國立成功大學

113學年度碩士班招生考試試題

編　號：88

系　所：資源工程學系

科　目：統計學

日　期：0201

節　次：第 3 節

備　註：不可使用計算機

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※ 考生請注意：本試題不可使用計算機。　請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

選擇題(每題 4 分)

1. Which of the following is(are) point estimator(s)?
   a. σ
   b. μ
   c. s
   d. α

2. A random sample of 16 statistics examinations was taken. The average score, in the sample, was 76.2 with a variance of 144. The 99% confidence interval for the true average examination score is
   a. 49.677 to 102.723
   b. 73.99 to 78.41
   c. 67.359 to 85.041
   d. 67.437 to 84.963

3. An interval estimate is a range of values used to estimate
   a. the shape of the population's distribution
   b. the sampling distribution
   c. a sample statistic
   d. a population parameter

Exhibit AA

$n = 16$　　$\bar{x} = 75.76$　　$s = 8.246$　　H_0: $\mu \geq 80$

H_a: $\mu < 80$

4. Refer to Exhibit AA. The standardized test statistic equals
   a. -2.12
   b. -0.53
   c. 0.53
   d. 0.483

5. Refer to Exhibit AA. The p-value is equal to
   a. -0.025
   b. 0.05
   c. 0.525
   d. 0.025

6. If a hypothesis is rejected at 95% confidence, it
   a. will always be accepted at 90% confidence
   b. will always be rejected at 90% confidence
   c. will sometimes be rejected at 90% confidence
   d. None of these alternatives is correct.

Exhibit BB

A statistics teacher wants to see if there is any difference in the abilities of students enrolled in statistics today and those enrolled five years ago. A sample of final examination scores from students enrolled today and from students enrolled five years ago was taken. You are given the following results.

	Today	**Five Years Ago**
Mean	82	88
Variance	112.5	54
Sample Size	45	36

7. Refer to Exhibit BB. The point estimate for the difference between the means of the two populations is
   a. 58.5
   b. 9
   c. -9
   d. -6

8. Refer to Exhibit BB. The point estimate for the standard deviation of the difference between the means of the two populations is
   a. 12.9
   b. 9.3
   c. 4
   d. 2

9. A sample of 41 observations yielded a sample standard deviation of 5. If we want to test H_0: $\sigma^2 = 20$, the test statistic is
   a. 100
   b. 10
   c. 51.25
   d. 50

Exhibit CC

The table below gives beverage preferences for random samples of teens and adults.

	Teens	Adults	Total
Coffee	50	200	250
Tea	100	150	250
Soft Drink	200	200	400
Other	50	50	100
	400	600	1,000

We are asked to test for independence between age (i.e., adult and teen) and drink preferences.

10. Refer to Exhibit CC. The calculated value for this test for independence is
    a. 0
    b. 8.4
    c. 62.5
    d. 82.5

11. Refer to Exhibit CC. The result of the test is that the
    a. hypothesis of independence can be rejected
    b. hypothesis of independence cannot be rejected
    c. test is inconclusive
    d. None of these alternatives is correct.

Exhibit DD

SSTR = 6,750 H_0: $\mu_1=\mu_2=\mu_3=\mu_4$
SSE = 8,000 H_a: at least one mean is different
$n_T = 20$

12. Refer to Exhibit DD. The test statistic to test the null hypothesis equals
    a. 0.22
    b. 0.84
    c. 4.22
    d. 4.5

13. Refer to Exhibit DD. The null hypothesis is to be tested at the 5% level of significance. The critical value from the table is
    a. 2.87
    b. 3.24
    c. 4.08
    d. 8.7

Exhibit EE

You are given the following information about y and x.

y Dependent Variable	x Independent Variable
5	15
7	12
9	10
11	7

14. Refer to Exhibit EE. The least squares estimate of b_0 equals
    a. -0.7647
    b. -1.3
    c. 164.1176
    d. 16.41176

15. Refer to Exhibit EE. The coefficient of determination equals
    a. -0.99705
    b. -0.9941
    c. 0.9941
    d. 0.99705

16. If the coefficient of correlation is a positive value, then
    a. the intercept must also be positive
    b. the coefficient of determination can be either negative or positive, depending on the value of the slope
    c. the regression equation could have either a positive or a negative slope
    d. the slope of the line must be positive

17. In multiple regression analysis, the general linear model
    a. can not be used to accommodate curvilinear relationships between dependent variables and independent variables
    b. can be used to accommodate curvilinear relationships between the independent variables and dependent variable
    c. must contain more than 2 independent variables
    d. None of these alternatives is correct.

