

#1) The transfer function of a linear, time-invariant (LTI) system is known in the form:

$$G(s) = \frac{Y(s)}{U(s)} = \frac{K(s+5)(s-1)}{s(s+\alpha)(s+2)^2(s+3)(2s+5)}$$

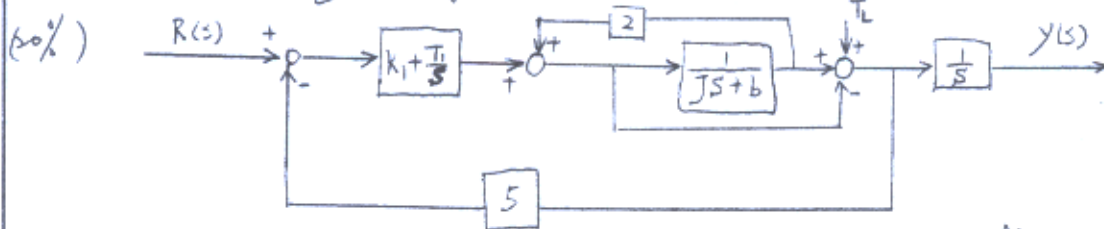
The unit impulse response of the system is of the form:

$$y(t) = \mathcal{L}^{-1}\{Y(s)\} = -\frac{1}{6} + a_1 e^{-t} + a_2 e^{-2t} + a_3 t e^{-2t} + a_4 e^{-2.5t} + a_5 e^{-3t}$$

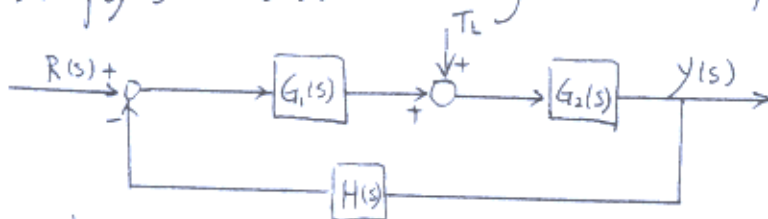
, where  $a_1, a_2, a_3, a_4, a_5$  are constants.

- (i) Determine  $K$  and  $\alpha$ . (10%)
- (ii) Give a pole-zero sketch in the  $s$ -plane. (5%)
- (iii) What is the static gain of the system? (5%)

#2) Block diagram of a servomechanism is shown below:



(i) Simplify the above block diagram to the following:

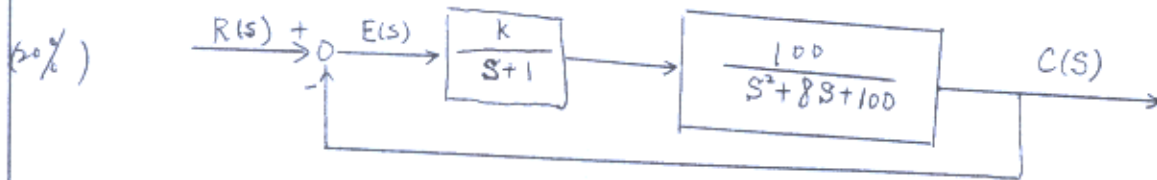


What is  $G_1(s)$ ,  $G_2(s)$  and  $H(s)$ ? (10%)

- (ii) Derive transfer functions between (a)  $R(s)$  and the output  $Y(s)$   
(b)  $T_L$  and the output  $Y(s)$ . (5%)
- (iii) Determine the system characteristic equation and the order of the system. (5%)

(背面仍有題目,請繼續作答)

#3) Shown below is a simple Control Configuration:



It is required to select a suitable value of  $K$  so that the steady state tracking error for a unit step input is less than 0.1. Is it possible to find such a  $K$  value? Justify your answer.

#4) The characteristic equation of a linear control system is

(20%) 
$$s^3 + 2s^2 + 20s + 10K = 0$$

Apply the Routh-Hurwitz criterion to determine the values of  $K$  for system stability.

#5)(i) Draw the Root Loci of the second-order system:

(20%) 
$$s(s+2) + k(s+4) = 0 \quad (10\%)$$

(ii) Find the two breakaway (or breakin) points of the root Loci. (10%)