編	號: 190,202,212 國立成功大學 103 學年度碩士班招生考試試題 共 / 頁,第 / 頁
系所組別: 電機工程學系、電腦與通信工程研究所甲丁組、電機資訊學院-微電奈米聯招	
考試科目:工程數學 考試日期:0222,節次:3	
*	考生請注意:本試題不可使用計算機。請於答案卷(卡)作答,於本試題紙上作答者,不予計分。
1.	(15 %) Solve the boundary value problem.
	$y'' - 9y = 0, y(-4) = y(4) = \cosh 12$
2.	(20%) Solve the initial value problem
	$Y''' - Y'' - 4y' + 4y = 6e^{-x}$, $y(0)=2$, $y'(0)=3$, $y''(0)=-1$
3.	(5%) (a)What kind of singularity (if any) does
	$f(z) = \frac{1}{2z} + \frac{1}{(2z)^2} + \frac{1}{(2z)^3} + \cdots$
	have at <i>z</i> = 0
	(10%) (b) Let $f(z) = \frac{1}{z^2(z+24)}$
	Find a Laurent series in powers of z which converges to f in region on $0 < z < 2$
4.	(20%) Evaluate $I = \int_0^\infty \frac{x^{1/3}}{(x+1)^2} dx$

- 5. (10%) Let f be continuous on [-L, L] and let f' be piecewise continuous. Suppose f(-L) = f(L). Prove that the Fourier series of f uniformly and absolutely converges to f.
- 6. (20%) Consider a circular membrance. Using polar coordinates, the particle of membrane at (r,θ) is assumed to vibrate vertical to the x, y plane, and its displacement from the rest position at time tis z(r, θ, t). The wave equation for this displacement function can be expressed as

$$\frac{\partial^2 z}{\partial t^2} = c^2 \left(\frac{\partial^2 z}{\partial r^2} + \frac{1}{r} \frac{\partial z}{\partial r} + \frac{1}{r^2} \frac{\partial^2 z}{\partial \theta^2} \right)$$

Where c is a constant. Assume that:

- \mathbb{P} The rest position of the membrane be in the x, y plane with origin at the center with radius R.
- \angle The motion of the membrane is symmetric about origin, in which case z depends only on r and t, i.e. $z(r, \theta, t) = z(r, t)$ and $\frac{\partial^2 z}{\partial \theta^2} = 0$.
- 丙、It is fastened onto a circular frame, i.e. z(R, t) = 0.
- T · It is set in motion with given initial position z(r, 0) = f(r) and velocity $\partial z(r, 0) / \partial t = g(r)$.

Solve this boundary value problem, i.e. find z(r, t).