

※ 考生請注意：本試題不可使用計算機。請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

1. (20%)

(1) (a) Write down equations that can describe streamlines.

(b) Let the fluid velocity be (u, v, w) . Draw a picture for explaining the relation of the velocity and the streamlines.

(2) If $u = x, v = 1, w = x$, and one of its corresponding streamline passes through the point $(1,0,0)$, find the streamline.

(3)(a) Can a particle path be a streamline ?

In what situation, a particle path is a streamline ?

(b) Explain the physical meaning of Df/Dt , where D/Dt denotes the substantial (or material) derivative and $f(t, x, y, z)$ is the fluid property.

2. (20%)

The thrust developed to propel the jet ski don as shown is a result of water pumped through the vehicle and exiting as a high-speed water jet. For the conditions shown in the Fig.1, what flowrate is needed to produce a 1.3 kN thrust? Assume the inlet and outlet jets of water are free jets.

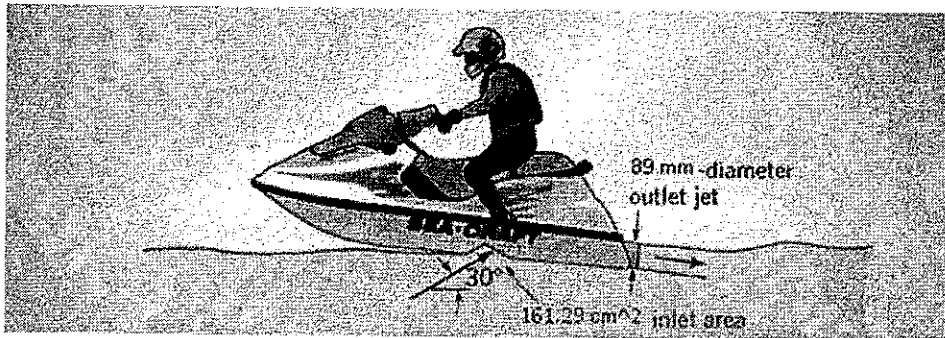


Fig. 1

3. (20%)

It is known that the velocity distribution for two-dimensional flow of a viscous fluid between wide parallel plates as shown is parabolic; that is, $U = U_0 \left[1 - \left(\frac{y}{h} \right)^2 \right]$

With $v = 0$. Determine, if possible, the corresponding stream function and velocity potential.

4. (20%)

The water flowrate, Q , in an open rectangular channel can be measured by placing a plate across the channel as shown in Fig. 2. This type of a device is called a weir. The height of the water, H , above the weir crest is referred to as the head and can be used to determine the flowrate through the channel. Assume that Q is a function of the head, H , the channel width, b , and the acceleration of gravity, g . Determine a suitable set of dimensionless variables for this problem.

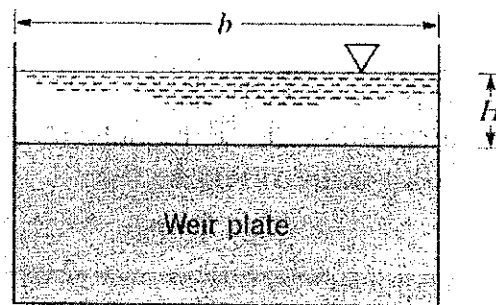


Fig. 2

5. (20%)

A laminar boundary layer velocity profile is approximated by $u/U = 2(y/\delta) - 2(y/\delta)^3 + (y/\delta)^4$ for $y \leq \delta$, and $u = U$ for $y > \delta$. (a) Show that this profile satisfies the appropriate boundary conditions. (b) Use the momentum integral equation to determine the boundary layer thickness, $\delta = \delta(x)$.