系所組別：系統及船舶機電工程學系乙組
考試科目：動力學

## ※ 考生請注意：本試題不可使用計算機

## Attention：

In general，a free－body diagram along with your equations is necessary in order to explain the procedures to solve the problem．Mathematical calculation for the answer is not necessary
（1）A small box of mass $m$ is given a speed of $V=\sqrt{\frac{1}{4} g r}$ at the top of the smooth half cylinder．Draw a free－body diagram and explain how to find the angle $\theta$ at which the box leaves the cylinder．（15\％）


Fig 1
（2）Use the concept of instantaneous center of zero velocity to find the velocity of point $E$ on link $B C$ and the angular velocity of link $A B$ at the instant shown in Fig 2. （15\％）


Fig 2.
（3）Use a rotating coordinate system attached to rod $A B$ and draw a free－body diagram， then write down all the necessary information and equations in order to find angular velocity and angular acceleration of rod CD．Explain your calculation． （15\％）


Fig． 3

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（4）The $20-\mathrm{kg}$ square plate is pinned to the $5-\mathrm{kg}$ smooth collar at A ．Determine the initial linear acceleration and angular acceleration of the plate when $P=100 \mathrm{~N}$ is applied to the collar．The plate is originally at rest．（15\％）


Fig． 4
（5）If a force $\mathrm{F}=200 \mathrm{~N}$ is applied to the $30-\mathrm{kg}$ cart，show that the $20-\mathrm{kg}$ block A will slide on the cart．Also determine the time for block $A$ to move on the cart 1.5 m ．The coefficients of static and kinetic friction between the block and the cart are $\mu_{\mathrm{s}}=0.3$ and $\mu_{\mathrm{k}}=0.25$ ．Both the cart and the block start from rest．（20\％）


Fig 5
（6）A ball having a mass of 8 kg and initial speed of $v_{1}=0.2 \mathrm{~m} / \mathrm{s}$ rolls over a $30-\mathrm{mm}$－long depression．Assuming that the ball rolls off the edges of the contact first $A$ ，then $B$ without slipping，determine its final velocity $v_{2}$ when it reaches the other side． Detail explanation to your equations is required！（20\％）


Fig． 6

