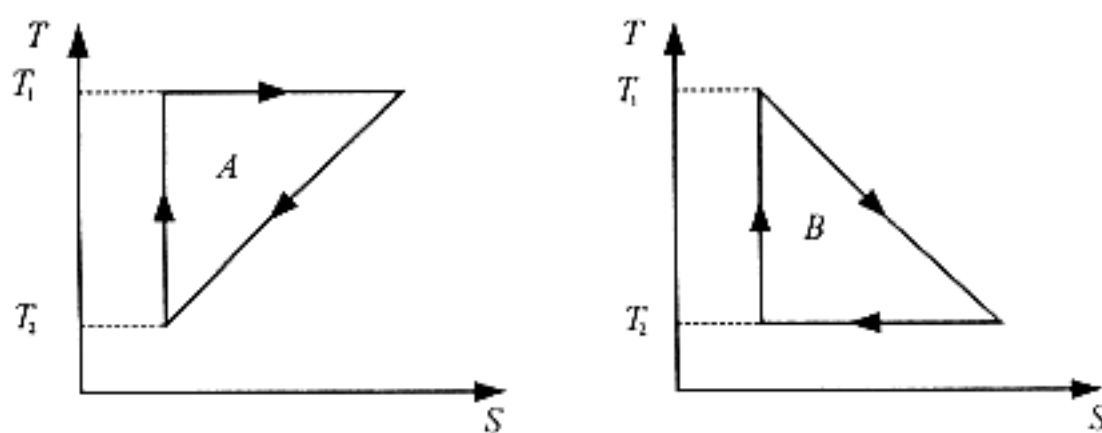


1. One mole of gas obeys Van der Waals equation of state,  $(p + a/V^2)(V - b) = RT$ . If its molar internal energy is given by  $u = cT - a/V$  (in which  $V$  is the molar volume,  $a$  is one of the constants in the equation of state, and  $c$  is a constant), calculate the molar heat capacities  $C_v$  and  $C_p$ . (20%)
2. One mole of a monatomic perfect gas initially at temperature  $T_0$  expands from  $V_0$  volume to  $2V_0$ , (a) at constant temperature, (b) at constant pressure. Calculate the work of expansion and heat absorbed by the gas in each case. (20%)
3. A body of constant heat capacity  $C_p$  and a temperature  $T_i$  is put into contact with a reservoir at temperature  $T_f$ . Equilibrium between the body and the reservoir is established at constant pressure. Determine the total entropy change and prove that it is positive for either sign of  $(T_f - T_i)/T_f$ . You may regard  $|T_f - T_i|/T_f < 1$ . (20%)

4. (a) Derive the expression for the efficiency of a Carnot engine directly from a  $TS$  diagram.  
 (b) Compare the efficiencies of cycles  $A$  and  $B$  of the following figures. (20%)



5. The state of a new matter is  $p = AT^3/V$ , where  $p$ ,  $V$  and  $T$  are the pressure, volume and temperature, respectively,  $A$  is a constant. The internal energy of the matter is

$$U = BT^n \ln(V/V_0) + f(T)$$

where  $B, n$  and  $V_0$  are all constants,  $f(T)$  only depends on the temperature. Find  $B$  in term of  $A$ , and the value of  $n$ . (20%)