

- (10%) A local health center noted that in a sample of 400 patients 80 were referred to them by the local hospital:
 - Provide a 95% confidence interval for all the patients who are referred to the health center by the hospital. (5%)
 - What sample size would be required to estimate the error of 0.08 or less at 95% confidence? (5%)

- (10%) The results of a recent poll on the preference of voters regarding presidential candidates are shown below:

Candidate	Voters Surveyed	Voters Favoring This Candidate
A	400	192
B	450	225

At 95% confidence, test to determine whether or not there is a significant difference between the preferences for the two candidates.

- (15%) The number of emergency calls per day at a hospital over a period of 120 days are shown below:

Number of Emergency Calls (X)	Observed Frequency (f)
0	9
1	12
2	30
3	27
4	22
5	13
6	7
Total	120

Use $\alpha = 0.05$ and test to see if the above data have a Poisson distribution.

- (15%) An automobile dealer wants to see if there is a relationship between monthly sales and the interest rate. A random sample of 4 months was taken. The results of the sample are presented below. The estimated least square regression equation is $\hat{y} = 75.06 - 6.2516 x$

Y Monthly Sales	X Interest Rate (%)
22	9.2
20	7.6
10	10.4
45	5.3

- Obtain a measure of how well the estimated regression line fits the data. (5%)
- You want to test to see if there is a significant relationship between the interest rate and monthly sales at the 1% level of significance. State the null and alternative hypotheses. (5%)
- Construct a 99% confidence interval for the average monthly sales for all months with a 10% interest rate. (5%)

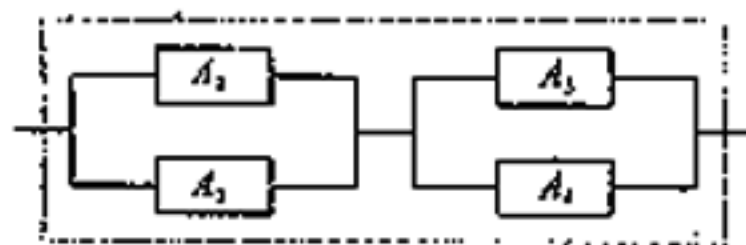
5. (15%) To enter a one-question contest, you have a choice of forming a 2-person team or a 4-person team. The enrollment fee is 500 dollars per person and the winning price is 4000 dollars. The game rule is that the team wins if at least one person in the team gets the right answer. It is assumed that everybody in the team is equally intelligent and can get the right answer with probability p independently of each other.
- Suppose you form a 2-person team to enter the contest. For what value of p can you have non-negative expected return? (5%)
 - For what value of p is a 4-person team no different from a 2-person team in terms of the expected return? (7%)
 - Would a 4-person team always be a better choice than a 2-person team? Please explain. (3%)

6. (10%) The following estimated regression equation involving three independent variables has been developed:

$$\begin{aligned} \hat{y} &= b_0 + b_1x_1 + b_2x_2 + b_3x_3 \\ &= 19.1 + 8.5x_1 + 18.0x_2 - 4.5x_3 \end{aligned}$$

where the estimates of the standard deviations of b_1 , b_2 and b_3 are $s_{b_1} = 2.4$, $s_{b_2} = 9.5$, and $s_{b_3} = 0.9$ respectively. There were 15 observations in the study. Would you recommend dropping any of the independent variables from the model? (Using $\alpha = .05$)

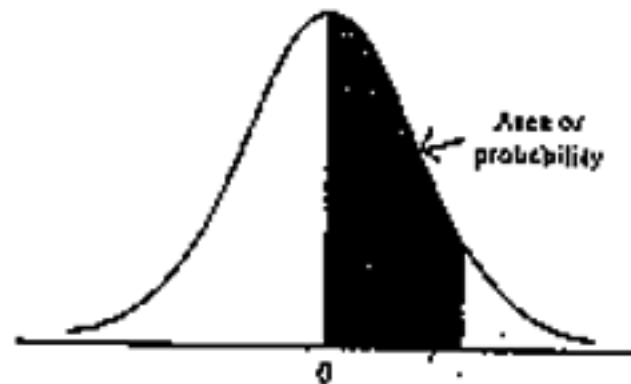
7. (15%) A system consists of four components A_1 , A_2 , A_3 and A_4 , as shown in the following diagram. The system will function if at least one of A_1 and A_2 functions and at least one of A_3 and A_4 functions. Suppose each component would fail with probability $(1 - p)$ independently of each other.



