

1. (30%) Consider the linear time-invariant system

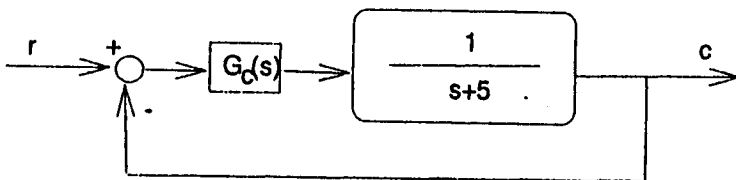
$$\begin{aligned}\dot{x} &= Ax + Bu \\ y &= Cx\end{aligned}$$

Identify the correct or incorrect statements. If the statements are incorrect, then explain why. (此大題為是非題，如果敘述不正確必須說明理由) (3 points each)

- We can check the system's stability from the information of matrix A only.
- If the system is controllable, then the system must be stable.
- If the system is uncontrollable, then we can not stabilize the system through state feedback for any unstable system.
- If the system is stable, then the system must be controllable or observable.
- The controllability of the system will not change through state feedback.
- The observability of the system will not change through state feedback.
- If the order of the system's transfer function is reduced, then the system must be uncontrollable.
- For any controllable system, we can find certain input u to get any desired output y.
- For any dynamic system, through some transformation $\bar{x} = Tx$. We can diagonalize the $\bar{A} = TxT^{-1}$ matrix.
- If the system is controllable and observable, the the system must be stable.

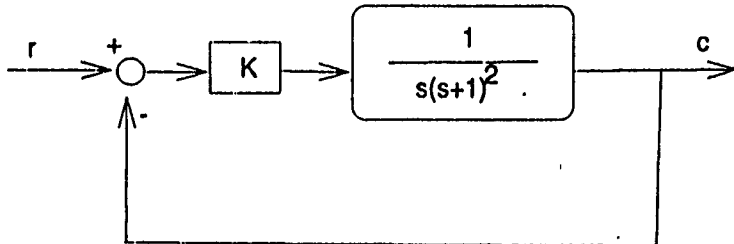
2. (20%) You are a graduate student of Biomedical Engineering at National Cheng-Kung University. You have a term project to design a PC controlled motor driving wheel chair (由個人電腦控制馬達驅動之電動輪椅). Please write down your design procedure, such as components selection, block diagram..... etc. (20 points)

3. (20%) Given the feedback control system:



- Assume the compensator is proportional $G_c(s) = K$. Determine K so that the closed loop bandwidth is $\omega = 10$ radians/second. What is the steady state error to a unit step input? (6 points)
- Assume the compensator is proportional plus integral, $G_c(s) = K_1 + \frac{K_2}{s}$. Select K_1 and K_2 so that $\omega_n = 10$ radians/second and the damping ratio $\zeta = 0.5$. (6 points)
- Suppose $K_2 = 1$. Using root locus, discuss if it is possible to select a value of K_1 to obtain an underdamped response for this system. (8 points)

4. (30%) Consider the control system



- Find the range of the gain K for stability of the closed-loop control system. (6 points)
- If $K=2$, what is the frequency (rad/sec) of oscillation for transients? (6 points)
- If $K=1$, find the steady-state error (i.e. input minus output) when the input r is a unit step function. Does this unit step response exhibit an overshoot of the steady-state output? (6 points)
- If $K=1$, find the steady-state error for a unit ramp input. (6 points)
- If $K=1$ and $r(t) = 4 \cos 3t$, what is the steady-state response $c_{ss}(t)$? (6 points)