

# 國立成功大學

## 114學年度碩士班招生考試試題

編 號： 53

系 所： 機械工程學系

科 目： 材料力學

日 期： 0210

節 次： 第 1 節

注 意： 1. 可使用計算機  
2. 請於答案卷(卡)作答，於  
試題上作答，不予計分。

**Problem 1 (20 Pts)**

The steel beam is subjected to a load of 12 kN, as shown in Fig. 1. Determine the principle stress and axis at point A due to the loading.

**Problem 2 (15 Pts)**

The shaft has a radius of 20 mm and is made of A314 steel ( $G_{A314}$ : 80 GPa) in Fig. 2. Determine the strains in the  $x'$  and  $y'$  direction if a torque  $T = 4 \text{ kN}\cdot\text{m}$  is applied to the shaft.

**Problem 3 (15 Pts)**

Initially, gaps between the A-36 steel plate and the rigid constraint are shown in Fig. 3. Determine the normal stresses  $\sigma_x$  and  $\sigma_y$  in the plate if the temperature increases by  $\Delta T = 80^\circ\text{F}$ . ( $\alpha_{A-36}$ :  $5.6(10^{-6})(1/^\circ\text{F})$ ,  $E_{A-36}$ :  $30(10^3)\text{ksi}$ ,  $\nu_{A-36}$ : 0.3)

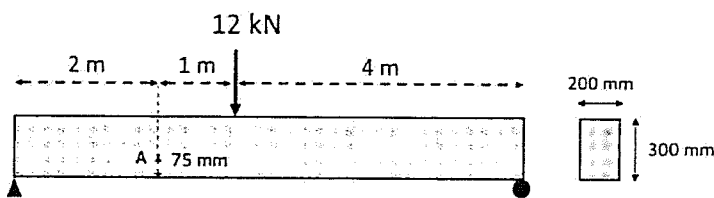


Fig. 1

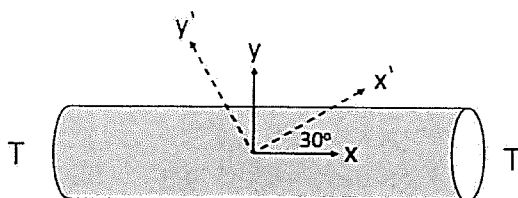


Fig. 2

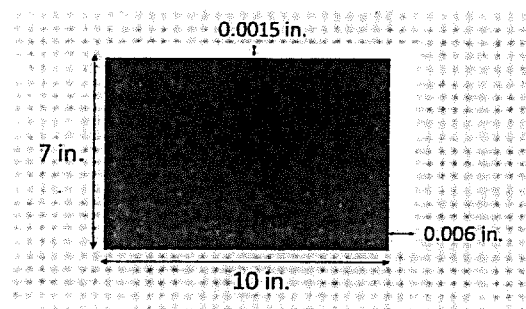


Fig. 3

**Problem 4 (10 Pts)**

The beam with the cross-section as shown in Fig. 4 is made of elastic perfectly plastic material. Determine the plastic moment that can be applied,  $a = 50 \text{ mm}$ ,  $E = 200 \text{ GPa}$ , and  $\sigma_Y = 230 \text{ MPa}$ .

**Problem 5 (20 Pts)**

The column with constant  $EI$  has the end constraints as shown in Fig. 5. (a) Determine the transverse deflection  $v(x)$ . (b) By observing the solution of  $v(x)$ , determine if buckling would occur and the smallest critical values of  $P$  and  $M$  when it happens.

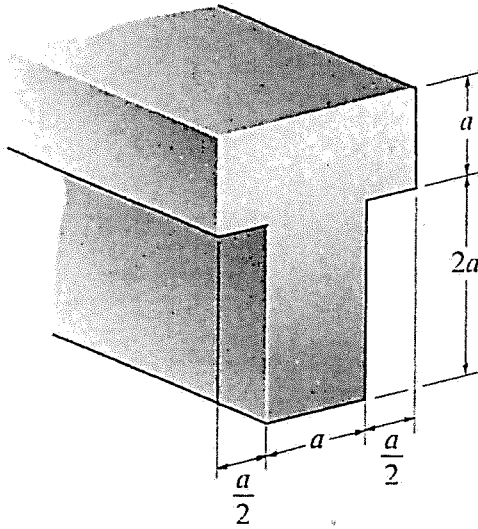


Fig. 4

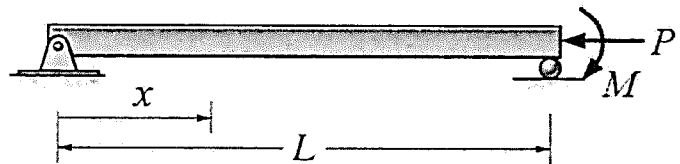


Fig. 5

**Problem 6 (20 Pts)**

A semicircular metal wire as shown in Fig. 6 is built-in to the wall at point A, simply-supported on the bottom at point B, and subjected to load  $P$  at mid-span-point C. The wire has a circular cross-section of radius  $r$ ,  $r \ll R$ . Young's modulus and Poisson's ratio of the wire are  $E$  and  $\nu$ , respectively. The cross-sectional area moment of inertia about the bending neutral axis is  $\pi r^4/4$ . Determine the deflection  $\delta_C$  at point C and the support reaction at point B by using Castigliano's theorem (alternative solution approach is not allowed).

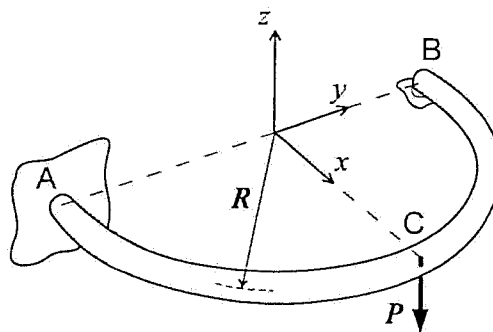


Fig. 6