

1. The *Fibonacci number* can be defined in a recurrence relation: (20%)

$$F(n) = F(n-1) + F(n-2) \text{ for } n \geq 2 \text{ with } F(0) = F(1) = 1.$$
 - a) Write a recursive program for computing $F(n)$, and analyze the complexity of the program.
 - b) Write a non-recursive program for computing $F(n)$ in liner time.
2. Using C++ (or C) code to implement the following functions for the **Doubly Linked Circular Lists with head node**. (20%)
 - a) Write the C++ Class (or C Struct) definition of a Doubly Linked Circular list.
 - b) Write the (member) function *insertright* which inserts a node with information field x to the right of a node pointed to by a pointer p in a double linked circular list.
 - c) Write the (member) function *deletenode* which the node pointed to by a pointer p from a doubly linked circular listed and stores its contents in x .
3. We divide the list to be sorted into two roughly equal parts called the left and the right sublists. The sublists are sorted recursively, and the sorted sublists are merged. (20%)
 - a) Write a **Recursive Merge Sort** algorithm.
 - b) Write the status of the list $L = (25, 6, 80, 1, 58, 10, 59, 16, 49, 18)$ at the end of each phase of the Recursive Merge Sort.
 - c) Is the resulting function a stable function? And what is its computing time (Big O)?
4. **Prim's algorithm and Sollin's algorithm**: (20%)
 - a) Using Prim's algorithm and Sollin's algorithm find the minimum-cost spanning tree of Figure 1.
 - b) Write the Prim's algorithm.
 - c) Write the Sollin's algorithm.
 - d) Discuss the difference of this two algorithms and its time complexity.
5. Explain the following terms: (20%)
 - a) Priority queue.
 - b) Huffman codes.
 - c) Max-Min Heap.
 - d) Hash tables.
 - e) Binary search tree.

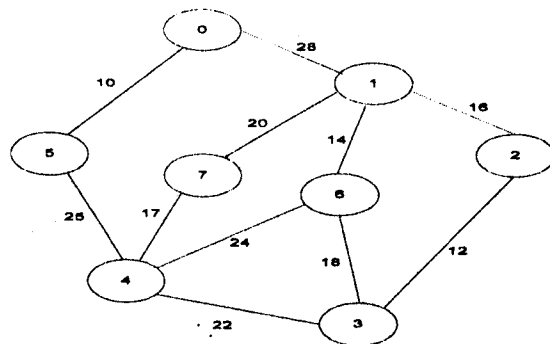


Figure 1.