

A-1. Please explain the following terminologies in detail: (12)

- a. Type I error and Type II error
- b. Standard Deviation and Standard Error
- c. Skewness and Kurtosis
- d. Hypothesis Test
- e. Coefficient of Variation
- f. Confidence Interval

A-2. Assume that the test scores from a college admissions test are normally distributed, with a mean of 450 and a standard deviation of 100. (7)

- a. What percentage of the people taking the test score between 400 and 500?
- b. Suppose someone receives a score of 630. What percentage of the people taking the test score better? What percentage score worse?
- c. If a particular university will not admit anyone scoring below 480, what percentage of the persons taking the test would be acceptable to the university?

A-3. An oil company has purchased an option on land in Alaska. Preliminary geological studies have assigned the following prior probabilities: $P(\text{high-quality oil})=0.50$, $P(\text{medium-quality oil})=0.20$, and $P(\text{no oil})=0.30$. (7)

- a. What is the probability of finding oil?
- b. After 200 feet of drilling on the first well, a soil test is taken. The probabilities of finding the particular type of soil identified by the test follow:
 $P(\text{soil} \mid \text{high-quality oil})=0.20$, $P(\text{soil} \mid \text{medium-quality oil})=0.80$, and
 $P(\text{Soil} \mid \text{no oil})=0.20$. How should the firm interpret the soil test? What are the revised probabilities, and what is the new probability of finding oil?

A-4. Assume that a study is being designed to collect new data on smokers and nonsmokers. The best preliminary estimate of the population proportion who smoke is 30%. (8)

- a. How large a sample should be taken to estimate the proportion of smokers in the population with a margin of error of 0.02? Use 95% confidence.
- b. Assume that the study uses your sample size recommendation in part (a) and finds 520 smokers. What is the 95% confidence interval for the proportion of smokers in the population?

- A-5. The monthly rent for a two-bedroom apartment in a particular city is reported to average \$550. A sample of 36 two-bedroom apartments is selected. The sample mean turns out to be \$562, with a sample standard deviation of \$40. (8)
- Conduct a hypothesis test with $\alpha=0.05$ to test if the average rent equals to \$550 or not.
 - Compute the p-value.
 - Use the sample results to construct a 95% confidence interval for the population mean. What hypothesis testing conclusion would you draw from the confidence interval result?
- A-6. A group of physicians conducted a year-long study on the effectiveness of nicotine chewing gum in helping people to stop smoking. The 113 people who participated in the study were all smokers. Sixty were given chewing gum with 2 milligrams of nicotine and 53 were given a placebo chewing gum with no nicotine content. No one in the study knew which type of gum he or she had been given. All were told to use the gum and refrain from smoking. (8)
- State the null and alternative hypotheses that would be appropriate if the researchers hoped to show that the group given nicotine chewing gum had a higher proportion of nonsmokers one year after the study began.
 - Results showed that 23 of the smokers given nicotine chewing gum had remained non-smokers for the one-year period and 12 of the smokers given the placebo had remained non-smokers during the same period. Do these results support the conclusion that nicotine gum can help a person to stop smoking? Test using $\alpha=0.05$. What is the p-value?

- B-1. A researcher wants to find the relationship between Corn Yield and Fertilizer. He collects the following data after the field study. Please answer the following questions.

Fertilizer	0.3	0.6	0.9	1.2	1.5	1.8	2.1	2.4
Corn Yield	10	15	30	35	25	30	50	45

- a. (2%) Please define your dependent and independent variable of this research.
- b. (2%) Please write down your theoretical regression model
- c. (6%) Please estimate your regression model via Least Square Method.
- d. (3%) Please estimate the Corn Yield when Fertilizer is 1.6, 2.2, and 3.0.
- e. (2%) Please draw a diagram that shows your data, regression line.
- f. (3%) What is coefficient of determination?
- g. (3%) What is coefficient of correlation?
- h. (3%) What is the relationship between coefficient of determination and coefficient of correlation in this problem?
- i. (4%) Please find the confidence interval of β_0 and β_1 . Please use $\alpha = 0.05$.

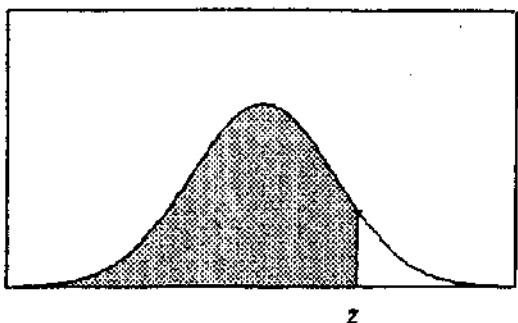
- B-2. The partially completed ANOVA for a 3X4 factorial experiment with two replications is shown here.

