

# 國立成功大學

## 114學年度碩士班招生考試試題

編 號： 79

系 所： 土木工程學系

科 目： 材料力學

日 期： 0210

節 次： 第 1 節

注 意： 1. 可使用計算機  
2. 請於答案卷(卡)作答，於  
試題上作答，不予計分。

1. (25%) A compressive load  $P$  is transmitted through a rigid plate to three bars that have identical cross-section area  $A$  (see Fig. 1). The middle bar has Young's modulus  $E=50\text{GPa}$ , but the other bars have Young's modulus  $E=100\text{GPa}$ . Initially, the middle bar is slightly shorter than the other bars (see Figure). The dimensions are:  $L=1\text{m}$ ,  $s=1.0\text{mm}$ ,  $A=3000\text{mm}^2$ .

- (a) Calculate the total strain energy  $U$  of the three bars when  $P=400\text{kN}$ .  
 (b) Calculate the total strain energy  $U$  of the three bars when  $P=750\text{kN}$ .

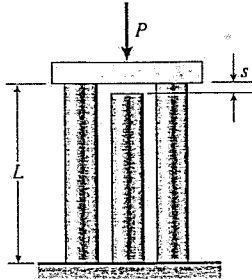


Fig.1

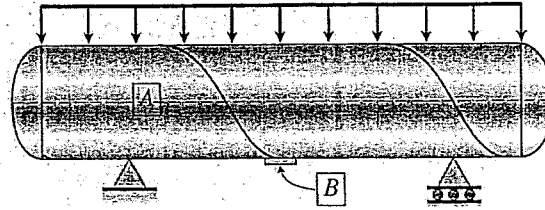


Fig. 2

2. (25%) The cylindrical pressure vessel is placed symmetrically on simple supports and is acted on by a uniform distributed load  $q=150\text{kN/m}$  (see Fig.2). The 6m long tank has an inner radius of  $r=1.2\text{ m}$  and a wall thickness of  $t=19\text{mm}$ . The span between two supports is 3.6m. The material is steel with a modulus of  $E=200\text{GPa}$  and the internal pressure  $p=720\text{kPa}$ . The effects of distributed load  $q$  and internal pressure  $p$  are considered. Element A is on the outer surface of the vessel, just to the right of the left-hand support. Element B is located on the bottom surface of the tank at the mid-span.

- (a) Draw state of stress at element A, and find principal stresses and principal directions.  
 (b) Draw state of stress at element B, and find maximum shear stress.

3. (25%) A steel beam ABC is simply supported at A and held by a high-strength steel wire at B (see Fig.3 ). A load  $P=1\text{ kN}$  acts at the free end C. The wire has axial rigidity  $EA= 1400\text{ N}$ , and the beam has flexural rigidity  $EI=90\text{ kNm}^2$ . What is the deflection C of point C due to the load  $P$ ?

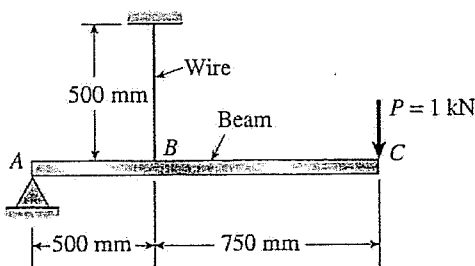


Fig. 3

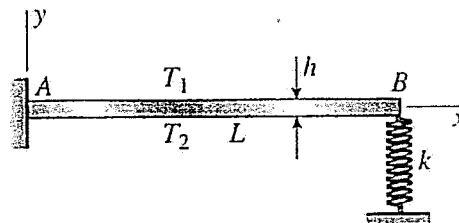


Fig.4

4. (25%) A cantilever beam with flexural rigidity  $EI$ , fixed at the left-hand end A and simply supported at the right-hand end B, is subjected to a temperature differential with temperature  $T_1$  on its upper surface and  $T_2$  on its lower surface (see Fig.4). Assume the coefficient of thermal expansion for the beam material is  $\alpha$ , and the spring support is unaffected by temperature changes.

- (a) Find all reactions for this beam.  
 (b) Determine the deflection curve.