

1. A low pass signal  $x(t)$  of bandwidth  $W$  is applied to the system shown in Figure 1. The block marked by  $H$  represents Hilbert transform and it is assumed that  $f_0 \gg W$ . Express the signals  $x_i(t)$  and  $X_i(f)$ , the Fourier transform of  $x_i(t)$ , for  $2 \leq i \leq 4$ , respectively. (15%)

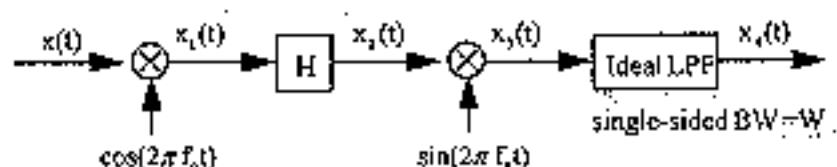


Figure 1

2. A certain communication channel is characterized by 80dB attenuation and additive noise with PSD as shown in Figure 2. The bandwidth of a message signal is 10 kHz and its amplitude is uniformly distributed in the interval  $[-1, 1]$ . If we require that the SNR after demodulation be 20dB, in each of the following cases find the necessary transmitted power. (Assume the carrier frequency is 1MHz.)
- Conventional AM with a modulation index of 0.1; (5%)
  - DSB-SC modulation; (5%)
  - SSB modulation. (5%)

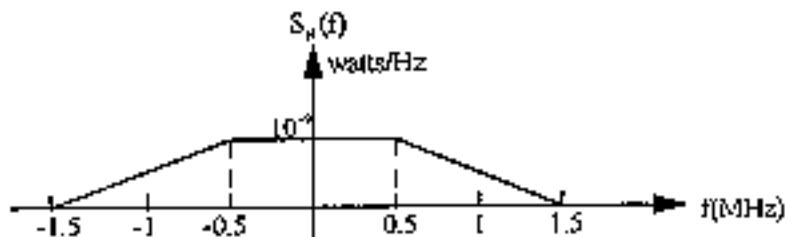


Figure 2

3. An angle-modulated signal has the form  $s(t) = 100\cos[2\pi f_c t + 4\sin 2\pi f_m t]$ , where  $f_c = 100\text{MHz}$  and  $f_m = 3\text{kHz}$ .
- Determine the average transmitted power. (3%)
  - Determine the peak-phase deviation. (5%)
  - Determine the peak-frequency deviation. (5%)
  - If  $s(t)$  is an FM signal, determine the modulation index  $\beta$  and the transmitted signal bandwidth by the Carson's rule. (5%)

4. The output signal-to-noise ratio (SNR) of a uniform quantizer can be expressed as  $\text{SNR}(\text{dB}) = a_0 + a_1 R_b$ , where  $R_b$  is the number of bits used per sample,  $a_0$  and  $a_1$  are constants.
- Calculate  $a_1$ . (5%)
  - Calculate  $a_0$  for a single-tone sinusoidal input signal. (5%)
  - Assume the bandwidth of the input signal is  $W$ . Show that the output data rate  $R_s$  (bits/sec) of the quantizer can be expressed by  $R_s = b_1 W \cdot \log(b_1 \cdot \text{SNR})$ ,  $b_1$  and  $b_2$  are constants. (5%)
5. (a) Plot the transfer function of the Duobinary equivalent correlative filter. Indicate the signaling rate  $R$  in your figure. (5%)
- How can you prevent error propagation in the Duobinary signaling scheme in (a)? (5%)
  - What is the advantage of the Duobinary signaling over the ideal Nyquist pulse? Why? (5%)
  - What is the disadvantage of the Duobinary signaling over the ideal Nyquist pulse? Why? (5%)
6. The bit error rate for a digital modulation scheme in an AWGN channel is expressed as a function of  $E_b/N_0$  (dB), where  $E_b$  is the energy per bit and  $N_0$  is the noise power spectral density. We call this function the performance curve.
- Plot the performance curves of coherent BPSK, coherent QPSK, coherent FSK, noncoherent FSK, DPSK in the same figure. Indicate clearly the relative positions between the above curves. (8%)
  - Explain the reasons that cause the relative positions in (a). (7%)