194 197

## 國立成功大學九十六學年度碩士班招生考試試題

共2頁,第/頁

絙號:

188 系所:航空太空工程學系甲組 飞帆 千年組科目:工程數學

一百两万艇

本試題是否可以使用計算機: ☑可使用 , □不可使用 (請命題老師勾選)

20%[1]

- (a). Find the general solution to the following equation:  $\frac{d^2y}{dt^2} \frac{dy}{dt} 2y = 3e^{2t}.$
- (b). Find the solution to the above equation for y(0) = 3 and  $\frac{dy}{dt}\Big|_{t=0} = 4$ .

[2]

Solve the system of equations  $\dot{x}(t) = Ax(t) + B(t)$ ,

where 
$$A = \begin{bmatrix} 3 & -1 \\ -1 & 3 \end{bmatrix}$$
,  $B(t) = \begin{bmatrix} -2 \\ -2 \end{bmatrix}$ ,  $x(t) = \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix}$ ,  $x(0) = \begin{bmatrix} 2 \\ 2 \end{bmatrix}$ 

5%(a). What are the eigenvalues of matrix A?

15%(b). What is the solution x(t) to the system?

20%[3]

(a). Find the coordinates (x, y, z) of the point on the plane

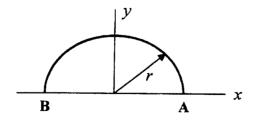
$$ax + by + cz = d$$
 with  $a^2 + b^2 + c^2 = 1$ ,

which is closest to the origin. Also find the shortest distance from the origin to the plane.

(b). Evaluate the line integral

$$I = \int_{C} f \, ds \,,$$

where  $f = x^2y$  and C is the semicircular arc of radius r from A to B as shown in the figure.



(背面還有題目,請繼續作答)

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共 2 頁,第2頁

絙赊:

188 系所:航空

:航空太空工程學系甲組 氏脈 門中組科目:工

2,70,1 MB

(請命題老師勾選)

20%[4]

Use the Fourier series method to solve the problem:

$$u_t = 4u_{xx}$$
  $0 < x < 2, t > 0$ 

$$u(0,t) = u(2,t) = 0,$$
  $t > 0$ 

$$u(x, 0) = 2 - 2\cos(\pi x) + 4\sin(2\pi x),$$
  $0 < x < 2$ 

[5]

12% (a). State the sufficient and necessary conditions such that a complex function is analytic. How about the relation between these conditions and the uniqueness of the derivative f(z)? Please use  $f(z) = \frac{1}{1-z}$  to explain your answer. Is this f(z) analytic at the point z = 1? Is this f(z) analytic at points satisfy |z| > 0.001?

8% (b). Find the complex integration  $\oint_C \frac{1}{1-z} dz = ?$  along the following closed curves in the counterclockwise sense.

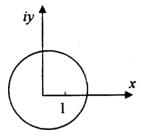


Figure 1

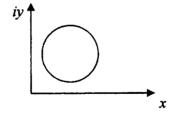


Figure 2