- What is the probability that the system would function? (5%)
 - Suppose now that each component A_i has a resistance R_i , $R_i = (1/f) \Omega$ if A_i is functioning; ∞ if A_i is not functioning. If two components A_i and A_j are in series, the equivalent resistance for A_i and A_j would be $(R_i + R_j)$. If A_i and A_j are in parallel, on the other hand, the equivalent resistance for A_i and A_j would be $(R_i R_j) / (R_i + R_j)$. What is the probability the system has the resistance less than 0.7Ω given that the system is functioning? (10%)
8. (10%) You are about to stack 150 coins on a smooth surface. There will be a shaking test when you stack 50, 100 and 150 coins respectively. Assume the coins would collapse only in these three shaking tests (not in your stacking process). It takes you 10 minutes to stack 50 coins that would collapse with probability p_1 in the first shaking test. It takes you 20 minutes more, if passing the first test, to stack another 50 coins and the total 100 coins would collapse with probability p_2 in the second shaking test. Finally, it takes you 30 minutes more, if passing the second test, to stack another 50 coins and the total 150 coins would collapse with probability p_3 in the final test. If the coins collapse in one of the shaking tests, you repeat the stacking process from the beginning. Assuming these shaking tests take no time, what would be the expected length of time until you can successfully stack 150 coins?

附表 1

TABLE
Standard Normal
Distribution

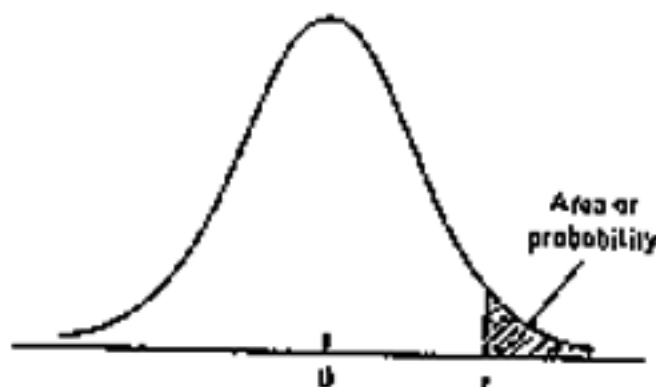


Entries in the table give the area under the curve between the mean and z standard deviations above the mean. For example, for $z = 1.25$ the area under the curve between the mean and z is .3944.

z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.0359
.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.0753
.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.1141
.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.1517
.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.1879
.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224
.6	.2257	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2518	.2549
.7	.2580	.2612	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852
.8	.2881	.2910	.2939	.2967	.2995	.3023	.3051	.3078	.3106	.3133
.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3341	.3365	.3389
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621
1.1	.3643	.3665	.3686	.3706	.3729	.3749	.3770	.3790	.3810	.3829
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3981	.3997	.4015
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
1.5	.4333	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.4706
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4985	.4986
3.0	.4986	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.4990

附表 2

TABLE
t Distribution

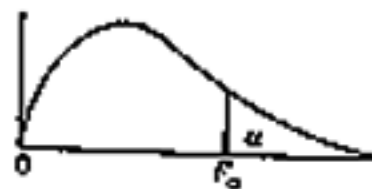


Entries in the table give t values for an area or probability in the upper tail of the t distribution. For example, with 10 degrees of freedom and a .05 area in the upper tail, $t_{10}.05 = 1.812$.

Degrees of Freedom	Area in Upper Tail				
	.10	.05	.025	.01	.005
1	3.078	6.314	12.706	31.821	63.657
2	2.878	2.920	4.303	6.965	9.925
3	2.638	2.353	3.182	4.541	5.821
4	2.533	2.122	2.776	3.747	4.604
5	2.476	2.013	2.571	3.563	4.033
6	2.440	1.943	2.447	3.143	3.707
7	2.415	1.895	2.365	2.908	3.499
8	2.397	1.860	2.306	2.896	3.355
9	2.383	1.833	2.262	2.821	3.250
10	2.372	1.812	2.228	2.764	3.169
11	2.363	1.796	2.201	2.718	3.118
12	2.356	1.782	2.179	2.681	3.075
13	2.350	1.771	2.161	2.650	3.032
14	2.345	1.761	2.145	2.624	2.997
15	2.341	1.753	2.131	2.602	2.967
16	2.337	1.746	2.120	2.583	2.941
17	2.333	1.740	2.110	2.567	2.918
18	2.330	1.734	2.101	2.552	2.898
19	2.328	1.729	2.093	2.539	2.881
20	2.325	1.725	2.086	2.528	2.865
21	2.323	1.721	2.080	2.518	2.851
22	2.321	1.717	2.074	2.508	2.839
23	2.319	1.714	2.069	2.500	2.827
24	2.318	1.711	2.064	2.492	2.817
25	2.316	1.708	2.060	2.485	2.807
26	2.315	1.706	2.056	2.479	2.799
27	2.314	1.703	2.052	2.473	2.791
28	2.313	1.701	2.048	2.467	2.783
29	2.311	1.699	2.045	2.462	2.776
30	2.310	1.697	2.042	2.457	2.770
40	2.303	1.684	2.028	2.423	2.704
60	2.296	1.671	2.000	2.390	2.660
120	2.289	1.658	1.980	2.358	2.617
∞	2.282	1.645	1.960	2.326	2.576

