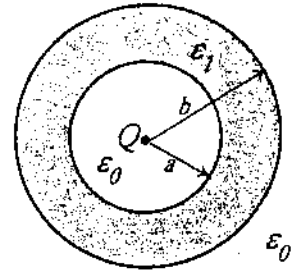


1. (10 Points)

- (a) Write down Maxwell's equations in integral form.  
 (b) Write down the boundary conditions for electric flux density, electric field intensity, magnetic flux density and magnetic field intensity.

2. (15 Points)

A charge  $Q$  is located at the center of a dielectric sphere as shown in the figure. Find and plot the electric flux density, electric field intensity, potential, polarization, and polarization charge density as functions of the distance  $r$  from the origin.



3. (15 Points)

The electrostatic potential function between two parallel very large plates is given by  $V(x) = Ax^{2/3} + Bx + C$  ( $A, B, C$  are constants), where  $x$  is the distance of a point between the plates from one of the plates. The permittivity of the dielectric between the plates is  $\epsilon$ . Determine the electric field distribution and the volume charge density distribution, as functions of  $x$ .

4. (15 Points)

Medium 1 ( $z > 0$ ) has a dielectric constant of 2 and a conductivity of  $4 \times 10^{-5}$  mho/m. Medium 2 ( $z < 0$ ) has a dielectric constant of 5 and a conductivity of  $5 \times 10^{-8}$  mho/m. If  $\mathbf{J}_2$  has a magnitude of 2 A/m<sup>2</sup>, and  $\theta_2 = 60^\circ$  with the normal to the interface, compute  $\mathbf{J}_1$  and  $\theta_1$ . What is the surface charge density at the interface ( $z = 0$ )?

5. (15 Points)

- (a) Find the magnetic field  $H$  at the center of a square loop carrying a current  $I$ . The side of the square loop is  $a/4$  meters long. (b) A circular loop that has radius  $b$  and carries a current  $I$  produces the same magnetic field strength at the center. Find the ratio of  $b$  to  $a$ .

6. (15 Points)

Two infinitely long transmission lines are connected together. One's characteristic impedance is  $200 \Omega$  and the other's is  $50 \Omega$ . If a wave at the  $200 \Omega$  line is propagating toward the junction, what are the reflection and the transmission coefficients? Design a transmission-line transformer to reduce the reflection to zero. What is the VSWR at this matching transmission line section?

7. (15 Points)

Given a characteristic impedance  $50 \Omega$  and a load impedance  $Z_L = 100 - j 50 \Omega$ , match the line to the given load using only transmission line sections. (Hint: you may use the Smith chart below, temporarily. But don't forget to write down important procedures and results on your answer sheet. Otherwise it will not be graded.)

