

1. Consider the motion of the propeller of an airplane making a turn. For simplicity, we shall suppose that the center  $O$  of the propeller describes a horizontal circle  $C$  with constant speed  $V$ ; let  $b$  be the radius and  $A$  the center of  $C$ . Fig. P1 shows the position of the propeller when the line from the center to the tip  $B$  makes an angle  $\theta$  with the vertical and the length of  $\overline{OB}$  is  $l$ . Find
- (1) the velocity, (8%)
  - (2) the absolute speed, (5%)
  - (3) the acceleration (12%)  
of the tip of the propeller.

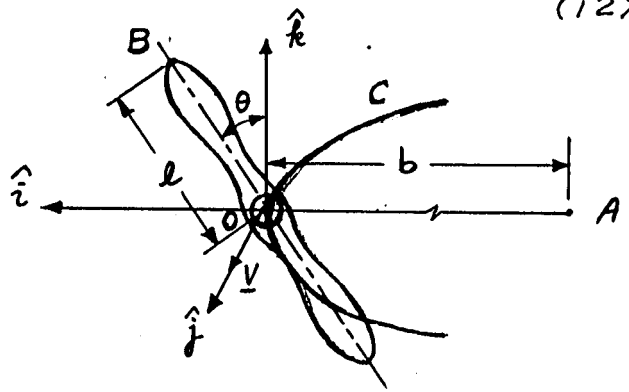


Fig. P1

2. A particle  $P$  of mass  $m$  is suspended from a massless linear spring with spring constant  $K$  and undeformed length  $L$ , as shown in Fig. P2. Use the indicated generalized coordinates  $q_1$  and  $q_2$  to find the following:
- (1) The kinetic energy  $T$ , (5%)
  - (2) The generalized forces  $Q_1$  and  $Q_2$ , (5%)
  - (3) The potential energy  $V$ , (5%)
  - (4) The equations of motion. (10%)

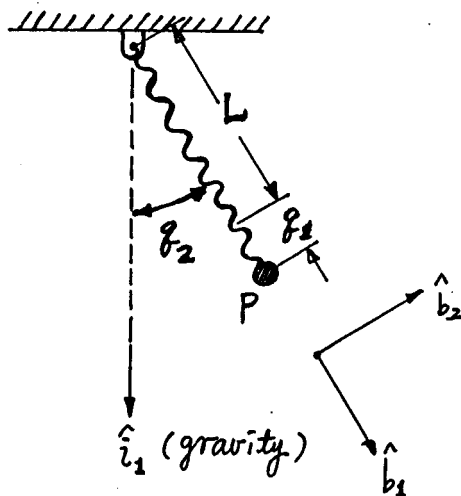


Fig. P2

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3. A right circular cone which is shown in Fig. P3, weighting 20 N is spinning like a top about a fixed point O at a speed  $\dot{\phi}$  of 15,000 rad/sec. What are two possible precession speeds for  $\theta = 30^\circ$ ? (20%)

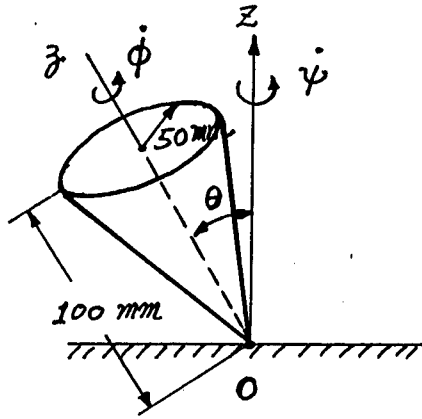


Fig. P3

4. The weight  $W = 200$  lb hangs on a pulley A free to rotate in frictionless bearing as shown in Fig. P4. The coefficient of friction between the facing of brake B and the pulley is 0.25. What minimum force P is needed to prevent rotation? (30%)

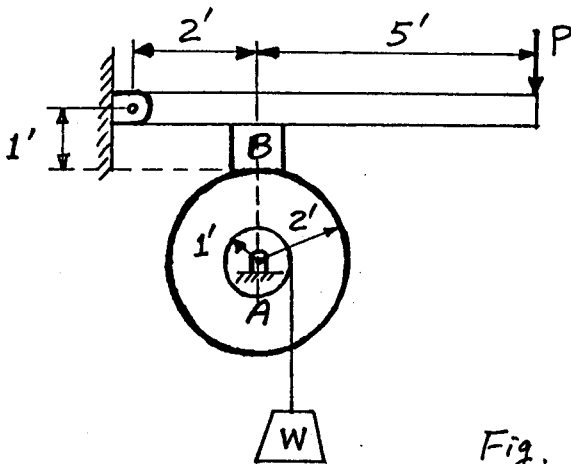


Fig. P4