

1. Determine the overall transfer function for the system shown below. (20%)

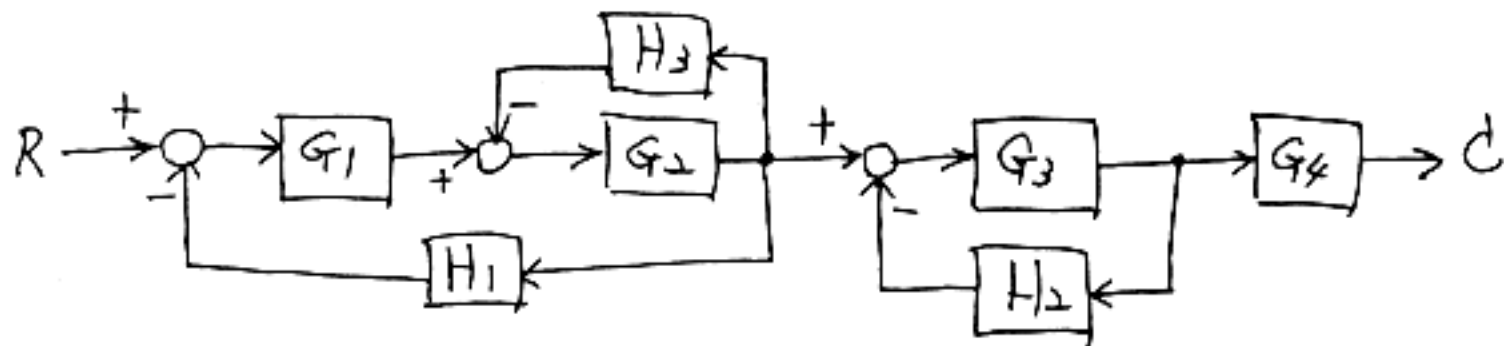


Figure 1.

2. Given the transfer function

$$G(s) = \frac{C(s)}{R(s)} = \frac{2}{s^3 + 6s^2 + 11s + 6} = \frac{2}{(s+1)(s+2)(s+3)}$$

Obtain two differential state representations (state models). (20%)

3. The steady-state error to a unit-ramp input of the system shown in Fig. 3(A) is

$$e_{ss} = \frac{2f}{\omega_n}$$

Show that the steady-state error for following a ramp input may be eliminated, if we introduce the input through a $(1+ks)$ element and choose the proper value for k (See Fig. 3(B)). (20%)

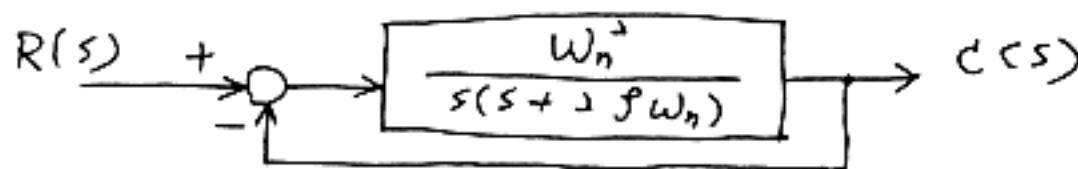


Figure 3(A)

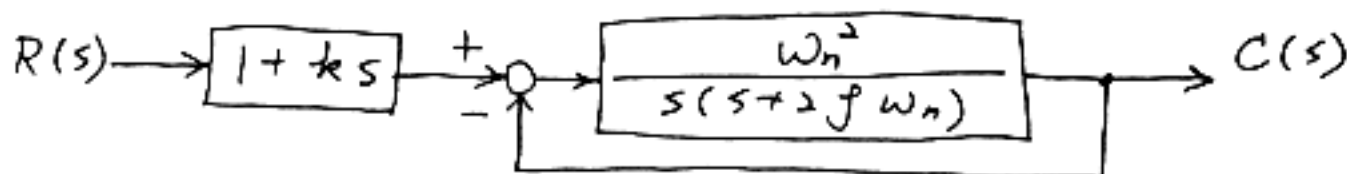


Figure 3(B)

(背面仍有題目,請繼續作答)

4. Figure 4 shows the system with an unstable feedforward (open-loop) transfer function.

- 1) Sketch the root-locus plot and locate the closed-loop poles (13%)
- 2) Show that the unit-step response curve will exhibit overshoot. (7%)

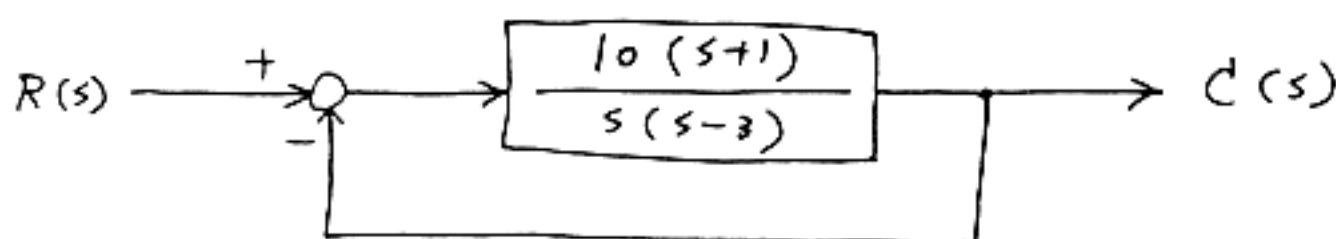


Figure 4

5. Obtain the time response of the system given by

$$\dot{x}(t) = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} x(t) + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(t)$$

where $u(t)$ is the unit step function occurring at $t=0$, and the initial conditions are $x_1(0)$ and $x_2(0)$. (20%)