

系所組別： 生物醫學工程學系乙組

考試科目： 電磁學

考試日期：0219，節次：2

※ 考生請注意：本試題 可 不可 使用計算機

1. A charge  $Q$  is distributed uniformly over an  $L \times L$  square plate. Determine the electric potential  $V$  and the electric field  $\mathbf{E}$  at a point on the axis perpendicular to the plate and through its center. (20%)
2. In a vacuum-tube diode, electrons are emitted from a hot cathode at zero potential and collected by an anode maintained a potential  $V_0$ , resulting in a convection current flow. Assuming that the cathode and the anode are parallel conducting plates and that the electrons leave the cathode with a zero initial velocity, find the relation between the current density  $J$  and  $V_0$ . Define your symbols and coordinate system with clear descriptions and figure. (20%)
3. A ground connection is made by burying a hemispherical conductor of radius 25 mm in the earth with its base up, as shown in Fig. 1. Assuming the earth conductivity is about  $10^{-6}$  S/m, find the resistance of the conductor to far-away points in the ground. (20%)
4. A current  $I$  flows in a long solenoid with  $n$  closely wound coil-turns per unit length. The iron core has a cross-sectional area  $S$ , and permeability  $\mu$ . Determine the force acting on the core if it is withdrawn to the position shown in Fig. 2. (15%)
5. A light ray is incident from air obliquely on a transparent sheet of thickness  $d$  with an index of refraction  $n$ , as shown in Fig. 3. The angle of incident is  $\theta_i$ . Find (a)  $\theta_t$ , (b) the distance  $l_1$  at the point of exit, and (c) the amount of the lateral displacement  $l_2$  of the emerging ray. (15%)
6. A hollow circular cylindrical cavity resonator is to be constructed of copper such that this length  $d$  equals its diameter  $2a$ . (a) Determine  $a$  and  $d$  for a resonant frequency of 10 GHz at the  $TM_{010}$  mode. (b) Find the quality factor  $Q$  of the cavity at resonance. (10%) (The conductivity of copper is  $5.8 \times 10^7$  S/m. For free space, the intrinsic impedance is  $377 \Omega$ , the permittivity is  $1/36\pi \times 10^{-9}$  F/m, and the permeability is  $4\pi \times 10^{-7}$  H/m.)

(背面仍有題目,請繼續作答)

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earth

Fig. 1

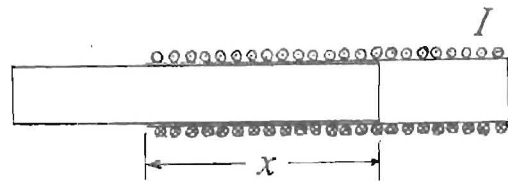


Fig 2

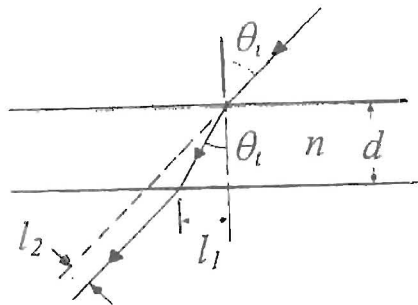


Fig. 3