

※考生請注意：本試題不可使用計算機。請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

1. (25%)

There are six different pole/zero patterns (1)~(6) and six different step responses (A)~(F) as shown in Fig. 1. Please match each pole/zero pattern with the correct step response and give the reason for justifying your answer.

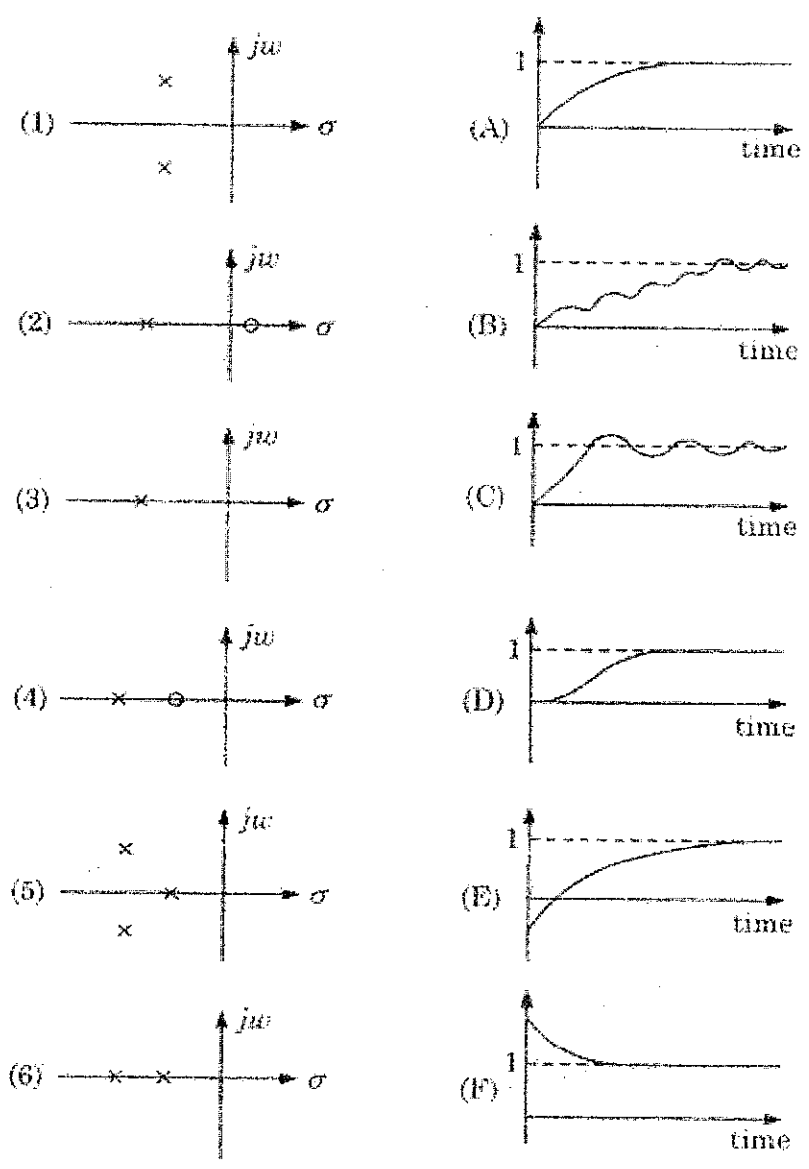


Figure 1

2. (25%)

A feedback control system has the structure shown in Fig. 2.

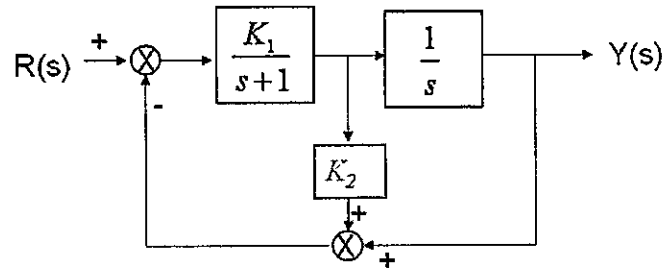


Figure 2

- (1) (10%) Determine the closed-loop transfer function $Y(s)/R(s)$
- (2) (8%) Determine the gains K_1 and K_2 so that the closed-loop response to a unit-step input is critically damped with two equal roots at $s = -10$.
- (3) (7%) Based on the answer of (2), please derive the unit-step response $y(t)$.

Useful Laplace formulas:

$$\mathcal{L}[t] = \frac{1}{s^2}$$

$$\mathcal{L}[e^{-at}] = \frac{1}{s+a}$$

$$\mathcal{L}[te^{-at}] = \frac{1}{(s+a)^2}$$

$$\mathcal{L}[\sin \omega t] = \frac{\omega}{s^2 + \omega^2}$$

$$\mathcal{L}[\cos \omega t] = \frac{s}{s^2 + \omega^2}$$

$$\mathcal{L}[e^{-at} f(t)] = F(s+a)$$

$$\mathcal{L}[tf(t)] = -\frac{d}{ds} F(s)$$

$$\mathcal{L}\left[\frac{df(t)}{dt}\right] = sF(s)$$

$$\mathcal{L}\left[\int_0^t f(\tau) d\tau\right] = \frac{F(s)}{s}$$

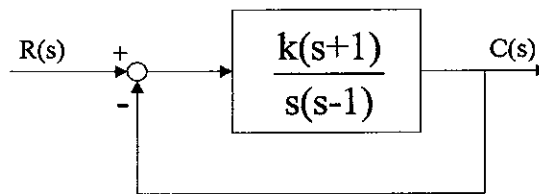
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3. (20%) A pure inertia system, $1/(ms^2)$, is under linear unity feedback control. The controller is of PID type,

$$G_c(s) = K_c (1 + 1/(T_i s) + T_d s)$$

- i) An engineer from the Alpha Inc. has tuned the controller so that the closed-loop poles are all at -2 when $m=5$. What are the values of K_c , T_i and T_d that he selected? (5%)
- ii) The inertia m may be subject to change. For the values of K_c , T_i and T_d that you obtained in i), the closed-loop system cannot remain stable for all $m > 0$. Find the condition(s) for stability. Find all the closed-loop poles at the stability boundary also. (10%)
- iii) Draw the root locus plot for m changing from 0 to ∞ when the values of K_c , T_i and T_d are fixed to what you obtained in i). (5%)

4. (10%) Consider the closed-loop system shown below. Determine the range of k for stability by use of the Nyquist stability criterion.



5. (20%) Consider the closed-loop system shown below.

- i) If $G(s) = k$ ($k \geq 0$), sketch the root locus as k varies from 0 to ∞ . (5%)
- ii) You are requested to design a new controller, $G(s)$, for the system using root-locus method such that the dominant poles of the system are located in the region shown in the s -plane. (15%)