18. A graph showing the probability of accepting the lot as a function of the percent defective in the lot is
    a. a power curve
    b. a control chart
    c. an operating characteristic curve
    d. None of these alternatives is correct.

19. A control chart that is used when the output of a production process is measured in terms of the percent defective is
    a. a P chart
    b. an X bar chart
    c. a process chart
    d. None of these alternatives is correct.

Exhibit FF

$f(x) = (1/10)\ e^{-x/10}\ \ x \geq 0$

20. Refer to Exhibit FF. The mean of x is
a. 0.10
b. 10
c. 100
d. 1,000

21. Refer to Exhibit FF. The probability that x is between 3 and 6 is
a. 0.4512
b. 0.1920
c. 0.2592
d. 0.6065

22. A population has a mean of 300 and a standard deviation of 18. A sample of 144 observations will be taken. The probability that the sample mean will be between 297 to 303 is
a. 0.4332
b. 0.8664
c. 0.9532
d. 0.0668

Exhibit GG

In a regression analysis involving 25 observations, the following estimated regression equation was developed.

$$\hat{Y} = 10 - 18X_1 + 3X_2 + 14X_3$$

Also, the following standard errors and the sum of squares were obtained.

$S_{b1} = 3\ S_{b2} = 6\ \ S_{b3} = 7$

$SST = 4{,}800\ \ SSE = 1{,}296$

23. Refer to Exhibit GG. If you want to determine whether or not the coefficients of the independent variables are significant, the critical value of t statistic at $\alpha = 0.05$ is
a. 2.080
b. 2.060
c. 2.064
d. 1.96

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24. Refer to Exhibit GG. The coefficient of X_2
   a. is significant
   b. is not significant
   c. can not be tested, because not enough information is provided
   d. None of these alternatives is correct.

25. Refer to Exhibit GG. The multiple coefficient of determination is
   a. 0.27
   b. 0.73
   c. 0.50
   d. 0.33

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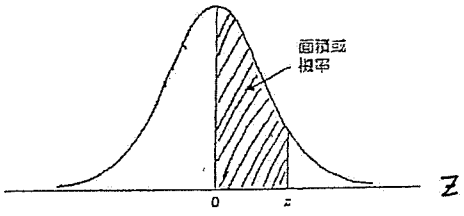
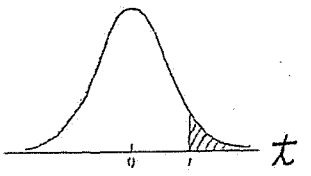
表　標準常態機率分配之面積或機率



