

※ 考生請注意：本試題不可使用計算機。請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

1. Consider the feedback control system shown in Figure 1. Find the following. (25%)
 - (a) For $K_1 > 0$ and $K_2 > 0$, what are the ranges of K_1 and K_2 that make the system stable.
 - (b) Find the values of K_1 and K_2 to yield a peak time of 1.5 seconds and a settling time of 3.2 seconds for the closed-loop system's step response.

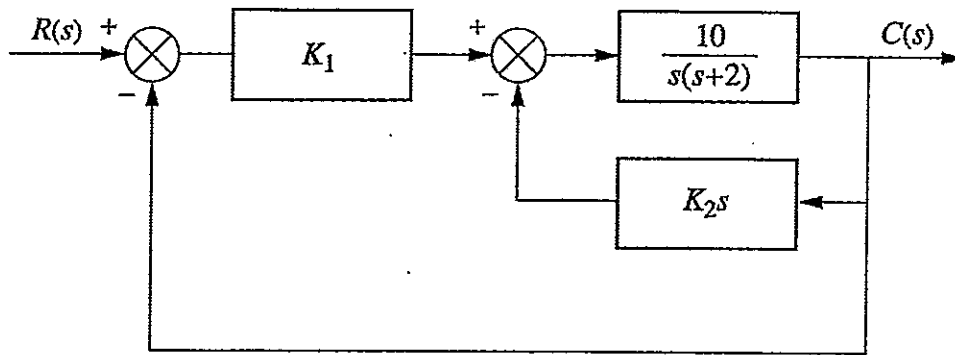


Figure 1. Closed-loop control system for Problem 1.

2. Consider a unit-feedback control system whose transfer function of the plant is

$$G(s) = \frac{2}{s^3 + 4s^2 + 5s + 2}$$

Find the following. (20%)

- (a) The system type and steady-state error with unit-step input.
- (b) For the system, which of the following controllers, P-controller (K_P), PD-controller (K_P and K_D), and PI-controller (K_P and K_I), can be utilized to eliminate the steady-state error in part (a)? What is the steady-state error unit-step input?
- (c) For your choice of controller in part (b), what are the range of the control gains that make the system stable?

3. Consider a closed-loop system where

$$G(s) = \frac{K(s^2 + 1)}{(s-1)(s+2)(s+3)}$$

Find the following. (30%)

- Plot the root locus of the system.
- Use Routh-Hurwitz to find the range of K that makes the system stable.
- Find the frequency of oscillation when the system is marginally stable.
- For unit-step input with $K=1$, find the steady-state error of the system.
- If the steady-state error in part (d) is not zero, can you design a compensator with type 1 to reduce steady-state error with unit-step input. Explain your result by plotting the root locus.

4. Consider a unit-feedback control system whose forward transfer function is

$$G(s) = \frac{K}{s(s+3)(s+4)(s+8)}$$

Find the following. (25%)

- Sketch the Nyquist diagram of the system.
- Gain and phase margins of the system