100 60	Temperature				
350	50				
200	60				
210	70				
100	80				
60	90				
40	100				

- 1. (5%) Use the method of least squares to compute an estimated regression line.
- 2. (5%) Interpret the regression line.
- 3. (5%) Compute the coefficient of determination and interpret.
- t
 \(10%)
 The temperatures in Tainan for the past seven days are 82, 80, 84, 83, 80, 79, and 82.
 Determine
 whether a constant 0.2 or 0.3 used for exponential smoothing is better for predicting the temperature data.
- 八、Answer the following two questions about nonparametric methods for statistics.
 - 1. (5%) What does 'nonparametric' mean?
 - 2. (5%) When should a nonparametric method be used for analyzing data?

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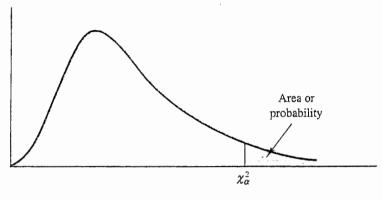
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TABLE 3 CHI-SQUARE DISTRIBUTION



Entries in the table give χ_a^2 values, where α is the area or probability in the upper tail of the chi-square distribution. For example, with 10 degrees of freedom and a .01 area in the upper tail, $\chi_{.01}^2 = 23.209$.

Degrees of Freedom		Area in Upper Tail									
	.995	.99	.975	.95	.90	.10	.05	.025	.01	.005	
- 1	.000	.000	.001	.004	.016	2.706	3.841	5.024	6.635	7.879	
2	.010	.020	.051	.103	.211	4.605	5.991	7.378	9.210	10.597	
CT 03	.072	.115	.216	.352	.584	6.251	7.815	9.348	11.345	12.838	
4	.207	.297	.484	.711	1.064	7.779	9.488	11.143	13.277	14.860	
5	.412	.554	.831	1.145	1.610	9.236	11.070	12.832	15.086	16.750	
6	.676	.872	1.237	1.635	2.204	10.645	12.592	14.449	16.812	18.548	
7	.989	1.239	1.690	2.167	2.833	12.017	14.067	16.013	18.475	20.278	
8	1.344	1.647	2.180	2.733	3.490	13.362	15.507	17.535	20.090	21.955	
9	1.735	2.088	2.700	3.325	4.168	14.684	16.919	19.023	21.666	23.589	
10	2.156	2.558	3.247	3.940	4.865	15.987	18.307	20.483	23.209	25.188	
11	2.603	3.053	3.816	4.575	5.578	17.275	19.675	21.920	24.725	26.757	
12	3.074	3.571	4.404	5.226	6.304	18.549	21.026	23.337	26.217	28.300	
13	3.565	4.107	5.009	5.892	7.041	19.812	22.362	24. 73 6	27.688	29.819	
14	4.075	4.660	5.629	6.571	7.790	21.064	23.685	26.119	29.141	31.319	
15	4.601	5.229	6.262	7.261	8.547	22.307	24.996	27.488	30.578	32.801	
16	5.142	5.812	6.908	7.962	9.312	23,542	26.296	28.845	32.000	34.267	
17	5.697	6.408	7.564	8.672	10.085	24.769	27.587	30.191	33.409	35.718	
18	6.265	7.015	8.231	9.390	10.865	25.989	28.869	31.526	34.805	37.156	
19	6.844	7.633	8.907	10.117	11.651	27.204	30.144	32.852	36.191	38.582	
20	7.434	8.260	9.591	10.851	12.443	28.412	31.410	34.170	37.566	39.997	
21	8.034	8.897	10.283	11.591	13.240	29.615	32.671	35.479	38.932	41.401	
22	8.643	9.542	10.982	12.338	14.041	30.813	33.924	36.781	40.289	42.796	
23	9.260	10.196	11.689	13.091	14.848	32.007	35.172	38.076	41.638	44.181	
24	9.886	10.856	12.401	13.848	15.659	33.196	36.415	39.364	42.980	45.558	
25	10.520	11.524	13.120	14.611	16.473	34.382	37.652	40.646	44.314	46.928	
26	11.160	12.198	13.844	15.379	17.292	35.563	38.885	41.923	45.642	48.290	
27	11.808	12.878	14.573	16.151	18.114	36.741	40.113	43.195	46.963	49.645	
28	12.461	13.565	15.308	16.928	18.939	37.916	41.337	44.461	48.278	50.994	
29	13.121	14.256	16.047	17.708	19.768	39.087	42.557	45.722	49.588	52.335	

