

選擇題：(每題五分，共六十分。)

- The perpendicular distance from (1,2) to the line  $y = (2x/3) + 1$  is  
A) 26    B) 13    C)  $\sqrt{13}$     D)  $\frac{\sqrt{13}}{13}$     E)  $\frac{2}{\sqrt{3}}$
- If one root of the equation  $x^2 + bx - 8 = 0$  is the square root of the other then  $b = ?$   
A) -2    B) -9    C) -6    D) 0    E) 26
- What is the value of  $\lim_{h \rightarrow 0} \frac{\sqrt{2+h} + \sqrt{2}}{h}$ ?  
A) Undefined    B) 0    C)  $\frac{\sqrt{2}}{2}$     D)  $\frac{\sqrt{2}}{4}$     E)  $+\infty$
- Given  $f(x) = \frac{x^2 - 2x - 1}{x - 1 - \sqrt{2}}$  if  $x \neq 1 + \sqrt{2}$  and  $f(x)$  is continuous at  $x = 1 + \sqrt{2}$ .  
Find  $f(1 + \sqrt{2})$ .  
A)  $\frac{1}{2}$     B) 2    C)  $2\sqrt{2}$     D)  $\sqrt{2}$     E) 0
- If  $f(x) = 5|2x - 1| - 2|3x^2 - 4|$  the  $f'(-1) = ?$ .  
A) 2    B) 0    C) 22    D) -22    E) -2
- If  $f(x) = x^2$ ,  $h(x) = f(1 + g(x))$ ,  $g'(1) = 1$  and  $h'(1) = 1$ , then  $g(1) = ?$   
A) -1    B)  $-\frac{1}{2}$     C) 0    D)  $\frac{1}{2}$     E) 1
- Suppose  $h(x) = \frac{x^4}{x - \sin x}$  for  $x \neq 0$ . In order that  $h(x)$  be continuous at 0,  $h(0) = ?$   
A) -1    B) 0    C) 1    D) 3    E) 6
- What is the difference between the maximum and minimum values of the function  $f(x) = x + \sin x$  on the closed interval  $[\frac{\pi}{6}, \pi]$ ?  
A)  $\frac{\pi}{2} + \sqrt{3} - 1$     B)  $\frac{5\pi}{6} - 1$     C)  $\sqrt{3} - \frac{\pi}{3}$     D)  $\frac{2\pi}{3}$     E)  $\frac{\pi}{2}$
- Suppose  $f$  is a non-negative increasing function on  $[0, 4]$ ,  $\int_0^4 f(x) dx = 5$ , and  $\{x | f(x) \geq 6\} = [3.5, 4]$ . Which of the following are impossible?  
I.  $\int_0^{3.5} f(x) dx = 1$     II.  $\int_0^{3.5} f(x) dx = 3$     III.  $f(2) = 2$   
A) II only    B) I and II only    C) I and III only    D) II and III only    E) I, II and III

(背面仍有題目,請繼續作答)

10. If  $F(x) = \int_0^x xf(t)dt$ , then what is  $x F'(x)$ ?

- A)  $x^2 f(x) + F(x)$       B)  $f(x) + F(x)$       C)  $x f(x) + F(x)$   
D)  $x F(x) + f(x)$       E)  $x f(x) + x F(x)$

11. What is the interval of convergence of the series  $\sum_{n=0}^{\infty} \frac{(-1)^n x^n}{4^n}$  ?

- A)  $0 \leq x < 1$     B)  $-1 < x < 1$     C)  $-4 \leq x \leq 4$     D)  $-4 < x \leq 4$     E)  $-4 < x < 4$

12. Which of the following is equal to the sum  $S = 1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \dots + \left(\frac{1}{2}\right)^{10}$ ?

- A)  $\frac{2^{10}-1}{2^{10}}$     B)  $\frac{2^{11}+1}{2^{10}}$     C)  $\frac{2^{10}+1}{2^{10}}$     D)  $\frac{2^{11}-1}{2^{10}}$     E)  $\frac{2^{11}+1}{2^{10}}$

計算題：(每題十分，共四十分。)

1. What is the area of the closed region bounded by  $x = -1$ ,  $x = 0$ ,  $y = x^2$  and  $y = x^3$ ?
2. Let the functions  $f$ ,  $g$ , and  $h$  be defined as follows:

$$f(x) = \begin{cases} x \sin \frac{1}{x}, & \text{for } -1 \leq x \leq 1 \text{ and } x \neq 0 \\ 0, & \text{for } x = 0 \end{cases} \quad g(x) = \begin{cases} x^2 \sin \frac{1}{x}, & \text{for } -1 \leq x \leq 1 \text{ and } x \neq 0 \\ 0, & \text{for } x = 0 \end{cases}$$

and  $h(x) = |x|^3$  for  $-1 \leq x \leq 1$ .

Which of these functions are differentiable at 0?

3.  $f(x, y) = 3y^2 \ln(x^3 + 4) + \frac{2y}{x}$  for  $x > 0$  and  $-\infty < y < \infty$ . What value of  $y$  minimizes  $\frac{\partial f}{\partial x}$  when  $x = 2$ ?
4. What are all the values of  $x$  for which the infinite series  $(x-5) + 2(x-5)^2 + 3(x-5)^3 + 4(x-5)^4 + \dots$  converges?