

※ 考生請注意：本試題可使用計算機。請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

For your reference: $\epsilon_0 = 10^{-9}/36\pi$ (F/m); $\mu_0 = 4\pi \times 10^{-7}$ (H/m); $\eta_0 = 120\pi$ (Ω); $c = 3 \times 10^8$ (m/s)
 Permittivity $\epsilon (= \epsilon_r \epsilon_0)$; Permeability $\mu (= \mu_r \mu_0)$; Conductivity σ

- Let $\vec{D} = \epsilon \vec{E}$ and $\vec{B} = \mu \vec{H}$, please state the boundary conditions for the tangential components of \vec{E} and \vec{H} as well as the normal components of \vec{D} and \vec{B} . (10%)
- A constant voltage V_0 is applied to a partially filled parallel-plate capacitor shown in Fig. 1. The permittivity of the dielectric is ϵ , and the area of the plates is A . Find the force on the upper plate. (15%)

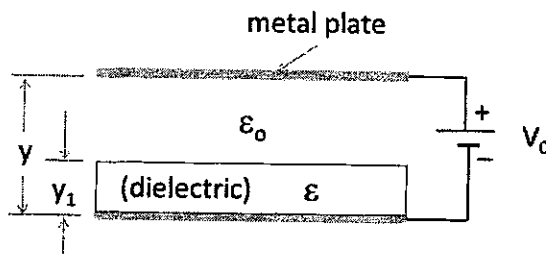


Fig. 1

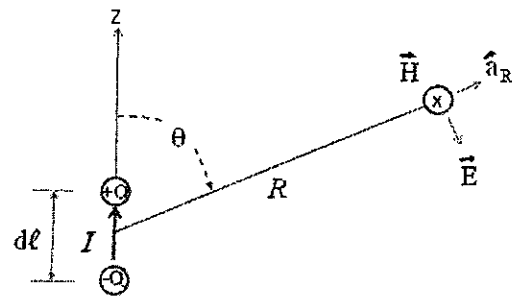


Fig. 2 A Hertzian dipole

- Express the magnetic energy density w_m in a dielectric (with μ) when \vec{H} is applied. (5%)
 - By using the stored magnetic energy, determine the inductance per unit length of an air coaxial transmission line that has a solid inner conductor of radius a and a very thin outer conductor of inner radius b . (10%)
- Given the electric field intensity \vec{E} , the magnetic field intensity \vec{H} , the volume charge density ρ , and the volume current density \vec{J} in free space, please write out the set of Maxwell's equations in the differential form. (8%)
 - In the source free condition (that is, $\rho = 0$ and $\vec{J} = 0$), please derive the wave equations for \vec{E} and \vec{H} from the Maxwell's equations. (7%)
- Find the current required to radiate a power of 50W at 100 MHz from a 0.01 (m) Hertzian dipole. (10%)
 - Find the magnitudes of \vec{E} and \vec{H} at $R = 100$ (m) and $\theta = 90^\circ$ as Fig. 2 shown. (10%)
- A C-band air-filled waveguide for use between 3.95 and 5.85 GHz with a cross-section area of 4.755 (cm) \times 2.215 (cm). Calculate the dominant mode cutoff frequency and the guided wavelength when the operation frequency is 4.2 GHz. (10%)
- Given that $\vec{H} = \hat{a}_y \cdot 2 \cos(15\pi x) \sin(8\pi \times 10^9 t - \beta z)$ (A/m) in air, please find \vec{E} and β . (15%)