

※ 考生請注意：本試題不可使用計算機。請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

1. (20%)

Consider the two-dimensional flow field defined by the following velocity components:

$$u = \frac{v}{1+t}, \quad v = 1, \quad w = 0$$

For this flow field find the equation of:

- The streamline through the point (1,1) at $t=0$
- The pathline for a particle released at the point (1,1) at $t=0$.

2. (20%)

A curved surface is formed as a circular arc with $R = 0.75\text{m}$ as shown in Fig. 1. The surface width, W , is 1.0m . Water stands to the right of the curved surface to depth $H = 0.65\text{m}$.

- Find the vertical force exerted on the curved surface.
- Find the horizontal force exerted on the curved surface.

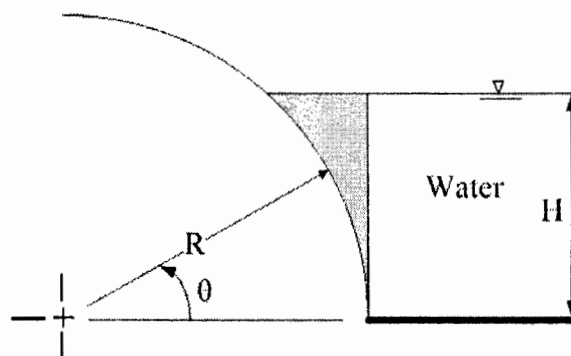


Fig. 1

3. (20%)

At a certain location wind is blowing steadily at 8 m/s . Determine the mechanical energy of air per unit mass and the power generation potential of a wind turbine with 50-m -diameter blades at that location. Also determine the actual electric power generation assuming an overall efficiency of 30 percent. Take the air density to be 1.25 kg/m^3 .

(背面仍有題目,請繼續作答)

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4. (20%)

The velocity potential for a cylinder (Fig. 2) rotating in a uniform stream of fluid is $\Phi = Ur \left(1 + \frac{a^2}{r^2} \right) \cos \theta + \frac{\Gamma}{2\pi} \theta$

where Γ is the circulation. For what value of the circulation will the stagnation point be located at: (a) point A; (b) point B?"

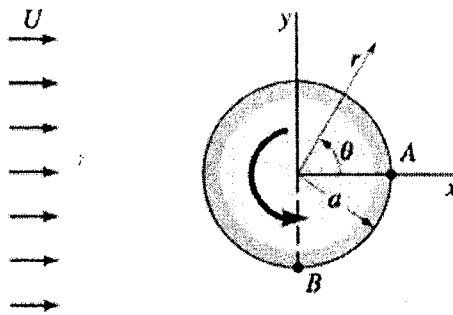


Fig. 2

5. (20%)

Show that the two-dimensional laminar-flow pattern with $dp/dx = 0$,

$$u = U_0 (1 - e^{Cy}) \quad v = v_0 < 0$$

is an exact solution to the boundary-layer equations. Find the value of the constant C in terms of the flow parameters. Are the boundary conditions satisfied? What might this flow represent?

