1．（20\％）A particle having a mass $m$ and a velocity $v_{m}$ in the $y$ direction is projected onto a horizontal belt that is moving with a uniform velocity $v_{b}$ in the $x$ direction．There is a coefficient of sliding friction $\mu$ between the belt and the particle．Assuming that the particle first touches the belt at the origin of the fixed $x y$ coordinate system and remains on the belt，find the coordinate $(x, y)$ of the point where sliding stops．


2．（30\％）Three masses are of the same mass，$m$ ．Mass $m_{1}$ hits $m_{2}$ with inelastic impact（ $e=0$ ）while sliding horizontally with velocity $v$ along the common line of centers of the three equal masses．Initially，masses $m_{2}$ and $m_{3}$ are stationary and the spring is unstressed．Find
（a）The velocities of $m_{1}, m_{2}$ ，and $m_{3}$ immediately after impact；
（b）The maximum kinetic energy of $m_{3}$ ；
（c）The minimum kinetic energy of $m_{2}$ after impact；
（d）The maximum compression of the spring；
（e）The final motion of $m_{1}$ ．


Frictionless

系所組別：航空太空工程學系丙組
考試科目：動力學
※ 考生請注意：本試題不可使用計算機。 請於答案卷（卡）作答，於本試題紙上作答者，不予計分。
3．Derive the equations of motion or the dynamic model of the spring－bar system as shown in figure 3 ．The length and the mass of the slender uniform bar are land $m$ ，respectively．Also，spring constant is $K$ ．（ $25 \%$ ）


Figure 3

4．Consider the rotating thin disc system in figure 4.
a．Derive the angular momentum of the thin disc for constant $\omega_{1}$ and $\omega_{2}$ ． Also，the mass of the disc is m ．（15\％）
b．What is the torque at O on the disc？$(10 \%)$


Figure 4

