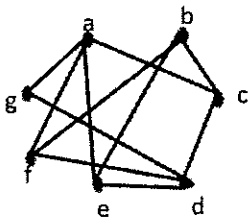
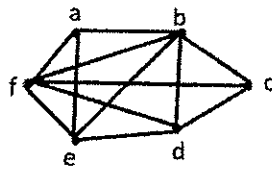


※ 考生請注意：本試題不可使用計算機。請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

- Suppose E is the event that a randomly generated bit string of length four begins with a 1 and F is the event that a randomly generated bit string contains an odd number of 0s. Are E and F independent, if the 16 bit strings of length four are equally likely? (10%)
- What algebraic expression in a Boolean algebra corresponds to the statement $p \rightarrow q$ in the propositional calculus? (5%)
- Draw a digraph for the divides relation, $x|y$, where the universe is \mathbb{N}_6 , which consisting of the integers from 1 through 6. (10%)
- How many strings of length 10 on the alphabet $\{A, B, C\}$ have the letter C appearing at least once in any two successive letters? (15%)
- Are the graphs A and B displayed in the following Figures bipartite? (10%)



Graph A



Graph B

- Determine whether the sequence $\{a_n\}$ is a solution of the recurrence relation $a_n = 2a_{n-1} - a_{n-2}$ for $n = 2, 3, 4, \dots$, where $a_n = 3n$ for every nonnegative integer n . Answer the same question where $a_n = 2^n$ and where $a_n = 5$. (15%)
- A rooted tree is a tree with one of its vertices singled out. This vertex is called the root of the rooted tree. The weight of a vertex v in a rooted tree is defined to be $1-n$, where n is the number of children of v . In the following list, it is shown the associated weights for the corresponding vertex. Reconstruct the tree. (10%)

vertices	a	b	a	b	c	c	d	e
weights	-1	-2	1	1	1	-1	1	1

8. For any integers a , b , and n , the expression $a \equiv b \pmod n$, denoted as $(a)_n = b$, is defined to mean $(a - b) = qn$ for some integer q . Find all numbers x such that $(3x)_{19} = 5$. (15%)
9. Find the language recognized by the given deterministic finite-state automaton. (10%)

