

國立成功大學

112學年度碩士班招生考試試題

編 號： 79

系 所： 化學工程學系

科 目： 物理化學

日 期： 0206

節 次： 第 3 節

備 註： 可使用計算機

※ 考生請注意：本試題可使用計算機。請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

1. (a) For the reversible and adiabatic expansion/compression of an ideal gas, prove that $\frac{T_1}{T_2} = \left(\frac{P_1}{P_2}\right)^{\gamma-1/\gamma}$, in which $\gamma = C_p / C_v$ (6%). (b) For a monoatomic ideal gas at 300 K and 1 bar, calculate the work (4%) and entropy change (4%) for its reversible and adiabatic compression to 5 bar. **(14%)**

2. Consider the concentration cell $\text{Cu} | \text{CuCl}_2(0.005 \text{ m}) :: \text{CuCl}_2(0.01 \text{ m}) | \text{Cu}$ in which two CuCl_2 solutions are separated by a partition. The partition is permeable to both Cu^{2+} and Cl^- ions, and the speed ratio of Cu^{2+} and Cl^- ions through the partition equals to the ratio of their transport numbers (t_+ and t_-). (a) Assuming the junction potential for the partition is zero and the activity coefficients are unity, derive the expression for the electromotive force (emf) of this cell. (6%) (b) Calculate the transport number of Cu^{2+} ions (3%) and the emf of this cell (4%). (i.e., the molar conductivities of $\frac{1}{2} \text{Cu}^{2+}$ and Cl^- ions at infinite dilution of 25°C are 56.6 and 76.31 $\text{S cm}^2 \text{mol}^{-1}$, respectively) **(13%)**

3. Consider the consecutive first-order reaction $\text{A} \xrightarrow{k_1} \text{B} \xrightarrow{k_2} \text{C}$

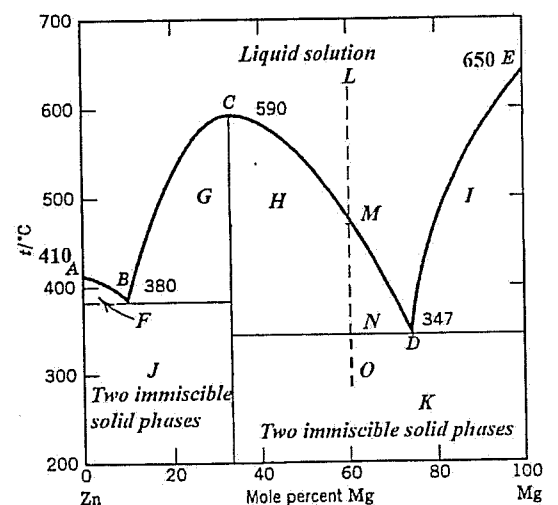
Neither B nor C is present initially. It has been proven that $[\text{B}] = \frac{k_1[\text{A}]_0}{k_2 - k_1} (e^{-k_1 t} - e^{-k_2 t})$

- (a) Under what condition is the induction period for the formation of C clearly observed? (3%)
 (b) Under what condition does the existence of B become invisible (i.e., very short life)? (3%)
 (c) Calculate the time to reach the maximum B concentration if the initial concentration of A ($[\text{A}]_0$) is 1.0 mol dm^{-3} , $k_1 = 5 \text{ s}^{-1}$ and $k_2 = 2 \text{ s}^{-1}$. (5%)
 (d) If the consecutive reaction becomes reversible ($\text{A} \xrightleftharpoons[k_{-1}]{k_1} \text{B} \xrightleftharpoons[k_{-2}]{k_2} \text{C}$) with $k_{-1} = 4 \text{ s}^{-1}$ and $k_{-2} = 1 \text{ s}^{-1}$, derive the equilibrium B concentration and calculate the value (4%). **(15%)**

4. The right figure is the solid-liquid phase diagram of Zn and Mg at a constant pressure.

- (a) Explain what is the congruent melting compound and determine its chemical formula (4%)
 (b) Write the eutectic composition(s) (2%)
 (c) Draw the cooling curve (temperature vs. time) for the liquid solution from L to O (2%)
 (d) Write the composition for area G (2%)
 (e) Determine the number of degrees of freedom (3%) and suggest the required variables for the curve C-M-D (2%)

(15%)



5. (a) Prove that $\Delta_{mix}H = 0$ and $\Delta_{mix}S = -R \sum x_i \ln x_i$ for ideal solutions. (8%)
 (b) Explain why $\Delta_{mix}H = 0$ but $\Delta_{mix}S \neq 0$ for ideal solutions from the microscopic viewpoint. (4%)
 (12%)
6. Answer the following questions: (31%)
- (a) An electrolyte exhibits lower molar conductivity at higher concentrations. Why? (4%)
- (b) For the isothermal expansion of an ideal gas, the work done by the irreversible process is less than that by the reversible process. Where does the lost work go (3%), and what kind(s) of energy (U, H, A, G) decrease(s) in the system? (2%)
- (c) What is the Joule-Thomson inversion temperature? (3%)
- (d) For the following compounds: CO, CO₂, H₂O, N₂O, and O₂, whose residual entropy at the absolute zero temperature is zero? (4%)
- (e) A first-order surface reaction occurs on the surface of a spherical vessel of radius 10 cm with a rate of $2.5 \times 10^{-3} \text{ mol dm}^{-3} \text{ s}^{-1}$ and a rate constant of $7.5 \times 10^{-4} \text{ s}^{-1}$. What will be the rate and the rate constant if the radius is increased to 50 cm at the same pressure and temperature? (4%)
- (f) For the isothermal expansion/compression of a real gas, prove that $\Delta H = -C_p \mu_{JT} \Delta P$, where C_p (heat capacity at constant pressure) and μ_{JT} (Joule-Thomson coefficient) are independent of pressure. (5%)
- (g) The following figure shows the vapor-liquid phase diagram of a binary system. During the pressure reduction of the liquid solution at $x_1=0.2$ from 90 bar, what is the pressure at which the liquid starts to generate bubbles and what is the composition of bubbles (i.e., $y_1=?$)? Also, what is the activity coefficient? (6%)