z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.0000	0.0040	0.0080	0.0120	0.0160	0.0199	0.0239	0.0279	0.0319	0.0359
0.1	0.0398	0.0438	0.0478	0.0517	0.0557	0.0596	0.0636	0.0675	0.0714	0.0753
0.2	0.0793	0.0832	0.0871	0.0910	0.0948	0.0987	0.1026	0.1064	0.1103	0.1141
0.3	0.1179	0.1217	0.1255	0.1293	0.1331	0.1368	0.1406	0.1443	0.1480	0.1517
0.4	0.1554	0.1591	0.1628	0.1664	0.1700	0.1736	0.1772	0.1808	0.1844	0.1879
0.5	0.1915	0.1950	0.1985	0.2019	0.2054	0.2088	0.2123	0.2157	0.2190	0.2224
0.6	0.2257	0.2291	0.2324	0.2357	0.2389	0.2422	02454	0.2486	0.2518	0.2549
0.7	0.2580	.02612	0.2642	0.2673	0.2704	0.2734	0.2764	0.2794	0.2823	0.2852
0.8	0.2881	0.2910	0.2939	0.2967	0.2995	0.3023	0.3051	0.3078	0.3106	0.3133
0.9	0.3159	0.3186	0.3212	0.3238	0.3264	0.3289	0.3315	0.3340	0.3365	0.3389
1.0	0.3413	0.3438	0.3461	0.3485	0.3508	0.3531	0.3554	0.3577	0.3599	0.3621
1.1	0.3643	0.3665	0.3686	0.3708	0.3729	0.3749	0.3770	0.3790	0.3810	0.3830
1.2	0.3849	0.3869	0.3888	0.3907	0.3925	0.3944	0.3962	0.3980	0.3997	0.4015
1.3	0.4032	0.4049	0.4066	0.4082	0.4099	0.4115	0.4131	0.4147	0.4162	0.4177
1.4	0.4192	0.4207	0.4222	0.4236	0.4251	0.4265	0.4279	0.4292	0.4306	0.4319
1.5	0.4332	0.4345	0.4357	0.4370	0.4382	0.4394	0.4406	0.4418	0.4429	0.4441
1.6	0.4452	0.4463	0.4474	0.4484	0.4495	0.4505	0.4515	0.4525	0.4535	0.4545
1.7	0.4554	0.4564	0.4573	0.4582	0.4591	0.4599	0.4608	0.4616	0.4625	0.4633
1.8	0.4641	0.4649	0.4656	0.4664	0.4671	0.4678	0.4686	0.4693	0.4699	0.4706
1.9	0.4713	0.4719	0.4726	0.4732	0.4738	0.4744	0.4750	0.4756	0.4761	0.4767
2.0	0.4772	0.4778	0.4783	0.4788	0.4793	0.4798	0.4803	0.4808	0.4812	0.4817
2.1	0.4821	0.4826	0.4830	0.4834	0.4838	0.4842	0.4846	0.4850	0.4854	0.4857
2.2	0.4861	0.4864	0.4868	0.4871	0.4875	0.4878	0.4881	0.4884	0.4887	0.4890
2.3	0.4893	0.4896	0.4898	0.4901	0.4904	0.4906	0.4909	0.4911	0.4913	0.4916
2.4	0.4918	0.4920	0.4922	0.4925	0.4927	0.4929	0.4931	0.4932	0.4934	0.4936
2.5	0.4938	0.4940	0.4941	0.4943	0.4945	0.4946	0.4948	0.4949	0.4951	0.4952
2.6	0.4953	0.4955	0.4956	0.4957	0.4959	0.4960	0.4961	0.4962	0.4963	0.4964
2.7	0.4965	0.4966	0.4967	0.4968	0.4969	0.4970	0.4971	0.4972	0.4973	0.4974
2.8	0.4974	0.4975	0.4976	0.4977	0.4977	0.4978	0.4979	0.4979	0.4980	0.4981
2.9	0.4981	0.4982	0.4982	0.4983	0.4984	0.4984	0.4985	0.4985	0.4986	0.4986
3.0	0.4986	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990

表　右尾面積的 t 分配表，例如，右自由度為 10，則 $t_{0.025} = 2.228$



自由度	右尾面積（陰影部分） 0.10	0.05	0.025	0.01	0.005
1	3.078	6.314	12.706	31.821	63.657
2	1.886	2.920	4.303	6.965	9.925
3	1.638	2.353	3.182	4.541	5.841
4	1.533	2.132	2.776	3.747	4.604
5	1.476	2.015	2.571	3.365	4.032
6	1.440	1.943	2.447	3.143	3.707
7	1.415	1.895	2.365	2.998	3.499
8	1.397	1.860	2.306	2.896	3.355
9	1.383	1.833	2.262	2.821	3.250
10	1.372	1.812	2.228	2.764	3.169
11	1.363	1.796	2.201	2.718	3.106
12	1.356	1.782	2.179	2.681	3.055
13	1.350	1.771	2.160	2.650	3.012
14	1.345	1.761	2.145	2.624	2.977
15	1.341	1.753	2.131	2.602	2.947
16	1.337	1.746	2.120	2.583	2.921
17	1.333	1.740	2.110	2.567	2.898
18	1.330	1.734	2.101	2.552	2.878
19	1.328	1.729	2.093	2.539	2.861
20	1.325	1.725	2.086	2.528	2.845
21	1.323	1.721	2.080	2.518	2.831
22	1.321	1.717	2.074	2.508	2.819
23	1.319	1.714	2.069	2.500	2.807
24	1.318	1.711	2.064	2.492	2.797
25	1.316	1.708	2.060	2.485	2.787
26	1.315	1.706	2.056	2.479	2.779
27	1.314	1.703	2.052	2.473	2.771
28	1.313	1.701	2.048	2.467	2.763
29	1.311	1.699	2.045	2.462	2.756
30	1.310	1.697	2.042	2.457	2.750
40	1.303	1.684	2.021	2.423	2.704
60	1.296	1.671	2.000	2.390	2.660
120	1.289	1.658	1.980	2.358	2.617
∞	1.282	1.645	1.960	2.326	2.576

