## Problem 1：（20 Points）

Prove that（a）the four equations of Maxwell＇s equations are not totally independent，and（b） electromagnetic waves cannot penetrate a perfect conducting surface．

## Problem 2：（20 Points）

On a transmission line，the voltage wave is given by $V(\ell)=120 e^{0.0025 \ell} \cos \left(10^{8} t+2 \ell\right)+60 e^{-0.0025 \ell} \cos \left(10^{8} t-2 \ell\right)$ ，where $\ell$ is the distance from the load $Z_{L}(=300 \Omega)$ ．Find the attenuation constant $\alpha$ ，propagation constant $\beta$ ，phase velocity $v_{p}{ }^{\psi}$ ， characteristic impedance $Z_{0}$ ，and the current wave $I(\ell)$ ．

## Problem 3 （20 Points）

When a uniform plane wave in air is normally incident onto a planar lossless medium，the reflection coefficient is measured to be -0.25 ，and the phase velocity of the transmitted wave is reduced by a factor of 3 ．Find（a）the relative permittivity and the relative permeability of this lossless medium．（b） Design a match layer before this medium to reduce the reflection to zero．

## Problem 4 （20 Points）

（a）What is the maximum power that can be received over a distance of 1 km in free space with a $2.4-\mathrm{GHz}$ circuit consisting of a transmitting antenna with a gain of 20 dB and a receiving antenna with a gain of 10 dB ？The transmitted power is 1 Watt．（b）What are the effective aperture and beam solid angle of the receiving antenna if it is lossless？

## Problem 5：（20 Points）

A load consists of a variable $L$ and $R$ in series combination such that $\left|Z_{L}\right|=5$ ．It is connected to a transmission line with a characteristic impedance of $1 \Omega$ as shown on next page．（a）Show the possible locations of this load on a Smith chart normalized to $1 \Omega$ ．（b）As one proceeds toward the generator， which does he or she encounter first，a voltage maximum or a voltage minimum？Show why． A single short－circuited stub，with characteristic impedance of $1 \Omega$ ，is to be used for impedance matching by properly selecting the lengths $d_{1}$ and $d_{2}$ ．（c）What value of the load $Z_{L}$ will require the shortest distance $d_{1}$ to the stub and then（d）what will be the length $d_{2}$ of the stub？

## 第2頁，共2頁

（Note：you may use the Smith chart on this page for your calculations，temporarily．But don＇t forget to plot simplified Smith charts on your answer sheets to show your important procedures and results． Otherwise they cannot be graded．）


