

(每題 20%, 共 100 分)

1. A round bar ACB of total length $2L$ rotates about an axis through the midpoint C with constant angular speed ω (radians per second). The material of the bar has specific weight γ . Derive a formula for the tensile stress σ_x in the bar as a function of the distance x from point C . What is the maximum tensile stress? Bar ACB is shown in Fig. 1.
2. The truss ABC shown in Fig. 2 is constructed of a horizontal steel bar BC having cross-sectional area 2580 mm^2 and length L and a steel tie rod AB with area 320 mm^2 . The angle θ can be adjusted to any desired value by varying the length of the tie rod and the vertical position of support A, but the initial length L does not change. Determine the angle θ in order that the vertical deflection of joint B will be a minimum under the action of the load P .
3. Compare the angle of twist ϕ_1 for a thin-walled circular tube (see Fig. 3) as calculated from the approximate equation, $\phi_1 = \tau L / 2\pi G r^3 t$, with the angle of twist ϕ_2 calculated from the exact equation $\phi_2 = \tau L / G I_p$. Express the ratio ϕ_1 / ϕ_2 in terms of the nondimensional ratio $\beta = r/t$.
4. A simple beam AB supports a uniform load of intensity $q = 6.0 \text{ kN/m}$ over a portion of the span (see Fig. 4). Assuming that $L = 10 \text{ m}$, $a = 4 \text{ m}$, and $b = 2 \text{ m}$, draw the shear-force and bending-moment diagrams for this beam.
5. The standpipe shown in Fig. 5 has inside diameter $d = 2 \text{ m}$ and wall thickness $t = 10 \text{ mm}$. What height h of water will produce a circumferential stress of 15 MPa in the wall of the pipe?

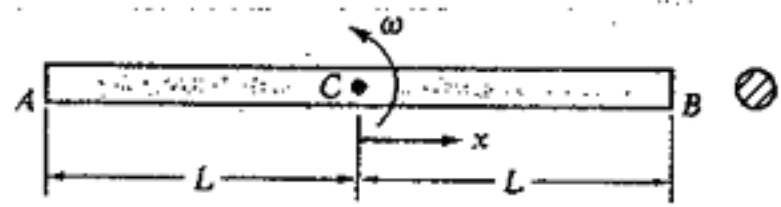


Fig. 1

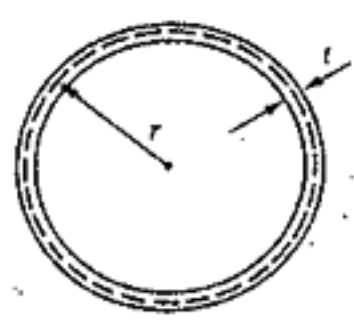


Fig. 3

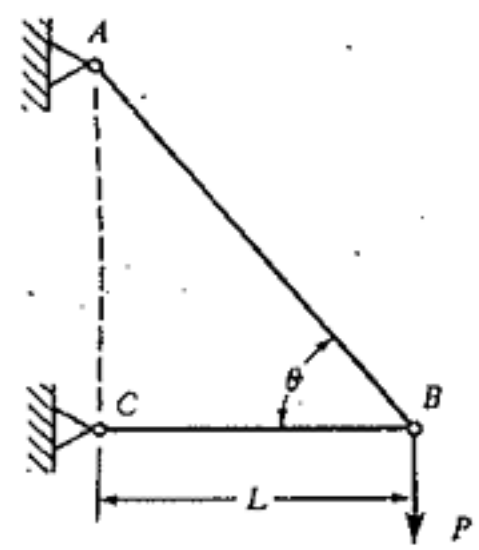


Fig. 2

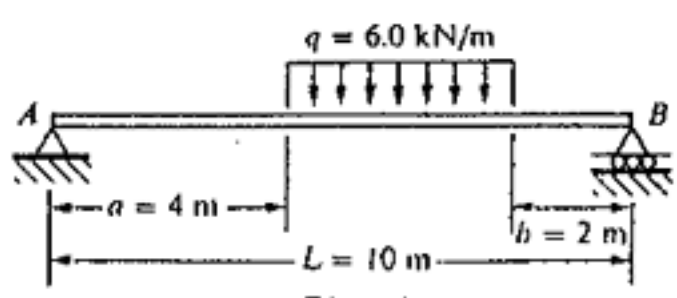


Fig. 4

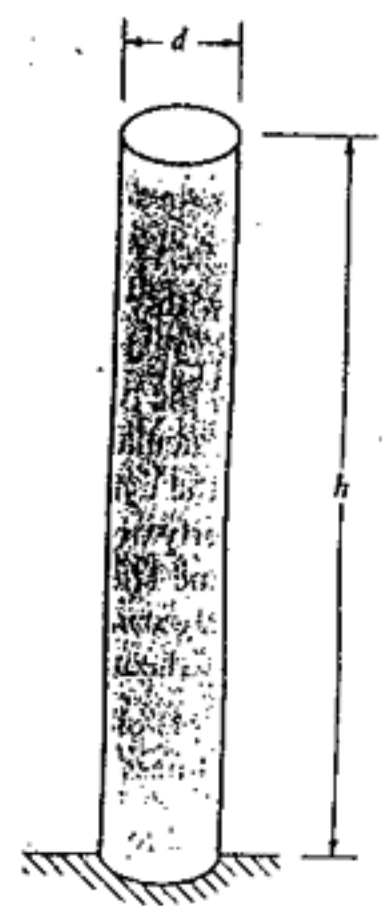


Fig. 5