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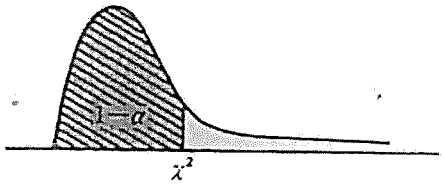
附表 4 χ^2 分配



自由度	機率							
	.005	.010	.025	.050	.950	.975	.990	.995
1	...	...	...	.004	3.84	5.02	6.63	7.88
2	.01	.02	.05	.10	5.99	7.38	9.21	10.60
3	.07	.11	.22	.35	7.81	9.35	11.34	12.84
4	.21	.30	.48	.71	9.49	11.14	13.28	14.86
5	.41	.55	.83	1.15	11.07	12.83	15.09	16.75
6	.68	.87	1.24	1.64	12.59	14.45	16.81	18.55
7	.99	1.24	1.69	2.17	14.07	16.01	18.48	20.28
8	1.34	1.65	2.18	2.73	15.51	17.53	20.09	21.96
9	1.73	2.09	2.70	3.33	16.92	19.02	21.67	23.59
10	2.16	2.56	3.25	3.94	18.31	20.48	23.21	25.19
11	2.60	3.05	3.82	4.57	19.68	21.92	24.72	26.76
12	3.07	3.57	4.40	5.23	21.03	23.34	26.22	28.30
13	3.57	4.11	5.01	5.89	22.36	24.74	27.69	29.82
14	4.07	4.66	5.63	6.57	23.68	26.12	29.14	31.32
15	4.60	5.23	6.26	7.26	25.00	27.49	30.58	32.80
16	5.14	5.81	6.91	7.96	26.30	28.85	32.00	34.27
17	5.70	6.41	7.56	8.67	27.59	30.19	33.41	35.72
18	6.26	7.01	8.23	9.39	28.87	31.53	34.81	37.16
19	6.84	7.63	8.91	10.12	30.14	32.85	36.19	38.58
20	7.43	8.26	9.59	10.85	31.41	34.17	37.57	40.00
21	8.03	8.90	10.28	11.59	32.67	35.48	38.93	41.40
22	8.64	9.54	10.98	12.34	33.92	36.78	40.29	42.80
23	9.26	10.20	11.69	13.09	35.17	38.08	41.64	44.18
24	9.89	10.86	12.40	13.85	36.42	39.36	42.98	45.56
25	10.52	11.52	13.12	14.61	37.65	40.65	44.31	46.93
26	11.16	12.20	13.84	15.38	38.89	41.92	45.64	48.29
27	11.81	12.88	14.57	16.15	40.11	43.19	46.96	49.64
28	12.46	13.56	15.31	16.93	41.34	44.46	48.28	50.99
29	13.12	14.26	16.05	17.71	42.56	45.72	49.59	52.34
30	13.79	14.95	16.79	18.49	43.77	46.98	50.89	53.67
40	20.71	22.16	24.43	26.51	55.76	59.34	63.69	66.77
50	27.99	29.71	32.36	34.76	67.50	71.42	76.15	79.49
60	35.53	37.48	40.48	43.19	79.08	83.30	88.38	91.95
70	43.28	45.44	48.76	51.74	90.53	95.02	100.43	104.22
80	51.17	53.54	57.15	60.39	101.88	106.63	112.33	116.32
90	59.20	61.75	65.65	69.13	113.14	118.14	124.12	128.30
100	67.33	70.06	74.22	77.93	124.34	129.56	135.81	140.17

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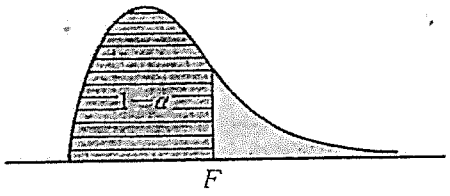
附表 4　F分配



