

(5) 1. 求  $x^2 + y^2 = c^2$  之正交曲線

(5) 2. 解  $y \frac{dy}{dx} + y^2 = x$

(5) 3. 求  $f(x) = x^2, -\pi \leq x \leq \pi, f(x+2\pi) = f(x)$  之福利華級數展開

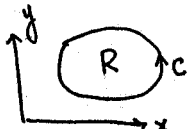
(5) 4. 求  $\delta(t) * f(t)$  其中  $\delta(t)$  表示 Dirac's delta function,  $*$  表示 convolution

(5) 5. 求  $\mathcal{L}^{-1} \left[ \frac{ab}{(s^2+a^2)(s^2+b^2)} \right]$

(5) 6. 求  $\oint_{|z|=1} \frac{dz}{z-2}, \oint_{|z|=1} \frac{dz}{z-1}, \oint_{|z|=1} \frac{dz}{z}$

(10) 7. 解  $\begin{cases} \frac{dx}{dt} + 3x + 4y = 5e^t \\ 5x - \frac{dy}{dt} + 6y = 6e^t \end{cases}$

(10) 8. 解  $(x^2 - t) \frac{d^2y}{dt^2} - t \frac{dy}{dt} + y = 0$

(10) 9. 設  $\nabla^2 \phi = 0$ , 證明  $\iint_R \left[ \left( \frac{\partial \phi}{\partial x} \right)^2 + \left( \frac{\partial \phi}{\partial y} \right)^2 \right] dx dy = \oint_C \phi \frac{\partial \phi}{\partial n} ds$ , 其中 

(10) 10. 求偏微分方程  $y \frac{\partial^2 z}{\partial x^2} + x \frac{\partial^2 z}{\partial y^2} = z - 1$  之通解

Hint:  $\int \frac{dx}{\sqrt{x^2+4}} = \ln(2\sqrt{x^2+4} + 2x)$

(15) 11. 求  $\int_0^{2\pi} \frac{d\theta}{5-4\cos\theta}, \int_0^{2\pi} \frac{\sin^2\theta}{5-4\cos\theta} d\theta, \int_0^{2\pi} \frac{\cos^2\theta}{5-4\cos\theta} d\theta$

(15) 12. 解  $\nabla^2 \phi = 0, 0 < x < a, 0 < y < b$

$\frac{\partial \phi}{\partial x} = 0, x=0$

$\frac{\partial \phi}{\partial x} = 0, x=a$

$\frac{\partial \phi}{\partial y} = \frac{\cos \pi x}{a}, y=0$

$\frac{\partial \phi}{\partial y} = 0, y=b$