

礦冶及材料科學研究所

1. Consider a solid cylinder of mass  $M$  and radius  $R$  rolling down an  $10\%$  inclined plane without slipping. See fig. 1. Find the speed of its center of mass when the cylinder reaches the bottom?

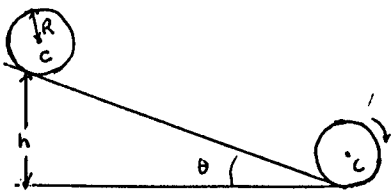


Fig. 1.

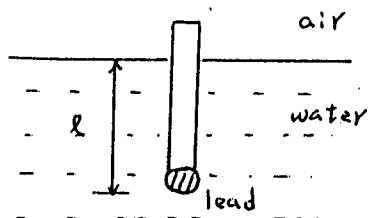


fig. 2.

2. A cylindrical wooden rod is loaded with lead at one end so that it floats upright in water. See fig. 2. The length of the submerged portion is  $l = 2.5$  m. The rod is set into vertical oscillation.

(a.) Show that the oscillation is simple harmonic? (b.) Find the period of the oscillation? Neglect the fact that the water has a damping effect on the motion.

3. A radio station operating at a frequency of  $1500$  kHz has two identical vertical dipole antennas spaced  $400$  m. apart. Where are the intensity maximum and minimum in the resulting radiation pattern?

4. In fig. 3.  $R = 15 \Omega$ ,  $C = 4.7 \mu F$ , and  $L = 25$  mH. The generator provides a sinusoidal voltage of amplitude  $\mathcal{E} = 75$  V (r.m.s) and frequency  $\nu = 550$  Hz. (a.) Calculate the r.m.s current amplitude? (b.) Find the r.m.s voltages  $V_{ab}$ ,  $V_{bc}$ ,  $V_{cd}$ ,  $V_{bd}$ ,  $V_{ad}$ ? (c.) What average power is dissipated by each of the three circuit elements?

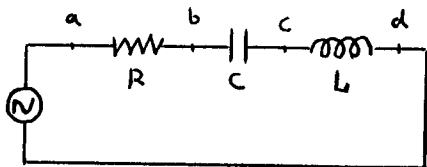


fig. 3.

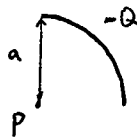


fig. 4.

NO. 118

5. Negative electric charge is distributed uniformly around a quarter

of a circle of radius  $a$ , with total charge  $-Q$ , what are the electric field and electrical potential at point  $P$ . See fig. 4.

6. An ideal diatomic gas ( $\gamma = 1.40$ ) is caused to pass through the cycle shown on the  $p$ - $V$  diagram in fig. 5., where  $V_2 = 3V_1$ . Determine, in terms of  $P_1, V_1, T_1$ , and  $R$ : (a.)  $P_2, P_3$ , and  $T_3$ ? (b.)  $W, Q, \Delta U$ , and  $\Delta S$ , per mole, for all three processes?

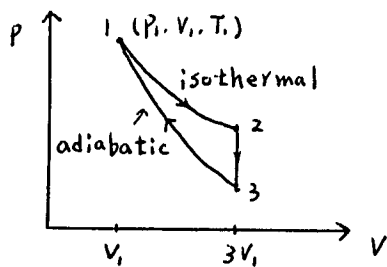


fig. 5.

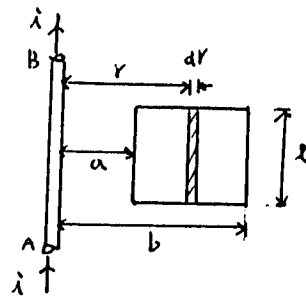


fig. 6.

7. The current in the wire AB of fig. 6. is upward and increasing steadily at a rate  $di/dt$ .
- At an instant when the current is  $i$ , what are the magnitude and direction of the field  $\vec{B}$  at a distance  $r$  from the wire?
  - What is the flux  $d\Phi$  through the narrow shaded strip?
  - What is the total flux through the loop?
  - What is the induced emf in the loop?