附表 3

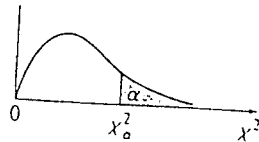
Table : Percentage points of the F distributions



Denominator d.f.	Numerator d.f.									
	1	2	3	4	5	6	7	8	9	
1	.100	39.86	49.50	53.59	55.83	57.24	58.30	59.01	59.44	59.86
	.050	161.4	199.5	215.7	224.6	230.2	234.0	236.8	238.7	240.5
	.025	647.8	799.5	864.2	899.6	921.8	937.1	948.2	956.7	963.1
	.010	4052	4999.5	5403	5625	5764	5859	5928	5982	6022
	.005	16211	20000	21615	22500	23056	23437	23785	24025	24291
2	.100	8.53	9.00	9.16	9.24	9.29	9.33	9.35	9.37	9.38
	.050	18.51	19.00	19.16	19.25	19.30	19.33	19.35	19.37	19.38
	.025	38.51	39.00	39.17	39.25	39.30	39.33	39.36	39.37	39.38
	.010	98.50	99.00	99.17	99.25	99.30	99.33	99.36	99.37	99.38
	.005	198.5	199.0	199.2	199.2	199.3	199.3	199.4	199.4	199.4
3	.100	5.54	5.46	5.39	5.34	5.31	5.28	5.27	5.25	5.24
	.050	10.13	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.81
	.025	17.44	16.04	15.44	15.10	14.88	14.73	14.62	14.54	14.47
	.010	34.12	30.82	29.46	28.71	28.24	27.91	27.67	27.49	27.35
	.005	55.55	49.80	47.47	46.19	45.39	44.84	44.43	44.13	43.88
4	.100	4.54	4.32	4.19	4.11	4.05	4.01	3.98	3.95	3.94
	.050	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00
	.025	12.22	10.65	9.98	9.60	9.36	9.20	9.07	8.98	8.90
	.010	21.20	18.00	16.69	15.98	15.52	15.21	14.98	14.80	14.66
	.005	31.33	26.28	24.26	23.15	22.46	21.97	21.62	21.35	21.14
5	.100	4.06	3.78	3.62	3.52	3.45	3.40	3.37	3.34	3.32
	.050	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.77
	.025	10.01	8.43	7.76	7.39	7.15	6.98	6.85	6.76	6.68
	.010	16.36	13.27	12.06	11.39	10.97	10.67	10.46	10.29	10.16
	.005	22.78	18.31	16.53	15.56	14.94	14.51	14.20	13.96	13.77
6	.100	3.78	3.46	3.29	3.18	3.11	3.05	3.01	2.99	2.96
	.050	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10
	.025	8.81	7.26	6.60	6.23	5.99	5.82	5.70	5.60	5.52
	.010	13.73	10.92	9.78	9.15	8.75	8.47	8.26	8.10	7.98
	.005	18.63	14.54	12.92	12.03	11.46	11.07	10.79	10.57	10.39
7	.100	3.59	3.26	3.07	2.95	2.88	2.83	2.78	2.75	2.71
	.050	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68
	.025	8.07	6.54	5.89	5.52	5.29	5.12	4.99	4.90	4.82
	.010	12.35	9.55	8.45	7.85	7.46	7.19	6.99	6.84	6.72
	.005	16.24	12.40	10.88	10.05	9.57	9.16	8.89	8.68	8.51

(背面仍有題目,請繼續作答)

