

* Useful constants :

$$\epsilon_0 = 10^{-9}/(36\pi) \text{ (F/m)}; \quad \mu_0 = 4\pi \times 10^{-7} \text{ (H/m)}; \quad \sqrt{\mu_0/\epsilon_0} = 120\pi \text{ (\Omega)}$$

1. Maxwell's Equations and Wave Equations :

- (a) Write Maxwell's equations in a **conductive medium** (μ, ϵ, σ) with the impressed source \vec{J} . (6%)
- (b) Write the expression of the complex permittivity ϵ_c from (a). (3%)
- (c) Indicate which term in (a) is the **displacement current density** and briefly explain the physical meaning of the displacement current. (6%)
- (d) The inhomogeneous wave equations of the E and H fields can be derived from (a) as follows.

$$\left(\nabla^2 - \mu\epsilon_c \frac{\partial^2}{\partial t^2} \right) \begin{Bmatrix} \vec{E} \\ \vec{H} \end{Bmatrix} = \begin{Bmatrix} \nabla\rho/\epsilon + \mu\partial\vec{J}/\partial t \\ -\nabla \times \vec{J} \end{Bmatrix}$$

Derive the time-harmonic wave equation (Helmholtz equation). (6%)

- (e) Write the definition and expression of the intrinsic impedance η_c of a uniform plane wave in the conductive medium. (4%)

- 2. A Hertzian electric dipole antenna of current I and length l is located along the z-axis. The radiation far-zone field can be derived as follows.

$$\vec{E}^r = \hat{\theta} \eta \frac{jkIl}{4\pi r} e^{-jkr} \sin\theta \quad \vec{H}^r = \hat{\phi} \frac{kIl}{4\pi r} e^{-jkr} \sin\theta$$

- (a) Determine the time-average power density. (3%)
- (b) Determine the radiation resistance of the Hertzian electric dipole. (5%)

Note : $\int_0^{2\pi} \int_0^\pi \sin^3\theta d\theta = 4/3$

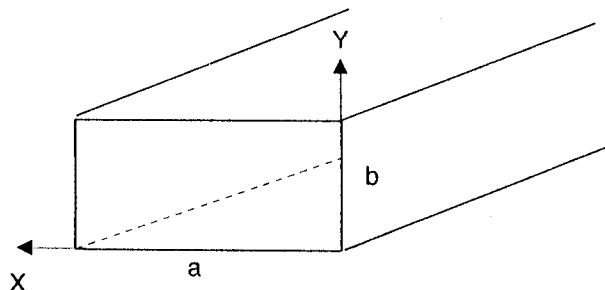
- (c) Show how to arrange two Hertzian electric dipoles to produce a circularly polarized wave (either RHCP or LHCP) in the x direction. Draw a figure of the arrangement and indicate the necessary conditions. (7%)

(若仍有題目,請繼續作答)

3. Waveguide Problem

A 10-GHz signal is coupled to a 1-m-long waveguide that has dimensions of $a = 2$ cm, $b = 1$ cm. The output end of the waveguide is loaded in $200 + j100 \Omega$.

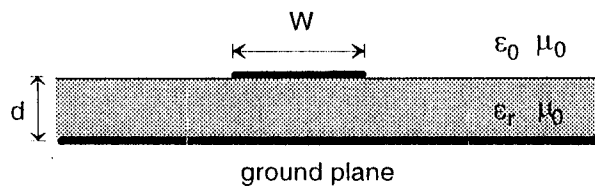
- (a) Determine the wavelength, frequency, and waveguide impedance
 Z_g of the lowest-frequency signal that will propagate down the waveguide.
 (Note: You have to derive the formulas of the above quantities from the following waveguide-mode field formulas first.) (10%)
- (b) The VSWR of the signal in the waveguide (loaded in $200 + j100 \Omega$). (4%)
- (c) Write the expression and plot the cross-sectional E and H field distribution of the dominate mode. (4%)
- (d) Prove that the E field of (c) satisfy the boundary condition. (4%)
- (e) Determine the surface currents on the waveguide wall ($y = 0$) of the dominate mode from the H field of (c). (4%)
- (f) Use Smith chart and results of (a) to determine the impedance seen at the input end of the waveguide. (9%)



Waveguide TM mode fields	Waveguide TE mode fields
$E_z^0(x, y) = E_0 \sin(\frac{m\pi}{a} x) \sin(\frac{n\pi}{b} y)$	$H_z^0(x, y) = H_0 \cos(\frac{m\pi}{a} x) \cos(\frac{n\pi}{b} y)$
$E_x^0(x, y) = -\frac{\gamma}{h^2} (\frac{m\pi}{a}) E_0 \cos(\frac{m\pi}{a} x) \sin(\frac{n\pi}{b} y)$	$E_x^0(x, y) = \frac{j\omega\mu}{h^2} (\frac{n\pi}{b}) H_0 \cos(\frac{m\pi}{a} x) \sin(\frac{n\pi}{b} y)$
$E_y^0(x, y) = -\frac{\gamma}{h^2} (\frac{n\pi}{b}) E_0 \sin(\frac{m\pi}{a} x) \cos(\frac{n\pi}{b} y)$	$E_y^0(x, y) = -\frac{j\omega\mu}{h^2} (\frac{m\pi}{a}) H_0 \sin(\frac{m\pi}{a} x) \cos(\frac{n\pi}{b} y)$
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$\gamma = j\beta = j\sqrt{\omega^2\mu\epsilon - (\frac{m\pi}{a})^2 - (\frac{n\pi}{b})^2} \quad h^2 = (\frac{m\pi}{a})^2 + (\frac{n\pi}{b})^2$	

(背面仍有題目,請繼續作答)

4. A microstrip transmission line is shown in the following figure.
- Explain why the microstrip line can not support a pure TEM wave. (4%)
 - Draw a figure to illustrate an approximated E and H field distribution over the cross section of the microstrip line for quasi-TEM wave approximation. (3%)
 - Write an approximated simple formula of the characteristic impedance (Z_0) and the guided wavelength (λ_g) of a microstrip line. (3%)



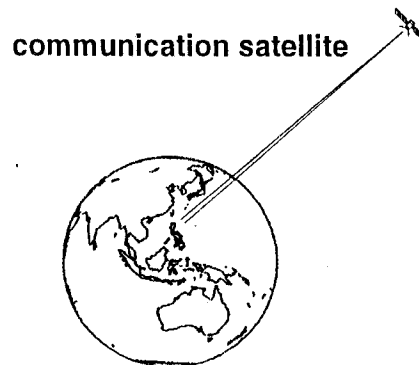
5. A communication satellite is in a synchronous orbit 36,000 km above the earth. The satellite transmitter power is 100 W and the satellite antenna with a gain 30 dB and radiation efficiency 0.6 at 20 GHz. The earth station receiver with an antenna gain 40 dB and radiation efficiency 0.6 receives the satellite transmitted signal.
- Determine the effectively isotropically radiated power (EIRP) of the satellite antenna in terms of dBw. (5%)
 - Determine the time-average power density of the satellite antenna radiated wave at the location of the earth station. (5%)
 - Determine the received power of the earth station antenna (assuming a matched load and no polarization mismatch). (5%)

* **Radio communication link:** Friis power transmission formula

$$\frac{P_L}{P_{rad}} = \frac{G_t \eta_r G_r \eta_r \lambda^2}{(4\pi r)^2}$$

P_{rad} = radiated power from the antenna, P_L = received power to the matched load

η_t (η_r) = transmitting (receiving) antenna radiation efficiency



(背面仍有題目,請繼續作答)

