

系所組別： 航空太空工程學系丙組

考試科目： 自動控制

考試日期： 0219，節次： 1

※ 考生請注意：本試題 可 不可 使用計算機

1. (20%) Assume you are given the system as shown in Figure 1:

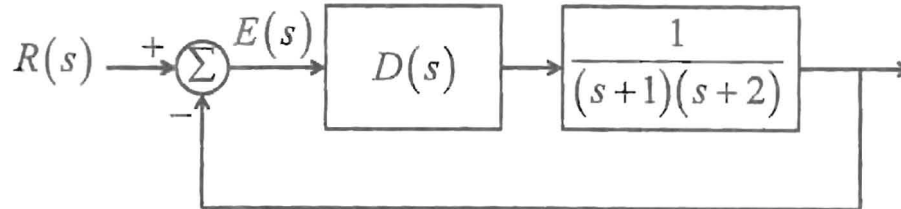


Figure 1

Your job is to design a compensator, $D(s)$ that meets the following specs:

- The closed-loop system has poles at $s = -2 \pm 1j$
- The steady-state error due to a step input equals 0.1
- No poles or zeros of $D(s)$ can be faster than $s = -2$.

What is your $D(s)$?

(背面仍有題目,請繼續作答)

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2. (30%) The feedback control system shown in Figure 2 is to be designed to satisfy the following specifications: (1) steady-state error of less than 10% to a ramp reference input, (2) maximum overshoot for a unit step input is less than 5%, and (3) 1% settling time of less than 3 sec.

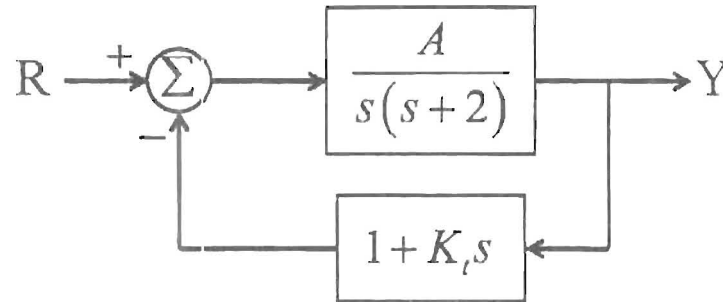


Figure 2

- Compute the closed-loop transfer function.
- Sketch the region in the complex plane where the closed-loop poles may lie (i.e. the region that meets the specifications).
- What does specification (1) imply about the possible values of A ?
- What does specification (3) imply about the closed-loop poles?
- Find the error due to a unit ramp input in terms of A and K_t .
- Suppose $A = 32$. Find the value of K_t that yields closed-loop poles on the right-hand boundary of the feasible region. Does this choice for K_t satisfy the desired specifications?
- Using $A = 32$ and the value for K_t computed in part (f), estimate the settling time of the system.

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3. Consider a closed-loop control system shown in Figure (3) with the open-loop transfer

$$\text{function } G(s) = \frac{b_2s^2 + b_1s^1 + b_0}{s^n(a_3s^3 + a_2s^2 + a_1s^1 + a_0)}, \quad a_0 \neq 0, \quad b_0 \neq 0 \text{ and } k=1.$$

The plot of the frequency response $G(j\omega)$ for $\omega > 0$ is shown in Figure (4).

5%(a). $n = ?$

10%(b). Suppose that the Nyquist path in the s plane encloses the entire right-half s plane, draw a complete Nyquist plot in the G plane.

5% (c). If $G(s)$ has one zero and two poles in the open right-half s plane, is the closed-loop system stable?

5%(d). Are there any closed-loop poles which are on the imaginary axis? Why?

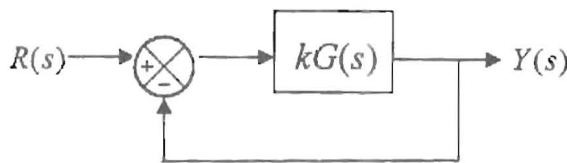


Figure (3)

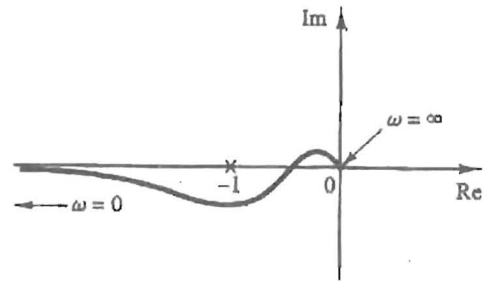


Figure (4)

4. Consider a closed-loop control system shown in Figure (3) with the open-loop transfer

$$\text{function } G(s) = \frac{20}{s(s+1)(s+5)}, \quad k > 0. \text{ The Bode diagram of } G(s) \text{ is shown in Figure (5)}$$

and the Bode diagram of closed-loop transfer function $M(s) = \frac{Y(s)}{R(s)}$ with $k=1$ is shown in Figure (6).

5%(a). What is the gain margin GM of the closed-loop system?

5%(b). What is the phase margin PM of the closed-loop system?

5%(c). What is the resonant frequency ω_r of the closed-loop system?

10%(d)., What is the gain margin of the closed-loop system if we set $k=10$.

