

※ 考生請注意：本試題可使用計算機。請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

1. A diatomic ideal gas is at 300 K and 1 bar initially. Calculate  $w$ ,  $\Delta H$ ,  $\Delta S$ , and  $\Delta G$  after adiabatic free expansion until the volume is doubled. **(16%)**
2. A cell  $\text{Cu}(s) | \text{CuCl}_2(0.01 \text{ mol kg}^{-1}) | \text{AgCl}(s) | \text{Ag}$  is constructed. It is known that the standard electrode potentials of Cu and AgCl at 298K are as follows:
- $$\text{Cu}^{2+} + 2e^- \rightarrow \text{Cu}(s) \quad E^\circ = 0.3419 \text{ V}$$
- $$\text{AgCl}(s) + e^- \rightarrow \text{Ag}(s) + \text{Cl}^- \quad E^\circ = 0.22233 \text{ V}$$
- (a) Write the cell reaction (3%) and give the standard electromotive force ( $E^\circ$ ) (3%); (b) Estimate the mean ionic activity coefficient of  $\text{Cu}^{2+}$  and  $\text{Cl}^-$  ions using Debye-Hückel limiting law (4%) (c) Calculate the electromotive force ( $E$ ) (4%) and the reaction Gibbs energy ( $\Delta G$ ) (3%) of the cell. **(17%)**
3. Derive the following relationships:
- (a) Prove that  $\left(\frac{\partial C_v}{\partial V}\right)_T = T \left(\frac{\partial^2 P}{\partial T^2}\right)_V$  (8%); (b)  $\left(\frac{\partial S}{\partial V}\right)_U = \frac{P}{T}$  (8%) **(16%)**
4. Suppose that a reaction of stoichiometry  $\text{A} + 2\text{B} = 2\text{Y} + 2\text{Z}$  is believed to occur according to the mechanism
- $$\text{A} \xrightleftharpoons[k_{-1}]{k_1} 2\text{X}$$
- $$\text{X} + \text{B} \xrightarrow{k_2} \text{Y} + \text{Z}$$
- (a) If the first step reaches the equilibrium very rapidly as compared to the second step, derive the expression for the rate of formation of the product Y. (8%)
- (b) Derive the expression for the activation energy ( $E_a$ ) of the above rate expression in terms of  $E_1, E_{-1}, E_2$ , which denote the activation energies for the rate constants  $k_1, k_{-1}, k_2$ , respectively. (8%) **(16%)**
5. The equation of state for a van der Waals gas is  $(P + \frac{a}{V_m^2})(V_m - b) = RT$ ,
- (a) prove that  $a = 3P_c V_c^2$  and  $b = \frac{V_c}{3}$ , in which  $P_c, V_c, T_c$  are the critical  $P, V, T$ , respectively. (8%);
- (b) derive the reduced equation of state and describe the law of correspondence state (8%). **(16%)**
6. Answer the following questions: **(19%)**
- (a) Determine the number of degrees of freedom and suggest the required variables for an aqueous solution

of potassium chloride and sodium chloride at 1 atm. (4%)

- (b) The combustion of  $C_2H_5OH_{(l)}$  in a bomb calorimeter produces about  $1364 \text{ kJ mol}^{-1}$  at  $25^\circ\text{C}$ . Calculate  $\Delta H_m$  for the combustion reaction at  $25^\circ\text{C}$ :  $C_2H_5OH_{(l)} + 3O_{2(g)} = 2CO_{2(g)} + 3H_2O_{(l)}$  (4%)
- (c) Suppose that a refrigerator cools to 250 K and discharges heat at 300 K. If the refrigerator operates with an efficiency of the 25% of the maximum theoretical coefficient of performance (COP), how much work would be required to freeze 18 kg of water ( $\Delta_f H \approx -6.0 \text{ kJ mol}^{-1}$ ) (4%)
- (d) The molar conductivities at infinite dilution ( $\Lambda^\circ$ ) of KCl, KI, and NaCl are 149.79, 150.31, and  $126.39 \text{ Scm}^2 \text{ mol}^{-1}$ . Calculate the  $\Lambda^\circ$  of NaI. (4%)
- (e) The main difference between Langmuir adsorption isotherm and BET adsorption isotherm. (3%)

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