

系所組別 環境工程學系乙組

考試科目 流體力學

考試日期：0307，節次：2

※ 考生請注意：本試題 可 不可 使用計算機

1. A flow rate of  $69 \text{ m}^3/\text{s}$  water exists at a depth of 3 m in a rectangular channel 5 m wide. Find the critical depth, specific energy, Froude number, conjugate depth and draw the F+M curve by the unit width. (20%)
2. (1). A velocity potential in two-dimensional flow is  $\phi = 5x + 5y + 6x^2 - 7y^2$ , Find the stream function for this flow. (10%)  
(2). The two-dimensional stream function for a flow is  $\psi = 11 + 13x - 7y + 8xy$ . Find the velocity potential. (10%)
3. A flow in a pipe is related to the parameters of head loss per unit length  $h_f/L$ , average velocity  $V$ , pipe inner diameter  $D$ , gravity  $g$ , viscosity  $\mu$ , mass density  $\rho$ , roughness size  $\epsilon$ , roughness gap  $\epsilon'$ , and shape factor  $m$ . Please derive the Darcy-Weisbach Equation by using the Dimensional Analysis. (20%)
4. The vertical reducing section shown in Fig.4 contains oil, sp gr 0.86, flowing upward at the rate of  $2 \text{ m}^3/\text{s}$ . the pressure at the larger section is 230 kPa. Neglecting losses but including gravity, determine the force on the contraction. (20%)

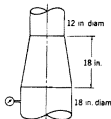


Fig. 4

5. (1). The cube of Fig. 5 is filled with liquid, sp gr 2.4. When it is accelerated to the right  $3 \text{ m/s}^2$ , draw the imaginary free surface and determine the pressure at A. (10%)  
(2). Locate the vertical axis of rotation and the speed of rotation of the U tube of Fig. 5 so that the pressure of liquid at the mispoint of the U tube and at A are both zero. (10%)

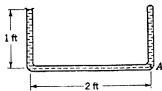


Fig. 5