

系所組別： 電腦與通信工程研究所丁組

考試科目： 電磁波

考試日期：0220，節次：2

※ 考生請注意：本試題 可 不可 使用計算機

## Problem 1 (20 Points)

The electric field component of an electromagnetic wave in free space is given by  $\vec{E}(y, z, t) = \hat{x}E_0 \cos(ay) \cos(\omega t - bz)$ . Note that this is not a uniform plane wave!

From Maxwell's equations, (a) find the corresponding magnetic field  $\vec{H}(y, z, t)$ , (b) find the relationship between the constant  $a$ ,  $b$ , and  $\omega$ . (c) Assume that this wave may be regarded as a sum of two uniform plane waves, determine the direction of propagation of the two component waves.

## Problem 2 (20 Points)

A lossy dielectric has an intrinsic impedance of  $200 \angle 30^\circ \Omega$  at a particular frequency. If, at that frequency, the plane wave propagating through the dielectric has the magnetic field component  $\vec{H} = 10e^{-\alpha x} \cos(\omega t - 0.5x) \hat{a}_y$  A/m. Find  $\vec{E}$  and  $\alpha$ . Determine the skin depth and wave polarization.

## Problem 3 (20 Points)

Show that the attenuation constants due to conductor and dielectric losses of a low-loss transmission line are given by  $\alpha_c \approx R / (2Z_0)$  and  $\alpha_d \approx Z_0 G / 2$ , where  $R$ ,  $L$ ,  $C$ , and  $G$  are the resistance, inductance, capacitance, and conductance per unit length of the line and  $Z_0 \equiv \sqrt{L/C}$ .

## Problem 4 (20 Points)

(a) What are the boundary conditions for the longitudinal fields of TE and TM modes in a uniform metallic waveguide? (b) Prove that a TEM mode can not propagate inside this kind of waveguides.

(背面仍有題目,請繼續作答)

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Problem 5 (20 Points)

An antenna has an input impedance of  $75 + j25$  ohms. (a) Locate this antenna load on Smith chart. (b) Find the admittance directly from Smith chart. (c) An engineer plans to match this antenna to a 50-ohm source by using a transmission-line section  $A$  and a short-circuited stub  $B$ . Assume that the characteristic impedance of all the transmission lines is 50 ohms. Find the required lengths of  $A$  and  $B$ . (d) What are the VSWR on the matching line  $A$  and stub  $B$ ? *Remember*: Write down every step of your reasoning and the result on a simplified Smith chart sketched on your answer sheet. Otherwise it can not be graded.

