

25% 1) The transfer function of a control network is determined to be

$$G(s) = \frac{s}{(1 + 0.5s)(1 + 0.12s + 0.04s^2)}$$

- a. Find the breaking frequency.
- b. Calculate the damping ratio ζ .
- c. Draw the Bode plot of the network by a relation of magnitude(db) to frequency(ω).

25% 2) An airplane is having a dynamics as follows:

$$\dot{u} = -0.08 u - 32.2 \theta \quad \dot{\alpha} = q - 0.0004 u - \alpha \quad \dot{q} = -3.6 \alpha - 3.6 \delta \quad \dot{\theta} = q$$

- a. Find the transfer function for Θ/Δ where Θ and Δ are the Laplace transform of θ and δ respectively.
- b. Take $K = -2$ for the closed-loop system shown in Fig. 1. Write the transfer function for Θ/Θ_i . Use the Routh-Hurwitz discriminant to determine the stability of the system.

25% 3) Correlate the Nyquist plots, step responses and frequency responses shown in Fig. 2.

25% 4) Two Nyquist diagrams for unity feedback systems that are open-loop stable are sketched in Fig. 3 and Fig. 4. The proposed operating gain is indicated as K_0 , and arrow indicate increasing frequency. In each case give your best estimate for a) Phase margin b) Range of gain for stability (if any) and c) System types as 0, I or II.

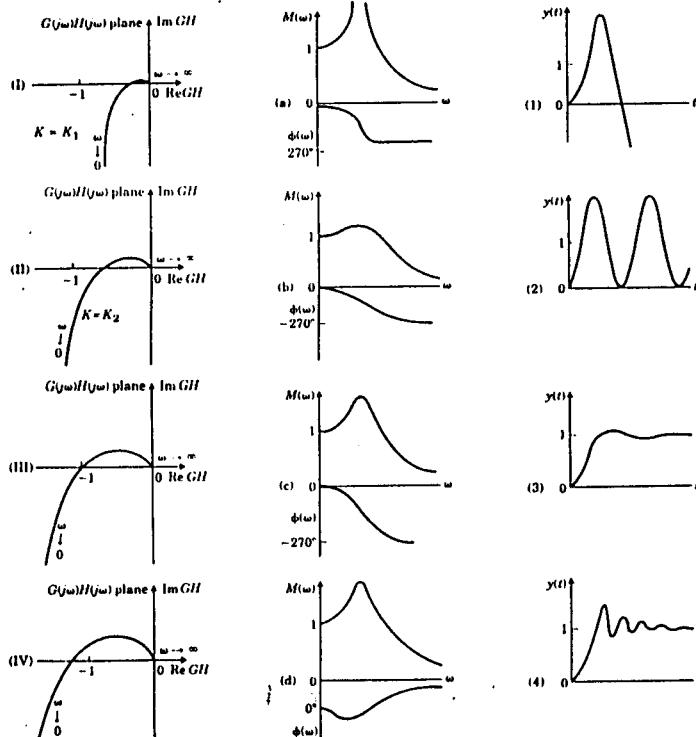


Fig. 2

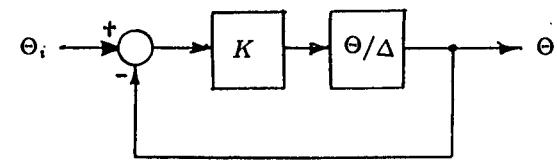


Fig. 1

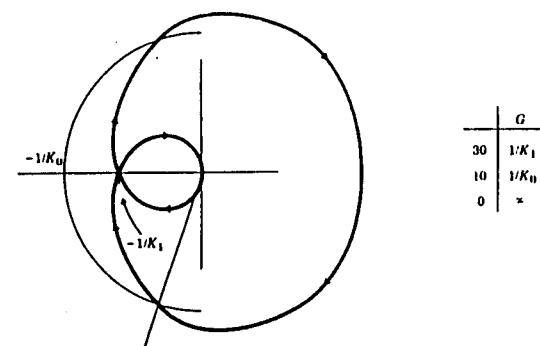


Fig. 3

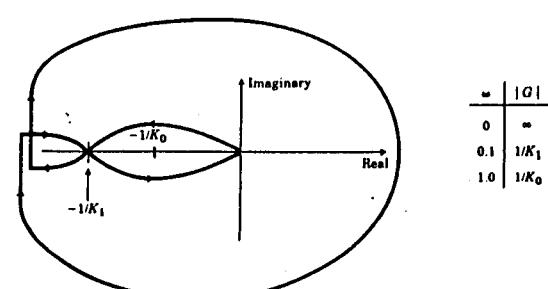


Fig. 4