

注意：必須把答題過程寫出來，請用微積分課上所學作答

1. Find  $\lim_{x \rightarrow -\infty} (3x + 9) / (2x^2 + 1)^{\frac{1}{2}}$  . 10%

2. Find a number  $a$  with the property that the line tangent to the graph of  $f(x) = x^2$  at  $(a, f(a))$  passes through  $(-1, 0)$ . 10%

3. An airplane, flying west at 400 miles per hour, goes over a certain town at 11:30 A.M., and a second plane at the same altitude, flying south at 500 miles per hour, goes over the town at noon. How fast are they separating at 1:00 P.M.? 10%

4.  $\lim_{x \rightarrow 0} (4x^2 \cos 3x) / (\sin^2 3x)$ . 10%

5.  $D_x \int_{x^2}^{x^{\frac{1}{2}}} t \cos t^3 dt$  . 10%

6.  $\int (x^2 + 1) (x - 2)^{\frac{1}{2}} dx$  . 10%

7.  $\int_0^9 \frac{1}{(x - 2)^{\frac{2}{3}}} dx$  . 10%

8. Find the volume of the solid generated by revolving the region bounded by  $y = 2x^{\frac{1}{2}}$ ,  $x = 4$ , and  $y = 0$  about  $x = 4$ . 10%

9.  $\int \frac{x^4 + 3x^3 - 4x + 1}{x^3 + 4x^2 + 4x} dx$  . 10%

10. Evaluate the iterated integral 10%

$$\int_0^1 \int_x^1 e^{y^2} dy dx.$$