Source	df	SS	MS	F
A		0.8		
B		5.3		
AB		9.6		
Error				
Total		17.0		

- a. (13%) Please complete the ANOVA table
- b. (3%) Which sums of squares are combined to find the Sum of Squares for Treatment? (3%) Do these data provide sufficient evidence to indicate that the treatment means differ? Use $\alpha = 0.05$.
- c. (3%) What is meant by factor interaction, and what is the practical implication if it exists?

表 1. 常態分配表

$$\Phi(z) = P(Z \leq z) = \int_{-\infty}^z \frac{1}{\sqrt{2\pi}} e^{-t^2/2} dt$$



z 的小數點第二位

表3. t分配表

$$P(t_k \geq t_{k,\alpha}) = \alpha$$

 $t_{k,\alpha}$

自由度	單尾顯著水準						
	0.1	0.05	0.025	0.01	0.005	0.0025	0.001
1	3.0777	6.3138	12.7062	31.8205	63.6567	127.3213	318.3088
2	1.8856	2.9200	4.3027	6.9646	9.9248	14.0890	22.3271
3	1.6377	2.3534	3.1824	4.5407	5.8409	7.4533	10.2145
4	1.5332	2.1318	2.7764	3.7469	4.6041	5.5976	7.1732
5	1.4759	2.0150	2.5706	3.3649	4.0321	4.7733	5.8934
6	1.4398	1.9432	2.4469	3.1427	3.7074	4.3168	5.2076
7	1.4149	1.8946	2.3646	2.9980	3.4995	4.0293	4.7853
8	1.3968	1.8595	2.3060	2.8965	3.3554	3.8325	4.5008
9	1.3830	1.8331	2.2622	2.8214	3.2498	3.6897	4.2968
10	1.3722	1.8125	2.2281	2.7638	3.1693	3.5814	4.1437
11	1.3634	1.7959	2.2010	2.7181	3.1058	3.4966	4.0247
12	1.3562	1.7823	2.1788	2.6810	3.0545	3.4284	3.9296
13	1.3502	1.7709	2.1604	2.6503	3.0123	3.3725	3.8520
14	1.3450	1.7613	2.1448	2.6245	2.9768	3.3257	3.7874
15	1.3406	1.7531	2.1314	2.6025	2.9467	3.2860	3.7328
16	1.3368	1.7459	2.1199	2.5835	2.9208	3.2520	3.6862
17	1.3334	1.7396	2.1098	2.5669	2.8982	3.2224	3.6458
18	1.3304	1.7341	2.1009	2.5524	2.8784	3.1966	3.6105
19	1.3277	1.7291	2.0930	2.5395	2.8609	3.1737	3.5794
20	1.3253	1.7247	2.0860	2.5280	2.8453	3.1534	3.5518
21	1.3232	1.7207	2.0796	2.5176	2.8314	3.1352	3.5272
22	1.3212	1.7171	2.0739	2.5083	2.8188	3.1188	3.5050
23	1.3195	1.7139	2.0687	2.4999	2.8073	3.1040	3.4850
24	1.3178	1.7109	2.0639	2.4922	2.7969	3.0905	3.4668
25	1.3163	1.7081	2.0595	2.4851	2.7874	3.0782	3.4502
26	1.3150	1.7056	2.0555	2.4786	2.7787	3.0669	3.4350
27	1.3137	1.7033	2.0518	2.4727	2.7707	3.0565	3.4210
28	1.3125	1.7011	2.0484	2.4671	2.7633	3.0469	3.4082
29	1.3114	1.6991	2.0452	2.4620	2.7564	3.0380	3.3962
30	1.3104	1.6973	2.0423	2.4573	2.7500	3.0298	3.3852
35	1.3062	1.6896	2.0301	2.4377	2.7238	2.9960	3.3400
40	1.3031	1.6839	2.0211	2.4233	2.7045	2.9712	3.3069
45	1.3006	1.6794	2.0141	2.4121	2.6896	2.9521	3.2815
50	1.2987	1.6759	2.0086	2.4033	2.6778	2.9370	3.2614
60	1.2958	1.6706	2.0003	2.3901	2.6603	2.9146	3.2317
70	1.2938	1.6669	1.9944	2.3808	2.6479	2.8987	3.2108
80	1.2922	1.6641	1.9901	2.3739	2.6387	2.8870	3.1953
90	1.2910	1.6620	1.9867	2.3685	2.6316	2.8779	3.1833
100	1.2901	1.6602	1.9840	2.3642	2.6259	2.8707	3.1737
200	1.2858	1.6525	1.9719	2.3451	2.6006	2.8385	3.1315
300	1.2844	1.6499	1.9679	2.3388	2.5923	2.8279	3.1176
400	1.2837	1.6487	1.9659	2.3357	2.5882	2.8227	3.1107
500	1.2832	1.6479	1.9647	2.3338	2.5857	2.8195	3.1066
600	1.2830	1.6474	1.9639	2.3326	2.5840	2.8175	3.1039
700	1.2828	1.6470	1.9634	2.3317	2.5829	2.8160	3.1019
800	1.2826	1.6468	1.9629	2.3310	2.5820	2.8148	3.1005
900	1.2825	1.6465	1.9626	2.3305	2.5813	2.8140	3.0993
1000	1.2824	1.6464	1.9623	2.3301	2.5808	2.8133	3.0984