<Note : Reading data from the bode diagram is enough to answer questions (a),(b) and (c) .>

(continued)

(背面仍有題目,請繼續作答)

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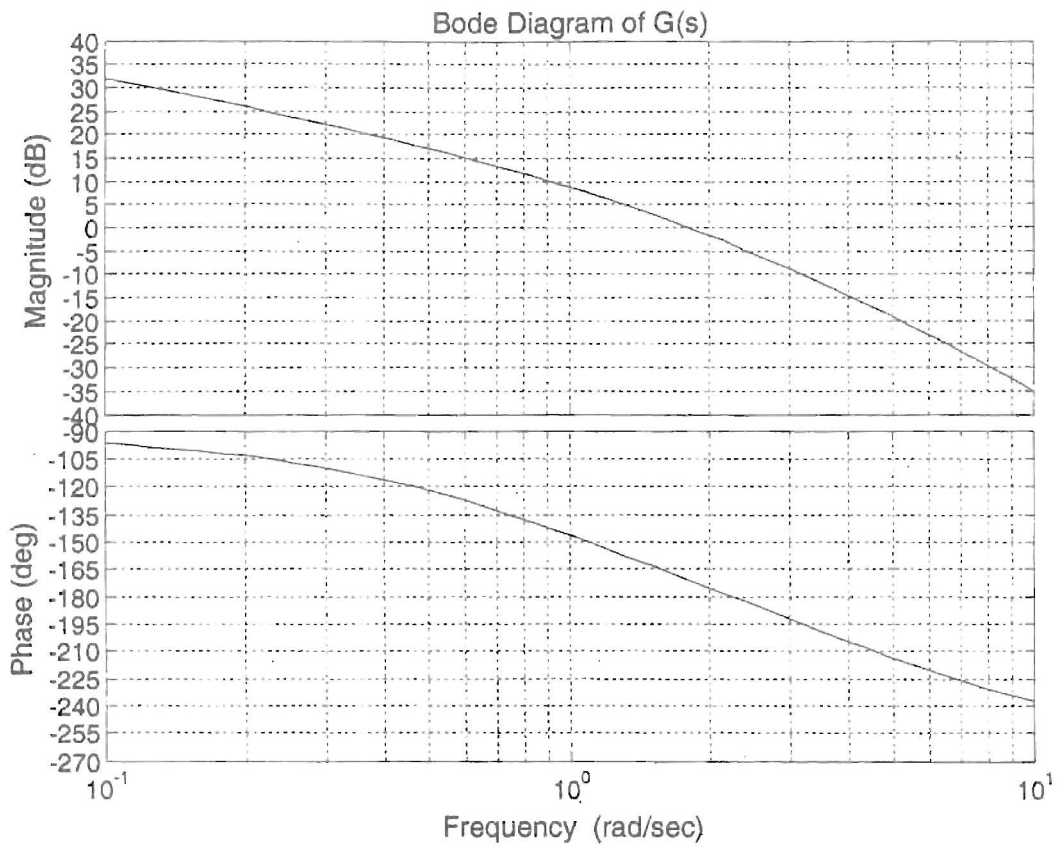


Figure (5)

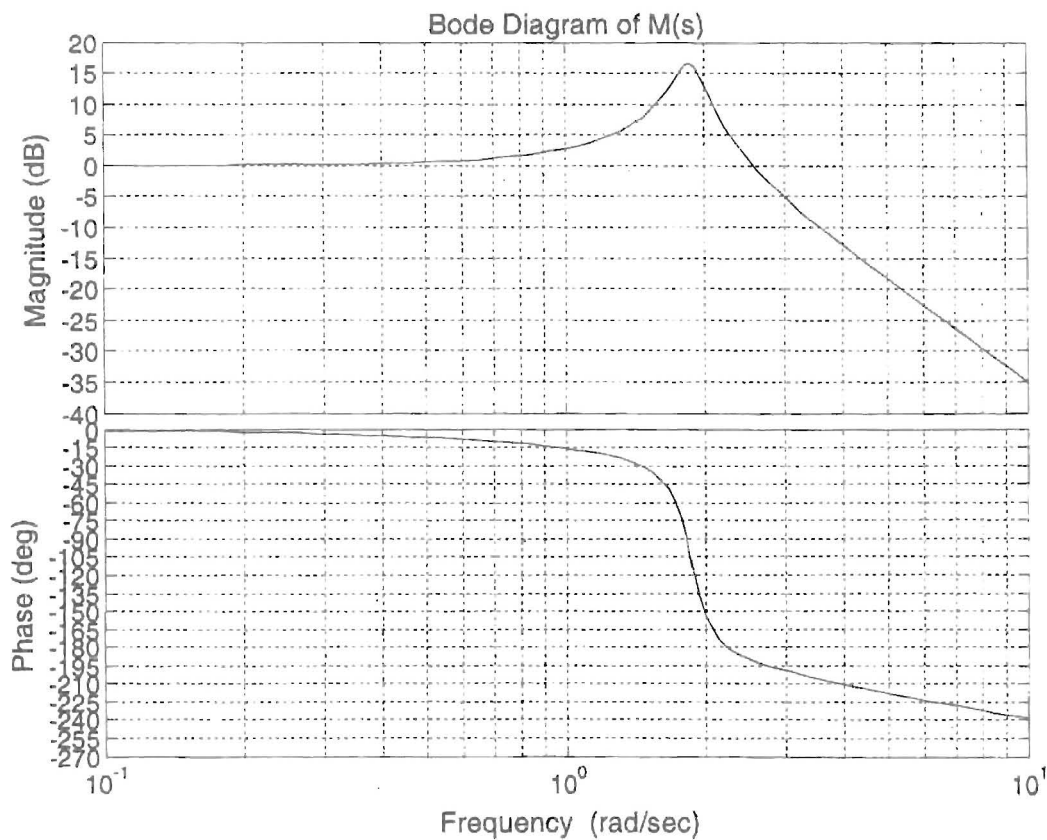


Figure (6)