

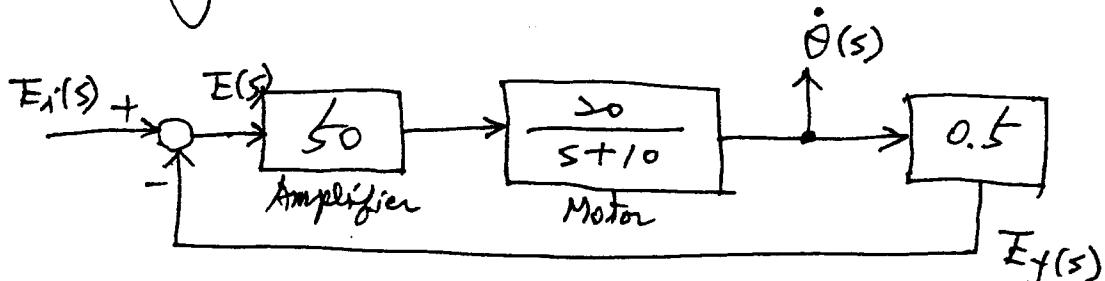
1. Given the Laplace transform $X(s)$ where

$$[20\%] \quad X(s) = \frac{3s^3 + 17s^2 + 33s + 15}{s^3 + 6s^2 + 11s + 6}$$

Find $x(t)$.

2. A block diagram of a velocity servomechanism

[20%] is shown below. For the input voltage 5V, determine the steady-state error in the velocity $\dot{\theta}$.



3. Sketch the root locus for a type 2 system

[20%] with a forward transfer function

$$G_1(s) = \frac{k}{s^2(s + \frac{1}{T_1})}.$$

Discuss the stability of the system.

Suppose a zero was added at $s = -\frac{1}{T_2}$ between the origin and the pole at $-\frac{1}{T_1}$ into $G_1(s)$,

$$\text{or } G_2(s) = \frac{k(s + \frac{1}{T_2})}{s^2(s + \frac{1}{T_1})} \text{ with } \frac{1}{T_1} > \frac{1}{T_2} > 0,$$

Sketch the new root locus with $G_2(s)$ and determine the stability of the system.

4. The system is described by

$$[20\%] \quad \ddot{y} + 6\dot{y} + 11y + 6u = 0$$

Obtain a state equation for the system
in diagonal form.

5. (a) The matrices A and B are

$$[10\%] \quad A = \begin{bmatrix} 0 & 1 & -1 \\ 1 & 0 & 1 \\ 0 & 1 & -1 \end{bmatrix}, \quad B = \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ 0 & 0 \end{bmatrix}$$

Determine if $[A, B]$ is a
controllable pair.

(b) Examine the controllability of the system

$$[10\%] \quad \frac{X(s)}{V(s)} = \frac{k(s+a)(s+b)}{(s+a)(s+b)(s+c)(s+d)}.$$