

國立成功大學  
110學年度碩士班招生考試試題

編 號：169

系 所：電機工程學系

科 目：控制系統

日 期：0202

節 次：第 2 節

備 註：不可使用計算機

※ 考生請注意：本試題不可使用計算機。請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

1. Consider a closed-loop system described in Figure 1, where  $C(s) = K \frac{s+a}{s+b}$ ,  $G(s) = \frac{1}{s^2 + 4\zeta s + 4}$ , and  $0 < \zeta < 1$ .

- (a) What are the constraints placed on  $K$ ,  $a$ , and  $b$  so that the system is both stable and Type 1? (12%)
- (b) What are the constraints on  $a$  and  $b$  so that the system is both Type 1 and remains stable for every positive value for  $K$ ? (12%)

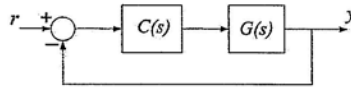


Figure 1

2. Consider the plant described by  $\dot{X} = \begin{bmatrix} 0 & 1 \\ 5 & -4 \end{bmatrix} X + \begin{bmatrix} 1 \\ 2 \end{bmatrix} u$  and  $y = [2 \ 1]X$ .

- (a) Find the transfer function using matrix algebra. (10%)
- (b) Suppose state feedback  $u = [k_1 \ k_2]X$ , determine the constraints on  $k_1$  and  $k_2$  so that the closed-loop system is stable. (8%)
- (c) Suppose output feedback  $u = k_3 y$ , determine the constraints on  $k_3$  so that the closed-loop system is stable. (8%)
3. The unity-feedback system with an open-loop transfer function  $G(s) = \frac{K(s+\alpha)}{(s+\beta)^2}$ , is to be designed to meet the following specifications: steady-state error for a unit step input  $e_{ss} = 0.1$ ; damping ratio  $\zeta = 0.6$ ; natural frequency  $\omega_n = \sqrt{10}$  rad/sec. Find the values of  $K$ ,  $\alpha$ , and  $\beta$ . (25%)

4. The system shown in Figure 2 has  $G_1(s) = \frac{1}{s(s+2)(s+4)}$ . Use the Routh-Hurwitz criterion to find the values of  $K_1$  and  $K_2$  for which the system oscillates at a frequency of 2 rad/sec. (25%)

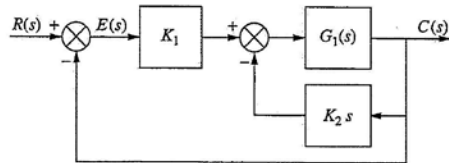


Figure 2