

* $\epsilon_0 = 10^{-9}/(36\pi)$ (F/m);

$\mu_0 = 4\pi \times 10^{-7}$ (H/m);

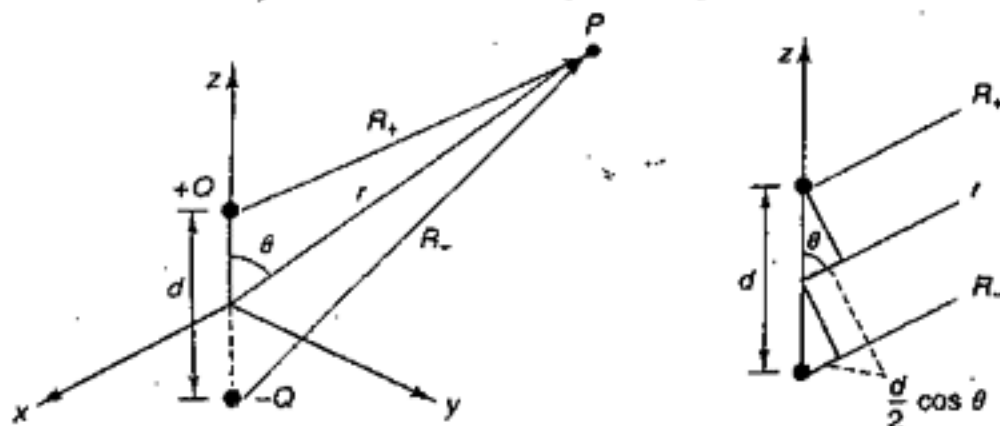
1. Maxwell's Equations (30%)

- (a) Write down the Maxwell's equations in differential form.
- (b) Which term in Maxwell's equations is the *displacement current density*? What is the difference between the displacement current and the free current?
- (c) Write down the equation of continuity.
- (d) Write down the scalar Poisson's equation for the scalar electric potential Φ and the expression of E-field in term of Φ .
- (e) Write down the vector Poisson's equation for the vector magnetic potential \vec{A} and the expression of B-field in term of \vec{A} .

2. The far-zone potential of the electric dipole is (10%)

$$V(\vec{r}) = \frac{Qd \cos \theta}{4\pi\epsilon_0 r^2} \quad r \gg d \text{ (far zone)}$$

- (a) Determine the far-zone E-field.
- (b) Prove the above far-zone potential satisfies Laplace's equation.



del operator $\nabla = \left(\hat{a}_r \frac{\partial}{\partial r} + \hat{a}_\theta \frac{1}{r} \frac{\partial}{\partial \theta} + \hat{a}_\phi \frac{1}{r \sin \theta} \frac{\partial}{\partial \phi} \right)$

Laplacian operator $\nabla^2 V = \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial V}{\partial r} \right) + \frac{1}{r^2 \sin \theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial V}{\partial \theta} \right) + \frac{1}{r^2 \sin^2 \theta} \left(\frac{\partial^2 V}{\partial \phi^2} \right)$

(spherical coordinate)

- 3. A parallel-plate capacitor with a uniform lossy dielectric has a resistance of 1 [KΩ]. The plate surface area is $S = 1 \text{ cm}^2$ and spaced by $d = 0.1 \text{ cm}$. If the dielectric constant is $\epsilon_r = 10$, find the conductivity σ of the dielectric. (Note: $RC = \epsilon/\sigma$) (5%)
- 4. If $\mu_r = 500$ and the density of atoms is $9.02 \times 10^{23} [\text{cm}^{-3}]$ for cobalt, calculate the average magnetization dipole moment per atom when a sample of cobalt is placed in a uniform B-field $B_m = 0.1 [T]$. (5%)

Magnetization $\vec{M} = \chi_m \vec{H}$ for linear, isotropic magnetic materials

$\chi_m =$ magnetic susceptibility

$\vec{B} = \mu_0 (\vec{H} + \vec{M}) = \mu_0 (1 + \chi_m) \vec{H} = \mu_0 \mu_r \vec{H} = \mu \vec{H}$... equation relating B and H

(背面仍有題目,請繼續作答)

(25%) 5. 簡答題

- (1) phonon scattering
- (2) punch through
- (3) two-dimensional electron gas
- (4) molecular beam epitaxy
- (5) metal organic chemical vapor deposition

(15%) 6. 就一 n-p-n bipolar transistor 而言, 試列舉三種可有效提高其電流增益(current gain)的方法, 並說明之.

(10%) 7. 如下圖所示之一度空間無限深量子井(quantum well)

- (1) 試推導並畫出在井內的能階分佈及波函數(wave function).
- (2) 井寬(L_z)縮小與放大時, 能階分佈有何變化? 其物理意義為何?