附表 4
卡方分配表



自由度	單尾顯著水準							
	0.99	0.975	0.95	0.9	0.1	0.05	0.025	0.01
1	0.0002	0.0010	0.0039	0.0158	2.7055	3.8415	5.0239	6.6349
2	0.0201	0.0506	0.1026	0.2107	4.6052	5.9915	7.3778	9.2103
3	0.1148	0.2158	0.3518	0.5844	6.2514	7.8147	9.3484	11.3440
4	0.2971	0.4844	0.7107	1.0636	7.7794	9.4877	11.1433	13.2767
5	0.5543	0.8312	1.1455	1.6103	9.2364	11.0705	12.8325	15.0863
6	0.8721	1.2373	1.6354	2.2041	10.6446	12.5916	14.4494	16.8119
7	1.2390	1.6899	2.1673	2.8331	12.0170	14.0671	16.0128	18.4753
8	1.6465	2.1797	2.7326	3.4895	13.3616	15.5073	17.5345	20.0902
9	2.0879	2.7004	3.3251	4.1682	14.6837	16.9190	19.0228	21.6660
10	2.5582	3.2470	3.9403	4.8652	15.9872	18.3070	20.4832	23.2093
11	3.0535	3.8157	4.5748	5.5778	17.2750	19.6751	21.9200	24.7250
12	3.5706	4.4038	5.2260	6.3038	18.5493	21.0261	23.3367	26.2170
13	4.1069	5.0088	5.8919	7.0415	19.8119	22.3620	24.7356	27.6882
14	4.6604	5.6287	6.5706	7.7895	21.0641	23.6848	26.1189	29.1412
15	5.2293	6.2621	7.2609	8.5468	22.3071	24.9958	27.4884	30.5779
16	5.8122	6.9077	7.9616	9.3122	23.5418	26.2962	28.8454	31.9999
17	6.4078	7.5642	8.6718	10.0852	24.7690	27.5871	30.1910	33.4087
18	7.0149	8.2307	9.3905	10.8649	25.9894	28.8693	31.5264	34.8053
19	7.6327	8.9065	10.1170	11.6509	27.2036	30.1435	32.8523	36.1909
20	8.2604	9.5908	10.8508	12.4426	28.4120	31.4104	34.1696	37.5662
21	8.8972	10.2829	11.5913	13.2396	29.6151	32.6706	35.4789	38.9322
22	9.5425	10.9823	12.3380	14.0415	30.8133	33.9244	36.7807	40.2894
23	10.1957	11.6886	13.0905	14.8480	32.0069	35.1725	38.0756	41.6384
24	10.8564	12.4012	13.8484	15.6587	33.1962	36.4150	39.3641	42.9798
25	11.5240	13.1197	14.6114	16.4734	34.3816	37.6525	40.6465	44.3141
26	12.1981	13.8439	15.3792	17.2919	35.5632	38.8851	41.9232	45.6417
27	12.8785	14.5734	16.1514	18.1139	36.7412	40.1133	43.1945	46.9629
28	13.5647	15.3079	16.9279	18.9392	37.9159	41.3371	44.4608	48.2782
29	14.2565	16.0471	17.7084	19.7677	39.0875	42.5570	45.7223	49.5879
30	14.9535	16.7908	18.4927	20.5992	40.2560	43.7730	46.9792	50.8922
35	18.5089	20.5694	22.4650	24.7967	46.0588	49.8018	53.2033	57.3421
40	22.1643	24.4330	26.5093	29.0505	51.8051	55.7585	59.3417	63.6907
45	25.9013	28.3662	30.6123	33.3504	57.5053	61.6562	65.4102	69.9568
50	29.7067	32.3574	34.7643	37.6886	63.1671	67.5048	71.4202	76.1539
60	37.4849	40.4817	43.1880	46.4589	74.3970	79.0819	83.2977	88.3794
70	45.4417	48.7576	51.7393	55.3289	85.5270	90.5312	95.0232	100.4252
80	53.5401	57.1532	60.3915	64.2778	96.5782	101.8795	106.6286	112.3288
90	61.7541	65.6466	69.1260	73.2911	107.5650	113.1453	118.1359	124.1163
100	70.0649	74.2219	77.9295	82.3581	118.4980	124.3421	129.5612	135.8067
200	156.4320	162.7280	168.2786	174.8353	226.0210	233.9943	241.0579	249.4451
300	245.9725	253.9123	260.8781	269.0679	331.7885	341.3951	349.8745	359.9064
400	337.1553	346.4818	354.6410	364.2074	436.6490	447.6325	457.3055	468.7245
500	429.3875	439.9360	449.1468	459.9261	540.9303	553.1268	563.8515	576.4928