

※ 考生請注意：本試題 可 不可 使用計算機

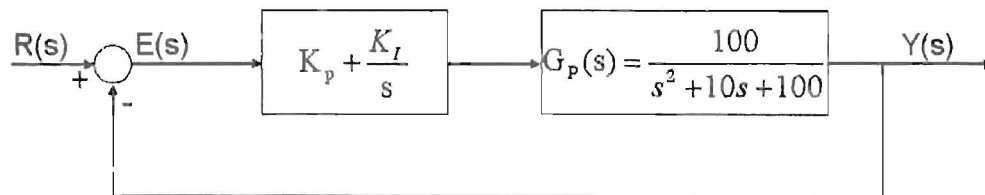
1、Sketch the root locus of a unity feedback system whose transfer function is (10%)

$$G(s) = \frac{K(s+2)}{(s+1)(s^2+6s+10)}$$

2、A control system with a type 0 process $G_p(s)$ and a PI controller is shown in Fig 1. (20%)

(a) Find the value of K_I so that the ramp-error constant K_V is 10.

(b) Find the value of K_P so that the magnitude of the imaginary parts of the complex roots of the characteristic equation of the system is 15 rad/sec. Find the roots of the characteristic equation.



3、If the following transfer function is excited with an input signal of the form: (20%)

$$y(t) = 4.4\sin(400t)$$

Calculate at the following input conditions: (a) Magnitude in dB (b) Magnitude as a gain (c) Phase (angle in degrees) (d) Steady-state, sinusoidal output

$$T(s) = \frac{25}{\left(\frac{s}{200} + 1\right)}$$

4、Consider the following dynamic system (20%)

$$\frac{d}{dx} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(t)$$

(a) Determine the state-transition matrix $\Phi(t)$

(b) When the input is $u(t) = 1$ for $t \geq 0$, and the initial state is zero, determine the time response (state vector $x(t)$) of the above system

(背面仍有考題)

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5、A controlled process is modeled by the following state equations. (15%)

$$\frac{dx_1(t)}{dt} = x_1(t) - 2x_2(t) \quad \frac{dx_2(t)}{dt} = 10x_1(t) + u(t)$$

The control $u(t)$ is obtained from state feedback such that

$$u(t) = -k_1x_1(t) - k_2x_2(t)$$

where k_1 and k_2 are real constants. Determine the region in the k_1 -versus- k_2 parameter plane in which the closed-loop system is asymptotically stable.

6、Determine the transfer function $\frac{x(s)}{F(s)}$ for the following system. where F : force input, m : mass, k : spring constant, b_1, b_2 : damping constants, x : displacement of the mass (15%)

