

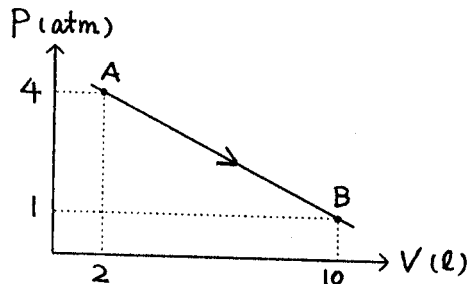
Physical constants which you may need:

gas constant  $R=8.314 \text{ J/mol-K}=0.082 \text{ atm-l/mol-K}$

Boltzmann's constant  $k=1.38 \times 10^{-23} \text{ J/K}$

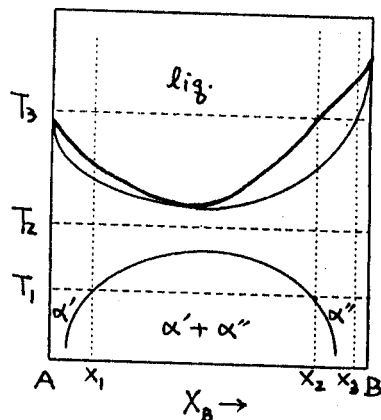
1. (24%) In order to relate the thermodynamic functions  $U$ ,  $H$  and  $S$  to the independent variables  $T$  and  $P$  (temperature and pressure), please derive the following differential forms: (i)  $dU=MdT+NdP$ ; (ii)  $dH=M'dT+N'dP$ ; (iii)  $dS=M''dT+N''dP$ . [Note: you must express  $M$ ,  $N$ ,  $M'$ ,  $N'$ ,  $M''$ ,  $N''$  in terms of thermodynamic parameters  $T$ ,  $P$ ,  $V$ ,  $c_p$ ,  $\alpha$ , and  $\beta$ . (where:  $c_p = \left(\frac{\partial H}{\partial T}\right)_p$ ,  $\alpha = \frac{1}{V}\left(\frac{\partial V}{\partial T}\right)_p$ ,  $\beta = -\frac{1}{V}\left(\frac{\partial V}{\partial P}\right)_T$  )].

2. (20%) For 1 mole of monatomic ideal gas under the process path from state A to state B (shown as right). Please calculate (a)  $\delta w$  (done by the gas); (b)  $\delta q$  (absorbed by the gas); (c)  $\Delta U$ ; (d)  $\Delta S$ ; (e)  $\Delta H$  of the process.



3. (7%) Describe the thermodynamic characterization of first-order phase transition.

4. (15%) For a hypothetical binary phase diagram shown as right, please plot the Gibbs free energy - composition ( $\Delta G^{\text{mix}}-X$ ) diagrams for temperatures  $T_1$ ,  $T_2$  and  $T_3$ .



5. (6%) Point out which of the statement(s) is (or are) wrong and explain the reason why:  
 (a) During a reversible process, the entropy change of a system is zero.

- (b) During an irreversible process, the entropy change of a system is greater than zero.
- (c) There is no such an engine that could fully convert heat from a single reservoir to work.
- (d) Heat could be conducted from a high temperature reservoir to a low temperature reservoir without any loss of heat.
6. (12%) One mole of molten aluminum is adiabatically contained and supercooled to 10 K below its melting point ( $T_m=932\text{K}$ ). Use the following data to find out (i) the amount of the aluminum which spontaneously freezes; (ii) the change of entropy by spontaneous freezing. DATA:  $C_{p(s)} = 26 \text{ J/mol-K}$ ;  $C_{p(l)} = 29 \text{ J/mol-K}$ ; heat of melting ( $\Delta H_m$ ) = 10700 J/mol at  $T_m=932\text{K}$ .
7. (10%) Using the following data, determine the  $P_{\text{H}_2}/P_{\text{H}_2\text{O}}$  ratio to oxidizing silicon in water vapor ambient at 1400K.  
DATA:  $\text{H}_2(\text{g}) + 0.5 \text{ O}_2(\text{g}) \rightarrow \text{H}_2\text{O}(\text{g}) \quad \Delta G^\circ = -246,000 + 54.8 T$   
 $\text{Si}(\text{s}) + \text{O}_2(\text{g}) \rightarrow \text{SiO}_2(\text{s}) \quad \Delta G^\circ = -907,100 + 175 T$
8. (6%) Point out which of the statement(s) is (or are) wrong and explain the reason why:
- (a) For an ideal solution of condensed phases,  $a_i = X_i$  (activity of component  $i$  = mole fraction of component  $i$ ).
- (b) For a nonideal solution of condensed phases,  $a_i = \gamma_i X_i$ . And when  $X_i \rightarrow 1$ ,  $a_i \rightarrow 1$  and  $\gamma_i \rightarrow 1$ .
- (c) For a binary regular solution,  $\ln \gamma_A = \alpha X_B^2$  and  $\Delta H^M = \alpha RT X_A X_B$ . Where  $\alpha$  is independent of temperature and composition.
- (d) The quasi-chemical model for regular solutions is more applicable at low temperatures than at high temperatures.