(背面仍有題目,請繼續作答)

Percentage Points of the F Distribution

D.F. of Numerator (n)	Degrees of Freedom for the Numerator (n)										D.F. of Denominator (m)					
	1	2	3	4	5	6	7	8	9	10						
1	161.4	199.5	215.7	224.6	230.2	236.4	240.5	243.9	245.9	248.0	249.1	250.1	251.1	252.2	253.3	254.3
2	18.51	19.00	19.16	19.25	19.30	19.35	19.37	19.38	19.40	19.41	19.43	19.45	19.46	19.47	19.48	19.49
3	10.13	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.81	8.79	8.74	8.66	8.62	8.59	8.57	8.53
4	7.71	6.94	6.39	6.16	5.94	5.69	5.44	5.20	5.04	5.00	5.96	5.91	5.86	5.80	5.75	5.72
5	6.61	5.79	5.41	5.19	5.03	4.95	4.84	4.72	4.77	4.74	4.68	4.62	4.56	4.53	4.50	4.46
6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10	4.06	3.94	3.87	3.84	3.81	3.77	3.74
7	5.59	4.74	4.35	4.12	3.87	3.59	3.33	3.07	2.88	2.68	2.64	3.57	3.51	3.44	3.38	3.34
8	5.32	4.46	4.07	3.84	3.69	3.58	3.44	3.39	3.35	3.24	3.22	3.15	3.12	3.08	3.04	3.01
9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18	3.14	3.14	3.07	3.01	2.94	2.86	2.83
10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.03	2.98	2.91	2.85	2.77	2.74	2.70	2.66
11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90	2.85	2.79	2.72	2.65	2.61	2.57	2.53
12	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.80	2.75	2.69	2.62	2.54	2.49	2.43	2.38
13	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.71	2.67	2.60	2.53	2.46	2.42	2.38	2.34
14	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.65	2.60	2.53	2.46	2.39	2.35	2.31	2.27
15	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.59	2.54	2.48	2.40	2.33	2.29	2.25	2.20
16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54	2.49	2.42	2.35	2.28	2.24	2.19	2.15
17	4.43	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.49	2.45	2.38	2.31	2.23	2.19	2.15	2.10
18	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.45	2.41	2.34	2.27	2.19	2.15	2.10	2.06
19	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.42	2.38	2.31	2.23	2.16	2.11	2.07	2.03
20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.39	2.35	2.28	2.20	2.12	2.08	2.04	1.99
21	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.37	2.32	2.25	2.18	2.10	2.05	2.01	1.96
22	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.34	2.30	2.23	2.15	2.07	2.03	1.98	1.92
23	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.32	2.27	2.20	2.13	2.05	2.01	1.96	1.91
24	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.30	2.25	2.18	2.11	2.03	1.98	1.94	1.89
25	4.24	3.39	2.99	2.76	2.60	2.49	2.40	2.34	2.28	2.24	2.18	2.10	2.03	1.94	1.90	1.85
26	4.23	3.37	2.98	2.74	2.59	2.47	2.39	2.32	2.27	2.21	2.16	2.09	2.01	1.93	1.87	1.82
27	4.21	3.35	2.96	2.73	2.57	2.46	2.37	2.31	2.25	2.20	2.13	2.06	1.97	1.93	1.88	1.84
28	4.20	3.34	2.95	2.71	2.56	2.45	2.36	2.29	2.24	2.19	2.12	2.04	1.96	1.91	1.87	1.82
29	4.18	3.33	2.93	2.70	2.55	2.43	2.35	2.28	2.22	2.18	2.10	2.03	1.94	1.90	1.85	1.81
30	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.21	2.16	2.09	2.01	1.93	1.89	1.84	1.79
40	4.08	3.23	2.64	2.61	2.43	2.34	2.25	2.18	2.12	2.08	2.00	1.92	1.84	1.79	1.74	1.62
50	4.00	3.15	2.55	2.53	2.37	2.25	2.17	2.10	2.04	1.99	1.92	1.84	1.75	1.69	1.64	1.51
120	3.92	3.07	2.68	2.45	2.29	2.17	2.09	2.02	1.96	1.91	1.83	1.75	1.66	1.59	1.53	1.47
∞	3.84	3.00	2.60	2.37	2.21	2.10	2.01	1.94	1.84	1.83	1.73	1.67	1.57	1.46	1.39	1.22