(背面仍有題目,請繼續作答)

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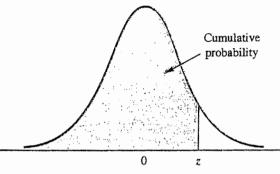
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CUMULATIVE PROBABILITIES FOR THE STANDARD NORMAL DISTRIBUTION



Entries in the table give the area under the curve to the left of the z value. For example, for z = 1.25, the cumulative probability is .8944.

z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
.0	.5000	.5040	.5080	.5120	.5160	.5199	.5239	.5279	.5319	.5359
.1	.5398	.5438	.5478	.5517	.5557	.5596	.5636	.5675	.5714	.5753
.2	.5793	.5832	.5871	.5910	.5948	.5987	.6026	.6064	.6103	.6141
.3	.6179	.6217	.6255	.6293	.6331	.6368	.6406	.6443	.6480	.6517
.4	.6554	.6591	.6628	.6664	.6700	.6736	.6772	.6808	.6844	.6879
.5	.6915	.6950	.6985	.7019	:7054	.7088	.7123	.7157	.7190	.7224
.6	.7257	.7291	.7324	.7357	.7389	.7422	.7454	.7486	.7517	.7549
.7	.7580	.7611	.7642	.7673	.7704	.7734	.7764	.77 9 4	.7823	.7852
.8	.7881	.7910	.7939	.7967	.7995	.8023	.8051	.8078	.8106	.8133
.9	.8159	.8186	.8212	.8238	.8264	.8289	.8315	.8340	.8365	.8389
1.0	.8413	.8438	.8461	.8485	.8508	.8531	.8554	.8577	.8599	.8621
1.1	.8643	.8665	.8686	.8708	.8729	.8749	.8770	.87 9 0	.8810	.8830
1.2	.8849	.8869	.8888	.8907	.8925	.8944	.8962	.8980	.8997	.9015
1.3	.9032	.9049	.9066	.9082	.9099	.9115	.9131	.9147	.9162	.9177
1.4	.9192	.9207	.9222	.9236	.9251	.9265	.9279	.9292	.9306	.9319
1.5	.9332	.9345	.9357	.9370	.9382	.9394	.9406	.9418	.9429	.9441
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	.9525	.9535	.9545
1.7	.9554	.9564	.9573	.9582	.9591	.9599	.9608	.9616	.9625	.9633
1.8	.9641	.9649	.9656	.9664	.9671	.9678	.9686	.9693	.9699	.9706
1.9	.9713	.9719	.9726 _.	.9732	.9738	.9744	.9750	.9756	.9761	.9767
2.0	.9772	.9778	.9783	.9788	.9793	.9798	.9803	.9808	.9812	.9817
2.1	.9821	.9826	.9830	.9834	.9838	.9842	.9846	.9850	.9854	.9857
2.2	.9861	.9864	.9868	.9871	.9875	.9878	.9881	.9884	.9887	.9890
2.3	.9893	.9896	.9898	.9901	.9904	.9906	.9909	.9911	.9913	.9913
2.4	.9918	.9920	.9922	.9925	.9927	.9929	.9931	.9932	.9934	.9936
2.5	.9938	.9940	.9941	.9 943	.9945	.9946	.9948	.9949	.9951	.9952
2.6	.9953	.9955	.9956	.9957	.9959	.9960	.9961	.9962	.9963	.9964
2.7	.9965	.9966	.9967	.9968	.9969	.9970	.9971	.9972	.9973	.9974
2.8	.9974	.9975	.9976	.9977	.9977	.9978	.9979	.9979	.9980	.9981
2.9	.9981	.9982	.9982	.9983	.9984	.9984	.9985	.9985	.9986	.9986
3.0	.9986	.9987	.9987	.9988	.9988	.9989	.9989	.9989	.9990	.9990

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