(20%) 1. Explain the following terms:

- (a) Aerodynamic Center
- (b) Pressure Center
- (c) Mean Aerodynamic Chord
- (d) Coanda Effect
- (e) Kutta Condition

(20%) 2. If the drag coefficient is shown in the polar form

$$C_D = C_{D_0} + KC_L^2$$

where  $C_{D_0}$  and K are constant

- Find (a) the lift coefficient for maximum lift/drag ratio,
  - (b) the maximum lift/drag ratio

in terms of  $C_{D_0}$  and K.

- ( 20%) 3. Consider a two-dimensional thin and symmetric airfoil with a trailing-edge flap hinged at the 0.8 chord length point. The flow is inviscid and incompressible. The classical thin airfoil theory is valid.
  - (a) When the flap deflection is zero, draw a typical  $\alpha C_l$  diagram where  $C_l$  is the lift coefficient and  $\alpha$  is the angle of attack. Indicate on your figure the zero-lift angle of attack  $\alpha_{L=0}$ , the stall angle  $\alpha_{stall}$  and the maximum lift coefficient  $C_{l,max}$ . What are the value of the slope of the lift curve  $\frac{\partial C_l}{\partial \alpha}$  and the value of the zero-lift angle of attack  $\alpha_{L=0}$  in this symmetric case?
  - (b) When the flap deflection is positive (downward), say  $10^{\circ}$ , draw a typical  $\alpha C_l$  curve on the same figure as in (a), showing the effects of the flap deflection. Comparing with the case of zero flap deflection, will the coefficients  $C_{l,max}$ ,  $\frac{\partial C_l}{\partial \alpha}$ ,  $\alpha_{L=0}$  and  $\alpha_{stall}$  increase or decrease? Discuss each term separately.
  - (c) When the flap deflection is negative (upward), say  $-10^{\circ}$ , draw a typical  $\alpha C_l$  curve on the same figure as in (a) and (b), showing the effects of the flap deflection. Comparing with the case of zero flap deflection, will the coefficients  $C_{l,max}$ ,  $\frac{\partial C_l}{\partial \alpha}$ ,  $\alpha_{L=0}$  and  $\alpha_{stall}$  increase or decrease? Discuss each term separately.

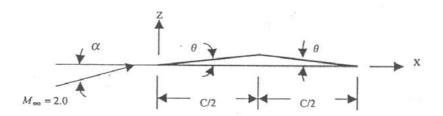
(2%) 4. A triangular-shaped airfoil when placed in a supersonic flow can be approximated using the linearized potential flow equation

$$(M_{\infty}^2 - 1)\phi_{xx} - \phi_{zz} = 0$$

and the general solution to this governing equation can be found to be

$$\phi(x,z)=f(x+Bz)+g(x-Bz), \qquad B=\sqrt{M_{\infty}^2-1}$$

- a) Determine the functions f(x) and g(x).
- b) Calculate the pressure coefficient  $C_p$  along the two sides of the airfoil.
- c) Obtain the lift coefficient  $C_{l}$ .



Note: 1) You are asked to derive the  $C_P$  and  $C_L$ .

Directly employing formulas will get no credits.

2) 
$$C_P = -\frac{2}{U_{\infty}} \frac{\partial \phi}{\partial x}$$

## Aerodynamics

5. Describe the different types of drags experienced by a finite wing in a subsonic, high subsonic and supersonic flow. In each case state the relevant flow properties of the wing that has the greatest effect on the magnitude of the drag.