$1-\alpha = 0.95$

ν_2 \ ν_1	1	2	3	4	5	6	7	8	9
1	161.45	199.50	215.71	224.58	230.16	233.99	236.77	238.88	240.54
2	18.513	19.000	19.164	19.247	19.296	19.330	19.353	19.371	19.385
3	10.128	9.5521	9.2766	9.1172	9.0135	8.9406	8.8868	8.8452	8.8123
4	7.7086	6.9443	6.5914	6.3883	6.2560	6.1631	6.0942	6.0410	5.9988
5	6.6079	5.7861	5.4095	5.1922	5.0503	4.9503	4.8759	4.8183	4.7725
6	5.9874	5.1433	4.7571	4.5337	4.3874	4.2839	4.2066	4.1468	4.0990
7	5.5914	4.7374	4.3468	4.1203	3.9715	3.8660	3.7870	3.7257	3.6767
8	5.3177	4.4590	4.0662	3.8378	3.6875	3.5806	3.5005	3.4381	3.3881
9	5.1174	4.2565	3.8626	3.6331	3.4817	3.3738	3.2927	3.2296	3.1789
10	4.9646	4.1028	3.7083	3.4780	3.3258	3.2172	3.1355	3.0717	3.0204
11	4.8443	3.9823	3.5874	3.3567	3.2039	3.0946	3.0123	2.9480	2.8962
12	4.7472	3.8853	3.4903	3.2592	3.1059	2.9961	2.9134	2.8486	2.7964
13	4.6672	3.8056	3.4105	3.1791	3.0254	2.9153	2.8321	2.7669	2.7144
14	4.6001	3.7389	3.3439	3.1122	2.9582	2.8477	2.7642	2.6987	2.6458
15	4.5431	3.6823	3.2874	3.0556	2.9013	2.7905	2.7066	2.6408	2.5876
16	4.4940	3.6337	3.2389	3.0069	2.8524	2.7413	2.6572	2.5911	2.5377
17	4.4513	3.5915	3.1968	2.9647	2.8100	2.6987	2.6143	2.5480	2.4943
18	4.4139	3.5546	3.1599	2.9277	2.7729	2.6613	2.5767	2.5102	2.4563
19	4.3808	3.5219	3.1274	2.8951	2.7401	2.6283	2.5435	2.4768	2.4227
20	4.3513	3.4928	3.0984	2.8661	2.7109	2.5990	2.5140	2.4471	2.3928
21	4.3248	3.4668	3.0725	2.8401	2.6848	2.5757	2.4876	2.4205	2.3661
22	4.3009	3.4434	3.0491	2.8167	2.6613	2.5491	2.4638	2.3965	2.3419
23	4.2793	3.4221	3.0280	2.7955	2.6400	2.5277	2.4422	2.3748	2.3201
24	4.2597	3.4028	3.0088	2.7763	2.6207	2.5082	2.4226	2.3551	2.3002
25	4.2417	3.3852	2.9912	2.7587	2.6030	2.4904	2.4047	2.3371	2.2821
26	4.2252	3.3690	2.9751	2.7426	2.5868	2.4741	2.3883	2.3205	2.2655
27	4.2100	3.3541	2.9604	2.7278	2.5719	2.4591	2.3732	2.3053	2.2501
28	4.1960	3.3404	2.9467	2.7141	2.5581	2.4453	2.3593	2.2913	2.2360
29	4.1830	3.3277	2.9340	2.7014	2.5454	2.4324	2.3463	2.2782	2.2229
30	4.1709	3.3158	2.9223	2.6896	2.5336	2.4205	2.3343	2.2662	2.2107
40	4.0848	3.2317	2.8387	2.6060	2.4495	2.3359	2.2490	2.1802	2.1240
60	4.0012	3.1504	2.7581	2.5252	2.3683	2.2540	2.1665	2.0970	2.0401
120	3.9201	3.0718	2.6802	2.4472	2.2900	2.1750	2.0867	2.0164	1.9588
∞	3.8415	2.9957	2.6049	2.3719	2.2141	2.0986	2.0096	1.9384	1.8799