

※ 考生請注意：本試題不可使用計算機。請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

1. (20 %) Consider a viscous fluid flows in laminar motion down an inclined plate at angle θ (Fig. 1). Assume the flow depth is constant. The velocity profile is $\vec{u} = \alpha y(2h - y)$, $v = w = 0$. Find:
- (a) the constant α in terms of specific weight, viscosity and the angle θ ;
 - (b) the volume flux Q per unit width.

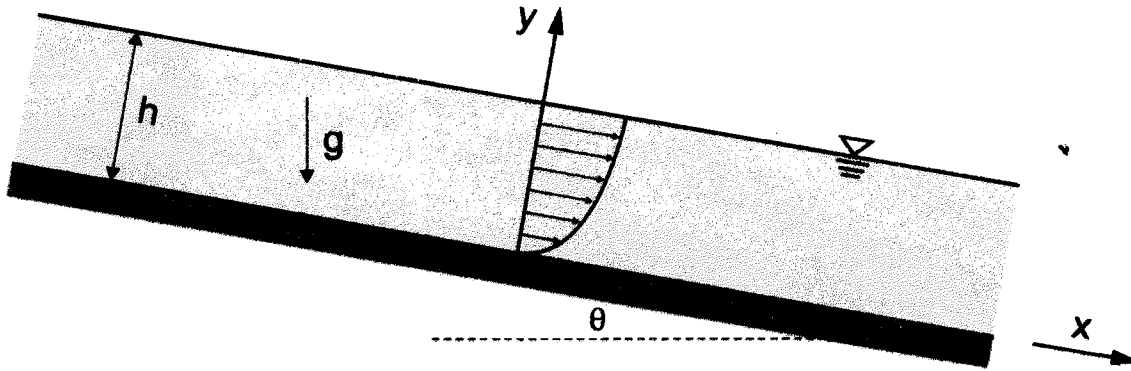


Figure 1

2. (12%) Find a relation between nozzle discharge velocity V_2 and tank free surface height h as in Fig. 2. Assume steady frictionless flow.

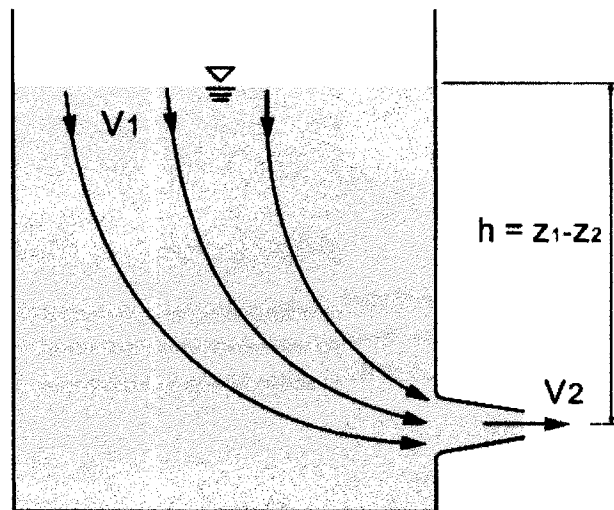


Figure 2

3. (30 %) Consider a steady uniform laminar flow moving on a flat plate. The velocity profile is

$$\frac{u}{u_{\infty}} = a + b \left(\frac{y}{\delta}\right) + c \left(\frac{y}{\delta}\right)^2$$

where a, b, c are constants to be determined. Find:

- (a) boundary thickness (δ)
- (b) displacement thickness (δ^*)
- (c) momentum thickness (θ)
- (d) wall shear stress (τ_0)
- (e) friction coefficient (C_f)
- (f) drag coefficient (C_{Df})

4. (10%) Write down Navier-Stokes equation and explain the physical meaning of each term.

5. (28%) Explain shortly of the following terms. (Note: NOT just translation)

- (a) Froude number and Reynolds number
- (b) Bernoulli principle
- (c) D'Alembert paradox
- (d) material derivative
- (e) Kármán vortex street
- (f) source and sink
- (g) boundary layer thickness