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※ 考生請注意：本試題不可使用計算機。 請於答案卷（卡）作答，於本試題紙上作答者，不予計分。

1．The solid ball of mass is dropped with a velocity $V_{1}$ the edge of the rough step．If it rebounds horizontally off the step with a velocity $\mathrm{V}_{2}$ ，determine the angle $\theta$ at which contact occurs．Assume no slipping when the ball strikes the step．The coefficient of restitution is $\boldsymbol{e}$ ．（20\％）
2．The system consists of a 10 kg disk $\mathrm{A}, 2 \mathrm{~kg}$ slender rod $B C$ ，and a 0.5 kg smooth collar C ．If the disk rolls without slipping，determine the velocity of the collar at the instant the rod becomes horizontal．ie．，$\theta=0^{\circ}$ ． The system is released from rest when $\theta=45^{\circ} .(15 \%)$
3．The smooth 0.5 kg double－collar in Fig． 3 can freely slide on arm $A B$ and the circular guide rod．If the arm rotates with a constant angular velocity of



Fig． 3



Hint：$\quad I_{G}=\frac{1}{12} m\left(a^{2}+b^{2}\right)$ for thin rectangular plate

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5．Four pins slide in four separate slots cut in a circular plate as shown in Fig．5．
When the plate is at rest，each pin has a velocity directed as shown and of the same velocity relative to the plate when the plate rotates about $O$ with a constant counterclockwise angular velocity $\omega$ ，determine the acceleration of $P_{1}$ and $\mathrm{P}_{3}$（16\％）
6．Sphere $A$ of mass $m$ and radius $r$ rolls without slipping with a velocity $V_{1}$ on a horizontal surface when it hits squarely an identical sphere $B$ that is at rest． Denoting by $\mu_{\mathrm{k}}$ the coefficient of kinetic friction between a ball and the surface， neglecting friction between the spheres，and assuming perfectly elastic impact， determine（a）the linear and angular velocities of each sphere immediately after the impact，（10\％）（b）the velocity of each sphere after it has started rolling uniformly．（10\％）


Fig．E

