

※ 考生請注意：本試題不可使用計算機。請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

1. (10%) Determine the Big-O as a function of  $n$  by estimating the number of times that the statement X is executed.

```
Void Function (int n)
{
    int r;
    r = 1;
    while (r < n) {
        X; r = 2*r; }
}
```

2. (10%)

Complete the parts indicated by XXX-1 and XXX-2 for stack operations

```
void add(int *top, element item)
{
    /* add an item to the global stack */
    if (*top >= MAX_STACK_SIZE-1) {
        stack_full( );
        return;
    }
    stack[XXX-1] = item;
}
```

```
element delete(int *top)
{
    /* return the top element from the stack */
    if (*top == -1)
        return stack_empty(); /* returns and error key */
    return stack[(XXX-2)];
}
```

3. (10%) Please translate the following expressions.

Infix to Postfix conversion:  $(a+b)/(c-d)*e+f/g$

Postfix to Infix conversion:  $abc*+de*-f+$

4. (10%) The Prim's algorithm is to find a MCST. Please answer (a) What is MCST? (b) Why is it called greedy algorithm?
5. (15%) On average, the time complexity of *Quicksort* is  $O(n \log n)$ , but its worst case is  $O(n^2)$  which is greater than that of *Mergesort*. (a) Why we can call it "quick"? (b) Explain when the worst case happens.
6. (15%) Construct a *MAX Heap* by the order of the following input: 9 · 14 · 15 · 4 · 7 · 18 · 3 · 6 · 20. You need to specify the method used, *top-down* or *bottom up*, before starting the construction.
7. (15%) *Mergesort* can be expressed by the recursive function  $T(n) = 2 * T(n/2) + O(n)$ , while *Quicksort* can be expressed by  $T(n) = T(k) + T(n-k) + O(n)$ , where  $1 \leq k \leq n-1$ . (a) Explain the reason, (b) Derive the time complexity from the function for *Mergesort*.
8. (15%)
  - (a) Write down the input and output for *Hash Function*.
  - (b) To access a record (or data), we can use sequential search or direct access. Hashing is a compromise method between two approaches, why? (c) Linear probing and chaining are often used to handle the collision, Compare them.