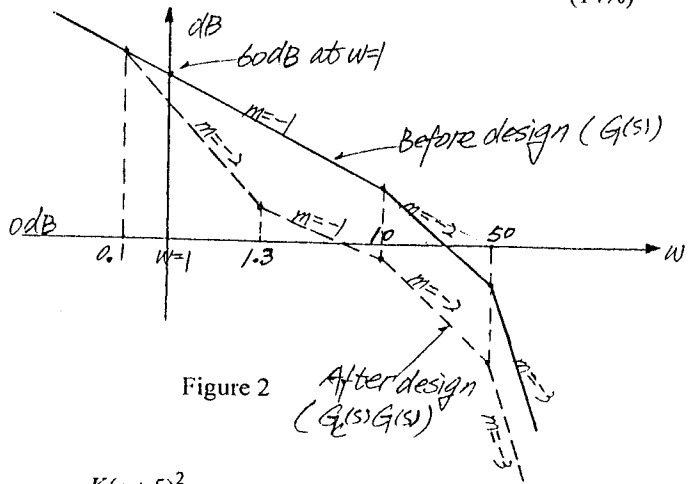
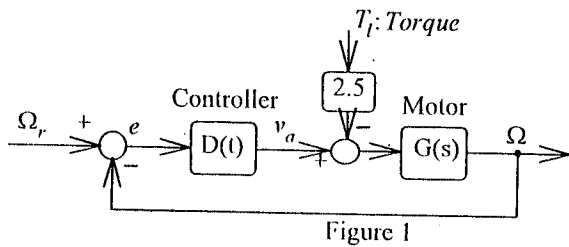
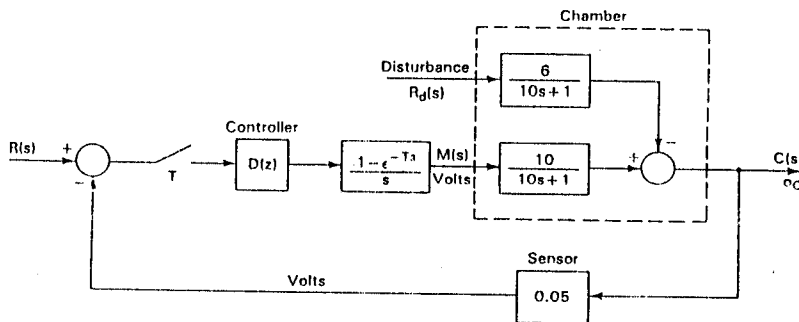


1. A DC motor speed control is shown in Figure 1, where  $G(s) = \frac{K_0}{s+1}$ ,  $D(t) = K[e + \frac{1}{K_I} \int_0^t e dt]$ ,  $\tau = 1/60$ , and  $K_0 = 10$ .
- Please compute the transfer function from torque  $T_i$  to output  $\Omega$ . (5%)
  - Please compute the transfer function from reference input  $\Omega_r$  to output  $\Omega$ . (5%)
  - Please determine  $K$  and  $K_I$  so that the characteristic equation of the closed-loop system will have roots at  $-60 \pm j60$ . (10%)
- (Hint: for parts (a) & (b),  $\frac{v_a(s)}{e(s)} = D(s)$ )



3. A unity feedback system has the open-loop transfer function  $G(s) = \frac{K(s+5)^2}{s^2(s-10)}$ . Please draw the Nyquist plot to determine the range of  $K$  for which the system is stable. (Note: Any other method is NOT accepted.) (13%)
4. (a) Please define the meanings of ( OR explain the physical meanings of ) “linearity”, “relaxed at  $t_0$ ”, “causal”, and “time invariant”. (12%)
- (b) If a linear system has  $p$  input terminals and  $q$  output terminals, and if the system is initially relaxed at  $-\infty$ , then the input-output description can be described as  $y(t) = \int_{-\infty}^t G(t, \tau) u(\tau) d\tau$ , where  $y(t) \in R^q$  is the output vector,  $u(t) \in R^p$  is the input vector, and  $G(t, \tau) \in R^{q \times p}$  is the impulse response matrix. Please give new input-output descriptions for the following systems : (1) a linear relaxed at  $t_0$  system, (2) a linear, causal, and relaxed at  $t_0$  system, (3) a linear time invariant system, and (4) a linear time invariant, causal, and relaxed at  $t_0 = 0$  system. (8%)
5. Consider the temperature control system of Figure 3. Suppose that the digital filter transfer function is given by  $D(z) = 1.2 + \frac{0.1z}{z-1}$  which is a PI controller. Suppose that  $T=2$  s and let  $R_d(s)=0$ .
- Using the closed-loop transfer function, derive a discrete state model for the system. (8%)
  - Derive a discrete state model for the plant from the plant transfer function. Then derive the state model of the closed-loop system by adding the filter and the feedback path to the flow graph of the plant. (6%)
  - Calculate the transfer function from the state model of (b), to verify these results. (6%)



(背面仍有題目,請繼續作答)

6. Consider a unity feedback system with  $G(s) = \frac{K(s+\alpha)}{s(s+3)(s+6)}$ .

(a) Sketch the root locus for  $\alpha=5$ .

(7%)

(b) Find the values of  $\alpha$  and  $K$  that will yield a second-order closed-loop pair of poles at  $-1 \pm j100$ .

(6%)