

編號: F 106 系所: 機械工程學系丙組

科目: 動力學

1. Explain the following items, either in Chinese or in English.

- (a) D'Alembert principle. [7%]  
 (b) Euler equations of motion. [8%]

2. Each of the three plates has a mass of 10 kg. If the coefficients of static and kinetic friction at each surface of contact are  $\mu_s = 0.3$  and  $\mu_k = 0.2$ , respectively. When the three horizontal forces are applied,

- (a) show that plate B will not slip. [5%]  
 (b) determine the acceleration of plate C. [10%]

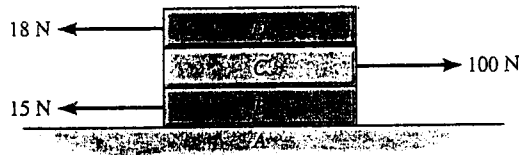


Fig. A2

3. The 40-kg flywheel (disk) is mounted 20mm off its true center at G. If the shaft is rotating at a constant speed  $\omega = 8 \text{ rad/s}$ , determine

- (a) the maximum reactions exerted on the journal bearing at A and B. [10%]  
 (b) the minimum reactions exerted on the journal bearing at A and B. [10%]

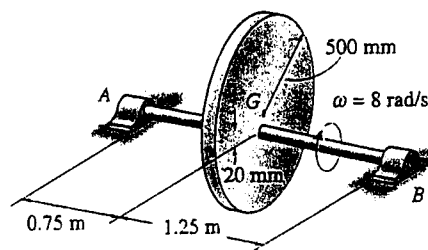


Fig. A3

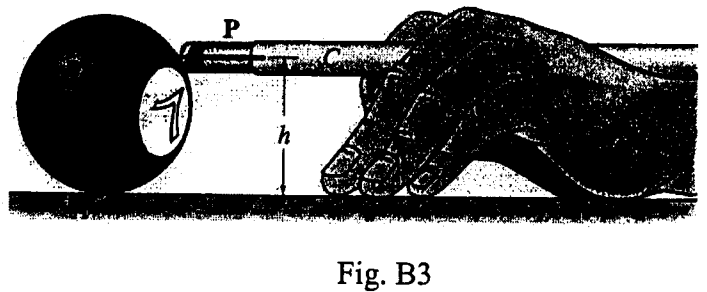
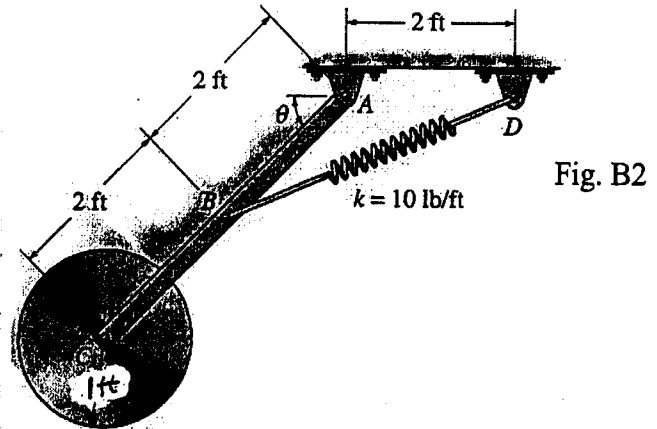
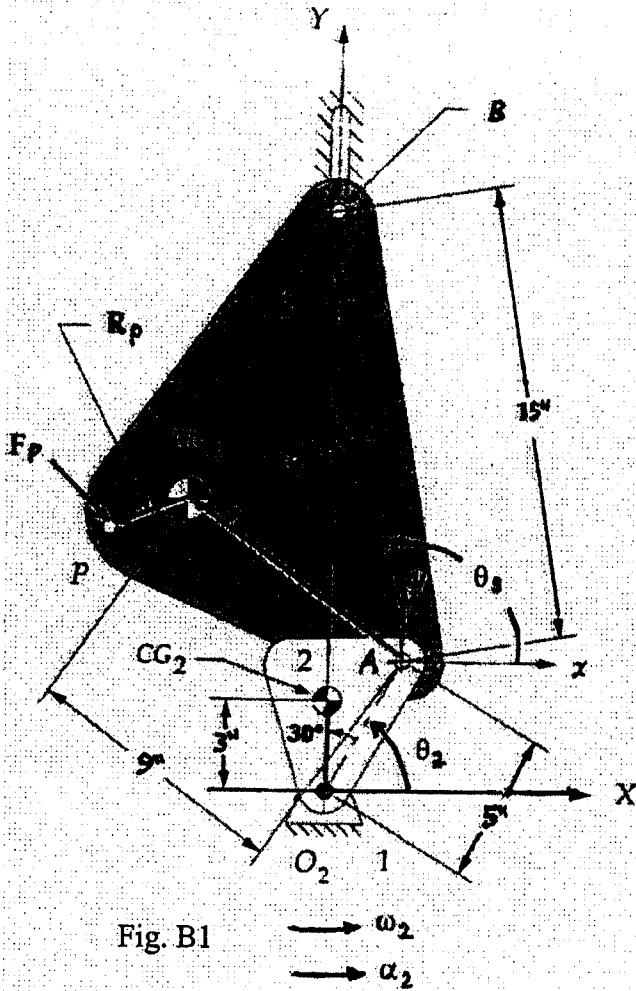
(背面仍有題目, 請繼續作答)

4. Please give answers for the following problems, either in Chinese or in English. But a higher score will be given for correct answers in English.

(a) Under what condition(s), the acting forces between two moving rigid bodies with point-contact will pass their centers of curvature of the contact points. [4 %]

(b) Under what condition(s), the mechanical efficiency of a mechanical system with some mechanical elements in motion is equal to one. [8 %]

5. For the planar three-bar linkage as shown in Fig. B1,  $CG_3$  is the mass center of link 3,  $F_p$  is the external force acting on link 3; between links 1 and 3 there is a pin-in-slot joint. If the gravity forces and inertial forces should be considered but frictions are to be neglected, please define the symbols needed, and (a) give the free-body diagram of link 3, (b) give the equilibrium equations of link 3. [13 %]



6. As shown in Fig. B2, the assembly consists of a 5 lb slender rod  $AC$  to which is pin-connected a 12 lb disk and spring  $BD$ . If the rod is brought into the horizontal position  $\theta = 0^\circ$ , and the disk is given a counterclockwise rotation of 3 rad/sec when the rod is released from rest, please determine the angular velocity of the rod at the instant  $\theta = 90^\circ$ . The spring has an unstretched length of 1 ft. [13 %]

7. Please determine the height  $h$  at which a billiard ball of mass  $m$  and radius  $r$  must be struck so that no friction force develops between it and the table at  $A$ , as shown in Fig. B3. Assume that the cue  $C$  only exerts a horizontal force  $P$  on the ball. [12 %]