

國立成功大學  
110學年度碩士班招生考試試題

編 號： 132

系 所： 航空太空工程學系

科 目： 自動控制

日 期： 0202

節 次： 第 1 節

備 註： 不可使用計算機

※ 考生請注意：本試題不可使用計算機。請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

1. Consider a system represented by the following differential equations:

$$Ri_1(t) + L_1 \frac{di_1(t)}{dt} + v(t) = v_a(t), \quad L_2 \frac{di_2(t)}{dt} + v(t) = v_b(t), \quad \text{and} \quad i_1(t) + i_2(t) = C \frac{dv(t)}{dt},$$

where  $R$ ,  $L_1$ ,  $L_2$ , and  $C$  are given constants, and  $v_a$  and  $v_b$  are inputs. Draw a block diagram to represent the system where the output is  $v$ . Also, obtain the transfer functions for  $\frac{V(s)}{V_a(s)}$  and  $\frac{V(s)}{V_b(s)}$ . (25%)

2. For a system transfer function given as:

$$\frac{Y(s)}{R(s)} = \frac{s+8}{s^2+4s+8} \quad \text{and} \quad R(s) = \frac{1}{s},$$

derive the output function  $y(t)$ , the rise time  $t_r$ , and the peak time  $t_p$ , where the rise time is defined as the first time when  $y(t)=r(t)$  evaluated from  $t=0$ . (25%)

3.

- (a). Sketch the Nyquist and Bode plot of the following system shown in Fig.3 with  $K = 1$ , please also provide the Nyquist  $\mathcal{D}$  contour plot. (20%)
- (b). Determine the range of  $K$ , such that the closed-loop is stable by Nyquist plot. (5%)
- (c). Determine the gain  $K$ , such that the gain margin of the system is 6dB. (5%)

$$KG(s) = \frac{K(s-5)}{s(s+10)}$$

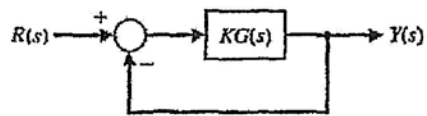


Fig.3

4.

Consider the system shown in Fig. 4. Design a controller  $G_c(s)$  such that the closed-loop system satisfies the following system specifications. (10%)

- (a). zero steady state error to a step input  $R(s)$ , and
- (b). the complex closed-loop poles having damping ratio = 0.5 and natural frequency = 1.5 rad/s

Sketch the root locus of the compensated system  $kG_c(s)G(s)$ . (10%)

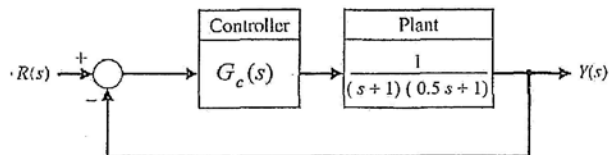


Fig.4